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BASED ON FAST SIMULATED DIFFUSION**

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MOSFET Model Parameter Extraction Based on Fast Simulated Diffusion

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Abstract

A new algorithm, namely a Fast Simulated Diffusion (FSD) is proposed to solve a multi-minimal optimization problem on multi-dimensional continuous space. The algorithm performs a greedy search and a random search alternately and can give the global minimum with a practical success rate. A new efficient hill-descending method which is employed as the greedy search in the FSD is proposed. When the FSD is applied to a set of standard test functions, it shows an order of magnitude faster speed than the conventional simulated diffusion. Some of the optimization problems encountered in system and VLSI designs are classified into the multi-optimal problems. A MOSFET parameter extraction problem is one of them and the proposed FSD is successfully applied to the problem with a deep sub-micron MOSFET. A program listings are also attached.

1. Introduction

Some of the VLSI design problems including transistor sizing and model parameter extraction can be considered as an minimization problem in multi-dimensional continuous space with an object function which has plural local minima. Well-established minimization procedures for convex functions like Levenberg-Marquardt method[1], can be easily trapped in one of the local minima and thus can not find a global minimizer. Recently a method called 'simulated diffusion' (SD) has been proposed[2] to find the global minimum of a multi-minimal function on continuous space. The simulated diffusion is conceived by the stimulus of 'simulated annealing' (SA), which is for combinatorial optimization problems[3]. Although much efforts have been made to theoretically study the behavior of the SD[4,5] and it has been demonstrated theoretically that under certain conditions the method guarantees to find the global minimizer with a probability of unity, little is known about the practical aspects of the SD as an optimization procedure. Although the SD could find a global minimizer, it was very slow[2].

In this paper, a new optimization method, named Fast Simulated Diffusion (FSD), is proposed to provide a faster way to find the global minimum. The new method is successfully applied to MOSFET parameter extraction problem in the deep sub-micron regime.

In Section 2, the basic idea of the conventional SD is described. In Section 3, the algorithm of the fast SD is presented and the advantage of the fast SD over the conventional SD is clarified in Section 4. Section 5 is dedicated for the discussion on the application of the

proposed fast SD method to the practical VLSI design problems, namely a MOSFET model parameter extraction problem for a circuit simulator. A conclusion is summarized in Section 6.

2. Conventional Simulated Diffusion (CSD)

First, a basic idea of the conventional simulated diffusion is described. Essentially, the SD makes use of the physical fact that a particle placed in a given potential and with Brownian motion is diffused into the global minimum of the given potential profile. The following is the more mathematical formulation of the process. An differential equation which describes a diffusion process of a particle with Brownian motion is given as

$$dx = - \nabla f(x) dt + \sqrt{2T} dw , \quad (1)$$

where t is time, x is the space coordinate which points the location where the particle is, $f(x)$ is a potential function in which the particle is put, ∇ is a gradient operation, dw is a Gaussian random noise and T is a temperature. The first term on the left-hand side corresponds to the drift component of the movement and the second term signifies the Brownian movement. When the temperature is high, the second term dominates and the movement of the particle is just stochastic. On the other hand, when the temperature becomes low, the first term dominates and the process approaches pure hill-descent. The second term is essential to get out of the local minima and the first term gives the tendency to minimize the function.

It has been shown[4] that with a proper cooling schedule, the probability distribution of x , $P(x)$, approaches

$$P(x) \propto \exp\{-f(x) / T\} \quad (2)$$

as t goes infinity. This means that the limit distribution is independent of the initial value and is peaked around the global minimizers of $f(x)$. This in turn means that if dx is integrated over a long period of time, x tends to converge to a global minimum of the function $f(x)$. This is the principle of the conventional simulated diffusion. Aluffi-Pentini et al.[2] numerically integrated Eq.1 to obtain the minimizer from this first principle. However, the numerical process turned out to be slow.

If there are constraints in the original minimization problem, it is possible to introduce penalization functions and make it a minimization problem without constraints[6]. Consequently, the SD can be applicable not only to the unconstrained minimization problems but also to the optimization problems with constraints.

3. Fast Simulated Diffusion (FSD)

In this work, instead of integrating Eq.1 directly, two basic modifications are made. One is the introduction of an accept/non-accept function of a Boltzman distribution type, which is commonly used in the simulated annealing. If the next point $x_{next} (= x+dx)$ gives the smaller function value than the current x , take the x_{next} . On the other hand, if x_{next} gives the larger function value than the current x , generate a random number R in $[0,1]$ and calculate $P=\exp\{-\{f(x+dx)-f(x)\}/T\}$. If $R < P$, then accept the x_{next} , otherwise discard the x_{next} and re-generate x_{next} . The higher the function value becomes in the next move, the less probable it becomes to

accept the move. The introduction of this Boltzman accept/non-accept function can be validated by Eq.2 which is the Boltzmann distribution itself and it is expected to help establishing the probability distribution of Eq.2 faster than simply integrating Eq.1. In practice, the use of this accept/non-accept function prunes very 'stupid' moves to be taken otherwise and consequently accelerates the convergence.

The other modification is concerning with the generation of the next move. Instead of adding the greedy hill-descending part (the first term of Eq.1) and the random perturbation part (the second term of Eq.1), the generation of x based on a greedy method and a random method are carried out *alternately*. That is, in one time, dx is calculated by $-\nabla f(x)dt$ and the next time, dx is calculated as $\sqrt{2T} dw$. By generating the next move by the gradient method and the random method alternately, it is possible to achieve hill-descending even if the temperature is relatively high. In the relatively high temperature range, the random term happens to generate ineffective moves and it is probable that no improvements of $f(x)$ will be observed if the two terms are added together as in the CSD, because the hill-descending part can be hidden by the dominating random noise and all moves are possibly rejected.

Several considerations are taken other than the above-mentioned two major modifications to make the method more efficient. First, since it is expensive to calculate the direction of $\nabla f(x)$ if the space has large dimensions, $\langle \nabla f(x) \cdot \boldsymbol{r} \rangle \boldsymbol{r}$ is used instead, where \boldsymbol{r} is a unit vector of a randomly picked axis. This is because the expected direction of $\langle \nabla f(x) \cdot \boldsymbol{r} \rangle \boldsymbol{r}$ approaches $\nabla f(x)$ in a long run[2].

Secondly, since it is difficult to choose a good value of dt , a new hill-descending method is proposed and used. The choice of dt is critical because if it is too small, the improvement of the solution is small but if it is too big, $-\nabla f(x) dt$ does not always give the improvement. The proposed method is described in Fig.1. First, pick a random axis direction. If the function is concave at the point along the picked axis, quadratic fitting is carried out and the minimum x in that direction is guessed and adopted as the x_{next} . If the function is convex, choose a small dx first and double the dx until $f(x+dx)$ fails to decrease from $f(x)$. The doubling process is confined up to a certain number of times (three in the following examples). It is not an objective of this new hill-descending method to obtain the exact minimum in that direction but to provide an inexpensive yet effective way to improve the solution, since there is always a possibility that the random search can give rise to a big jump and then the previous hill-descending becomes wasteful. This method is considered as an inexpensive adaptive method to determine a good value of dt .

The detailed algorithm of the FSD is shown in Fig.2. In the first several external loops (around 10 loops), the hill-descending is not taken and only random search is carried out because big jumps are accepted in the high temperature stage and the hill-descending is not effective at all.

The initialization scheme and the temperature update algorithms in [7] are adopted. That is, the initial temperature, T_{init} , is determined by a statistics gathered over randomly selected N_{init} points as is shown in Fig.2. The adopted temperature update algorithm (cooling schedule) is basically a geometric decrease. The theory of the SD suggests that the cooling schedule

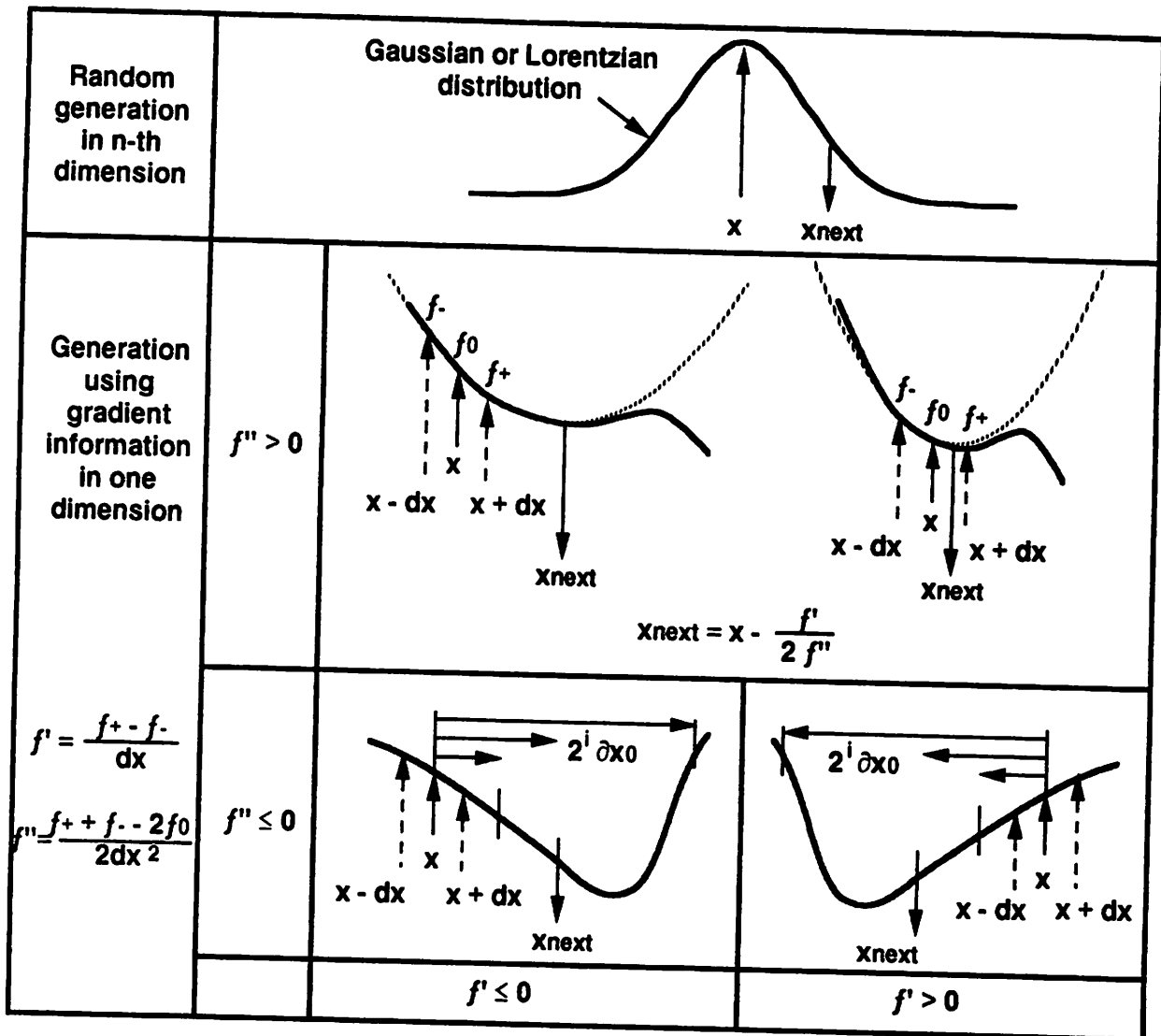


Fig. 1 Proposed hill-descending method using f' and f'' information

```

main {
  T = Tinit = ( $\kappa$  * (standard deviation of  $f(X)$  over randomly selected Ninit points));
                                     // Set initial temperature by using heuristics.  $\kappa = 0.2$ , Ninit=200
  S = Sinit;                          // Set initial S to Sinit
  Xinit = (Xinit_Given_by_User or one of those randomly selected Ninit points
           whichever gives the minimum value of  $f$ );
  Xopt = X = Xinit;                    // Set initial X to the best X known
  do {                                  // External loop with varying T
    iINT = 0;
    while (a certain times (ex. 15~25*dimension)) { // Internal loop with constant T
      iINT ++;
      Generate_X();                    // Generate new X by simulated diffusion
       $\Delta f = f(X_{new}) - f(X)$ ;
      if ( $\Delta f < 0$ ) {
        X = Xnew;                      // If cost decreases,
                                     // adopt the Xnew.
        if (  $f(X) < f(X_{opt})$  ) { Xopt = X } // Save best X.
      } else {
        P =  $\exp(-\Delta f / T)$ ;          // Even if cost increases,
                                     // adopt the Xnew
        R = random number in [0,1];    // according to
        if (R < P) {X = Xnew}          // Boltzman distribution.
      }
    }
    if (  $f(X) > f(X_{opt})$  ) { X = Xopt } // Resume the best X.
    if (cost is not improved considerably) {
      iLast_Gasp ++;                  // If cost is not improved considerably,
    } else {                          // take Last_Gasp loop,
      iLast_Gasp = 0;                // where T is increased a little
    }                                  // and then decreased to freeze.
    Update_T();
    Update_S();                      //  $S = Sinit * (T / Tinit)^a$ ;  $a = 0.5 \sim 1$  (ex.  $a=0.75$ )
  } until ((iLast_Gasp > iLast_Gasp_Max) and (T / Tinit < T_Ratio_Min) )
      // until Last_Gasp loop is taken long enough and T gets low enough.
  solution = Xopt;
}

Generate_X() {                        // generate new X
  if (iINT < mINT) {
    gradient_Flag = 0;
  } else {
    gradient_Flag = 1 - gradient_Flag;
  }
  if (gradient_Flag == 1) {
    Randomly select single variable  $X_i$  and move only in this axis.
    Generate Xnew with gradient information according to  $f''$  and  $f'$  values.
  } else {
    Xnew = X + S * (n-th dimensional Gaussian or Lorentzian distribution)
  }
}

Update_T() {                          // update temperature
  if (iLast_Gasp = 0) {
    T_Factor =  $\exp(-\lambda T / \sigma)$  // ex.  $\lambda=0.7$ ,  $\sigma$ =standard dev. of accepted  $f(x)$ 
    if (T_Factor < T_Factor_Min) { T_Factor = T_Factor_Min (=0.5) }
    T *= T_Factor
  }
  if ( 1  $\leq$  iLast_Gasp  $\leq$  n2) { T *= T_Factor2 (T_Factor2 > 1, ex. 1.3) } // ex. n2=4
  if (n2  $\leq$  iLast_Gasp) { T *= T_Factor1 (T_Factor1 < 1, ex. 0.75) }
}

```

Fig.2 Algorithm of Fast Simulated Diffusion

should be much slower the geometric decrease to guarantee to reach the global minimum even for ill-conditioned functions[11]. However, for practical problems, the geometric cooling works well [7,12].

The initial distribution of dw is chosen so that almost all the feasible space is covered by the random search at the initial stage. Such a distribution can be determined when the feasible region of x is given as a supercube, $[x_{min}, x_{max}]$. In practical problems, this feasible region is known apriori (see Section 5) or is set sufficiently large. If the randomly generated x falls out of the feasible region, it is re-generated. At the last stage of the FSD, when the object function shows little change, Last_Gasp sequence is taken where the temperature is increased a little and then decreased to freeze. The details are described in Fig.2.

In Fig.2, a multiplier S controls the random search space volume. S should be shrunked proportional to \sqrt{T} as T is lowered according to the first principle of the SD, but in practice, S can be shrunked faster and is proportional to T^n ($n = 0.5 \sim 1.0$).

4. Comparison between the FSD and the CSD

TABLE I shows a comparison between the FSD and the CSD when they are applied to a set of standard test functions given in [2]. On the average, the FSD is about an order of magnitude faster than the CSD. Let's define a 'reachability' as a probability to be able to find out the global minimum in a finite period of time using the given algorithm. Successful trials in ten trials in TABLE I can be used as an index for the reachability. Improvement in efficiency or

TABLE I Comparison of the conventional SD and the Fast SD

problem description			CSD (*1)	Fast Simulated Diffusion (this work)		
problem # (*1,2)	dimension	# of local minima	NF1: # of function evaluation	NF2: # of function evaluation (*3)	success rate in 10 trials (*4)	NF2/NF1 (%)
1	1	3	7168	3644	1.0	50.8
2	1	19	77699	2586	1.0	3.3
3	2	760	241215	3067	1.0	1.3
4	2	760	76894	2968	0.8	3.9
5	2	760	183819	2734	0.7	1.5
6	2	6	10822	4573	1.0	42.3
7	2	25	159549	3408	1.0	2.1
8	3	125	72851	3572	1.0	4.9
9	4	625	49690	3818	1.0	7.7
10	5	1e5	72226	5246	1.0	7.3
11	8	1e8	136061	9819	0.9	7.2
12	10	1e10	98985	12206	1.0	12.3
13	2	900	23770	4081	1.0	17.2
14	3	2.7e4	66010	4036	1.0	6.1
15	4	8.1e5	122166	4473	1.0	3.7
16	5	7.6e5	66365	4588	1.0	6.9
17	6	1.1e7	98974	5559	1.0	5.6
18	7	1.7e8	109886	6509	0.9	5.9
average	3.8	5.7e8	93009	4828	0.96	5.2

*1) F. Aluffi-Pentini, V.Parisi, & F.Zirilli, "Global Optimization and Stochastic Differential Equations ," J. of Optimization theory and Application, Vol.45, No.1, pp.1-16, Sept.1985.

*2) Expressions for problem # 4 and 5 presented in Aluffi-Pentini's paper seems to contain errors and hence they are modified and used.

*3) Average over 10 trials

*4) The rate of having reached to the global minimum in 10 trials. Aluffi-Pentini et al's paper does not contain this information. It only gives yes or no in one trial as the reachability information.

speed might be obtained at the risk of degradation in the reachability. Judging from TABLE I, the reachability of the FSD is in the practical range.

When the first term in Eq.1 is neglected, the method becomes similar to the SA. This SA-like method is supposed to be better than the mere extension of the SA to a continuous space[8], since the random search space is decreased by a factor of $\sqrt{2T}$ as the temperature is lowered. The FSD is faster than this SA-like method as shown TABLE II because less number of 'stupid' moves are generated. In TABLE II, the results of using a Lorentzian distribution[9] instead of the Gaussian distribution are also shown. Further improvement in both speed and reachability is observed. Since the Lorentian distribution has a longer tail than the Gaussian distribution, with the Lorentzian distribution, the possibility of a big jump is rather high even at the low temperature and it helps to get out of the local minima at the final stage.

5. Application to MOSFET Model Parameter Extraction

Model parameter extraction problem is to minimize the object function

$$f(p) = \sum_{\text{various bias conditions}} \text{weight}(\text{bias condition}) \cdot |I_{D,\text{measured}} - I_{D,\text{model}}(p)| \quad (3)$$

with the model parameters p as variables. In the above expression, I_D denotes drain current of a MOSFET and the weight function is optional. SPICE LEVEL3 MOS model is used as a MOS model in this section as an example, although the method is not restricted to a specific device models. The model parameters p that minimizes $f(p)$ is considered to be a good extracted parameter set and can be used for the circuit simulation afterwards. With the conventional

TABLE II Two modified version of the Fast Simulated Diffusion

problem #	NF1: # of function evaluation	Simulated Annealing-like random search			Simulated Diffusion with Lorentzian Distribution		
		NF3: # of function evaluation	success rate in 10 trials (Table I *4)	NF3 / NF1 (%)	NF4: # of function evaluation	success rate in 10 trials (Table I *4)	NF4 / NF1 (%)
1	7168	3111	1.0	43.4	2939	1.0	41.0
2	77699	3060	1.0	3.9	2387	1.0	3.1
3	241215	4131	0.7	1.7	2877	1.0	1.2
4	76894	5967	0.7	7.8	3170	0.8	4.1
5	183819	5831	0.7	3.2	2678	0.7	1.5
6	10822	5151	0.9	47.6	3609	1.0	33.4
7	159549	7701	0.9	4.8	3023	1.0	1.9
8	72851	11322	1.0	15.5	3232	1.0	4.4
9	49690	11475	1.0	23.1	3401	1.0	6.8
10	72226	20053	1.0	27.8	4108	1.0	5.7
11	136061	28689	0.9	21.1	7716	1.0	5.7
12	98985	33986	1.0	34.3	9856	1.0	10.0
13	23770	7378	1.0	31.0	3294	1.0	13.9
14	66010	10761	1.0	16.3	3446	1.0	5.2
15	122166	11424	1.0	9.4	4051	1.0	3.3
16	66365	14790	1.0	22.3	4140	1.0	6.2
17	98974	19730	1.0	19.9	4903	1.0	5.0
18	109886	22962	1.0	20.9	6295	1.0	5.7
average	93009	12640	0.93	13.6	4174	0.97	4.5

extraction program, the extracted parameters give the local minimum of $f(p)$ which is the nearest to the given an initial parameter set[1]. However, in practice, it is difficult to guess the initial parameter set correctly. The FSD does not require any initial value. All information needed beforehand is on the bounds, p_{min} and p_{max} , for each parameter. This is rather easy because it is known that, for example, the parameter KAPPA is in the range of 0~2. The used values for the bounds are tabulated in TABLE III. The same set of bounds is used to extract 0.25 μ m and 1 μ m MOSFET parameters.

In order to further increase the efficiency in this specific problem of parameter extraction, the search is carried out in the logarithmic space for NSUB, VMAX and NSS. This measure is taken to achieve a balanced search over a space because for example, VMAX is in the range of $1e4 \sim 1e8$ and the increase from $1e4$ to $1.1e4$ tends to generate the similar effect on $I_{D,model}$ as the increase from $1e7$ to $1.1e7$ does. For other parameters, the search is made in the linear scale.

The multi-minimal nature of the object function is shown in Fig.3 together with the generated x points with the FSD. An example of the fitted drain current is shown in Fig.4 for 1 μ m MOSFET. Figure 5 shows another example of the parameter extraction with a 0.25 μ m channel-length MOSFET[10]. Good agreement is observed even down to the deep sub-micron region.

6. Conclusions

Fast simulated diffusion is proposed to provide a fast method to find a global minimum of a multi-minimal function on multi-dimensional continuous space. The fast simulated diffusion

TABLE III MOSFET model parameter extraction results

parameter name	P_{min}	P_{max}	extracted params for 1 μ m MOS	extracted params for 0.25 μ m MOS
VTO	0	1.5	0.769	0.743
UO	10	1000	900	406
NSUB	1e16	1e20	1.80e17	5.97e18
GAMMA	0.2	1.5	0.928	0.477
ETA	0	2	0.0293	0.00754
THETA	0	2	0.996	0.775
KAPPA	0	2	0.382	0.299
VMAX	1e4	1e8	5.26e7	1.81e5
XJ	1e-8	3e-8	2e-7(fixed)	2.02e-8
TOX	-	-	2e-8(fixed)	5e-9(fixed)
NFS	-	-	0(fixed)	0(fixed)
LD	-	-	0.1(fixed)	0(fixed)
W	-	-	10e-6(fixed)	4e-6(fixed)
L	-	-	1.0e-6(fixed)	0.25e-6(fixed)
# of func. eval.	-	-	4258	3114
time (min.*MIPS)	-	-	~18	~13

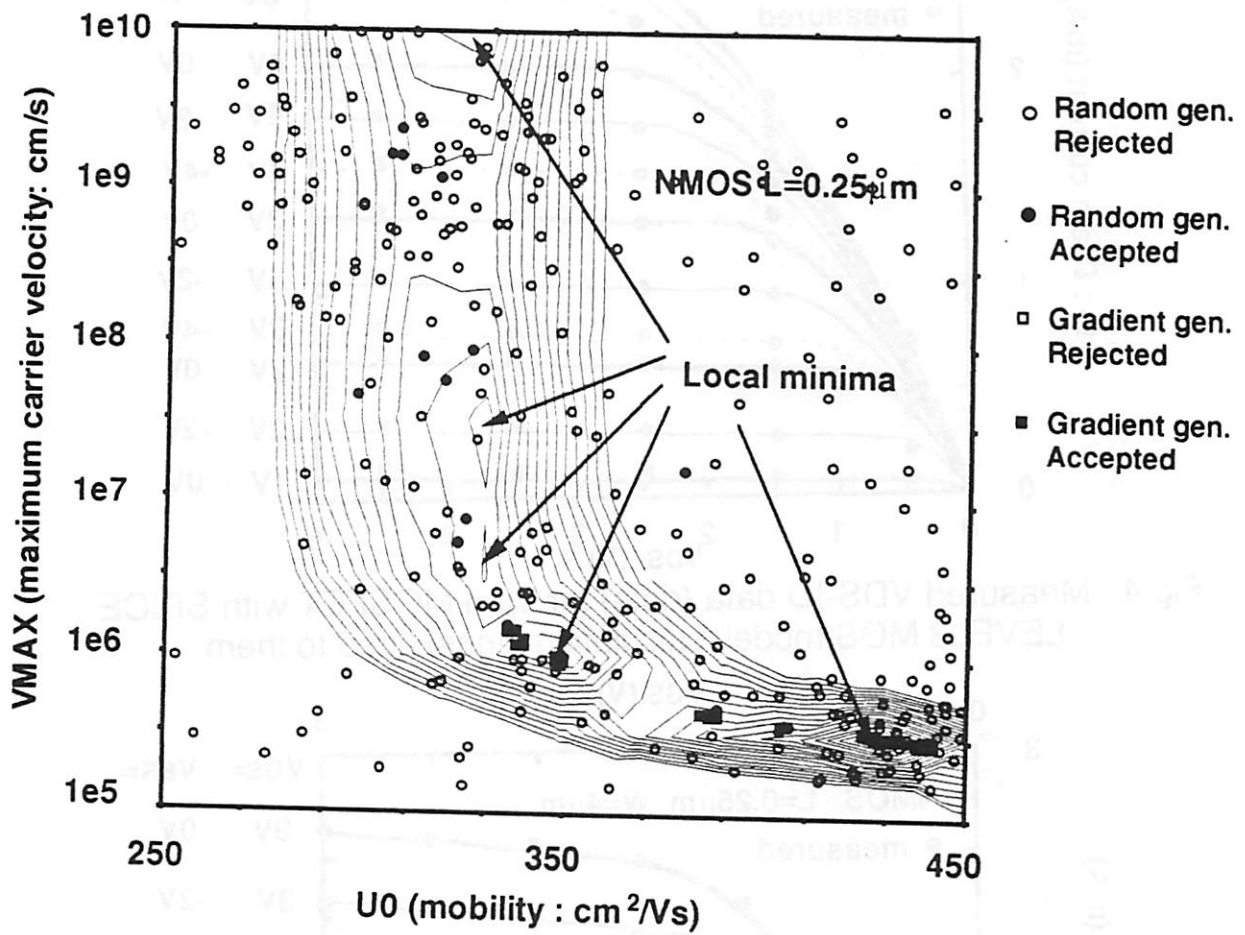


Fig.3 Multiple-minimum nature of MOS model parameter extraction problem and generated x points

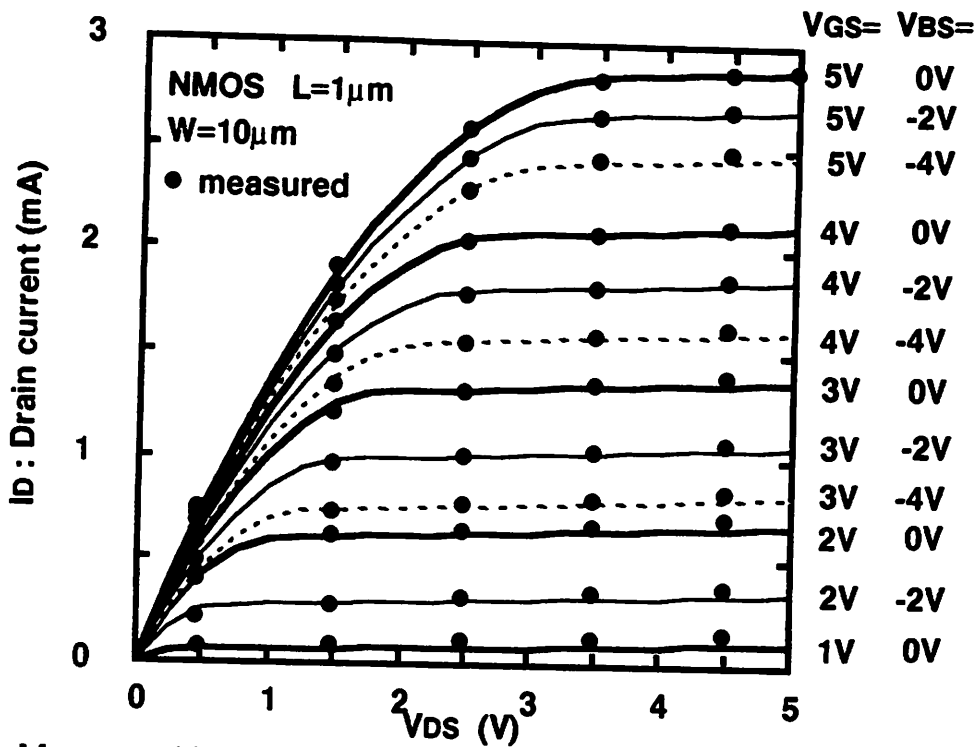


Fig.4 Measured V_{DS} - I_D data (dots) for $1\mu\text{m}$ MOSFET with SPICE LEVEL3 MOS model calculation (lines) fitted to them

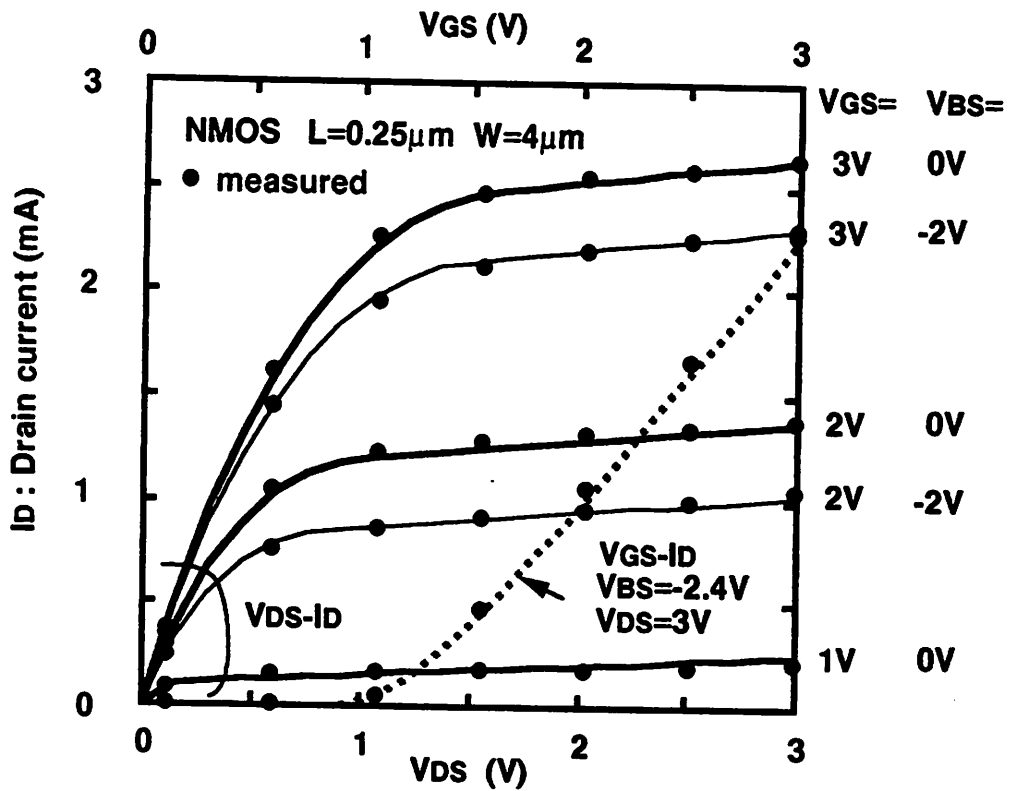


Fig.5 Measured V_{DS} - I_D data (dots) for $0.25\mu\text{m}$ MOSFET with SPICE LEVEL3 MOS model calculation (lines) fitted to them

shows about an order of magnitude faster speed over the conventional simulated diffusion, when applied to a set of standard test functions. The fast simulated diffusion is successfully applied to MOSFET model parameter extraction in the deep submicron region. The method is supposed to be applicable to other optimization problems encountered in system and VLSI designs.

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Appendix A Program Listing

Program source codes are shown in the following pages. The programs are written in QuickBasic Ver.1.0 for Macintosh SE/30. There are two programs. The first one is a simulated diffusion program for a set of test functions, which corresponds to Section 4 of this paper. The second one is a simulated diffusion program to extract device parameters for MOSFET LEVEL3 model which is found in SPICE 2 and SPICE3 circuit simulators. This program corresponds to Section 5 of the paper.


```

'--- Minimization with simulated annealing ---
OPTION BASE 0
maxnX% = 14
maxnData% = 1000
maxnEXT% = 100
DIM SHARED oldX(maxnX%), newX(maxnX%), oldEXTX(maxnX%)
DIM SHARED optEXTX(maxnX%), optINTX(maxnX%)
DIM SHARED minX(maxnX%), maxX(maxnX%), initX(maxnX%),
x(maxnX%), rangeX(maxnX%)
DIM SHARED histEXTCost(maxnEXT%), histINTACost(maxnData%)
DIM SHARED vgsM(maxnData%), vdsM(maxnData%), vbsM(maxnData%)
DIM SHARED idM(maxnData%), ivgdbM(maxnData%),
weightM(maxnData%)
DIM SHARED iX2iV(maxnX%+1), iV2iX(maxnX%+1)
DIM SHARED minV(maxnX%), maxV(maxnX%), initV(maxnX%),
nameVS(maxnX%)
DIM SHARED iIne%, ntokenMax%
DIM SHARED maxVgd, maxids
ntokenMax% = 6
DIM tokenS(ntokenMax%)

Initializer:
  reed% = 17635
  infinity = 1E+20
  infinitesimal = 1E-20
  initTK = .1
  updateTLambda = .7
  factorUpdateTLB = .5
  epsExitEXTrelCost = .02
  minnEXT% = 5
  iGaussCalled% = 0
  iGenerateXCaled% = 0
  epsFindFac = 1!
  '--- mos3 initialization ---
  nXP% = 14
  iVto% = 1: insub% = 2: igammac% = 3: iuo% = 4: itheta% = 5
  ikappa% = 6: ivmax% = 7: ieta% = 8: ix% = 9: id% = 10
  iox% = 11: ifns% = 12: iF% = 13: iw% = 14
  ialP% = 15
  CALL initializeV(iVto%, "vto", -2!, 2!, .8)
  CALL initializeV(insub%, "nsub", 1E+16, 1E+20, 1E+18)
  CALL initializeV(igammac%, "gamma", 0!, 2!, .5)
  CALL initializeV(iuo%, "uo", 10!, 1600!, 400!)
  CALL initializeV(itheta%, "theta", 0!, 2!, .7)
  CALL initializeV(ikappa%, "kappa", 0!, 2!, .5)
  CALL initializeV(ivmax%, "vmax", 100000!, 1E+08, 1000000!)
  CALL initializeV(ieta%, "eta", 0!, 2!, 1!)
  CALL initializeV(ix%, "x", 0!, .00001, 0!)
  CALL initializeV(id%, "d", 0!, .00001, 0!)
  CALL initializeV(iox%, "tox", 1E-10, .0000001, 3E-08)
  CALL initializeV(ifns%, "ifs", 0!, 0!, 0!)
  CALL initializeV(iF%, "F", 0!, .0001, .000001)
  CALL initializeV(iw%, "w", 0!, .001, .00001)
  iX2iV(ialP%) = ialP%
  iV2iX(ialP%) = ialP%

  pi = 3.141592
  q = 1.6E-19
  vtherm = .025
  ni = 1.45E+10 * 1000000!
  epsi = 8.855E-12 * 11.9
  epsox = 8.855E-12 * 3.9

Windower:
'--- initialize window 1, 2 ---
WINDOW 3, "Text Window", (0,30)-(480,300),1
TEXTSIZE 9
WINDOW 2, "Graphics Window", (200,30)-(480, 310),3
TEXTSIZE 9
PICTURE ON
WINDOW 1, "Report Window", (0,30)-(200, 300),1
'--- initialize I/O ---
TEXTSIZE 9
OPEN "scm." FOR OUTPUT AS #1

'--- menu ---
MENU 1,0,1, "File"
MENU 2,0,1, "Edit"
MENU 3,0,1, "Run"
MENU 4,0,0, "Params"
MENU 5,0,1, "Graph"

MENU 1,1,1, "Load": cmdkey 1,1, "L"

MENU 1,2,1, "Show Loaded Data": cmdkey 1,2, "S"
MENU 1,3,1, "Output Select": cmdkey 1,3, "O"
MENU 1,4,0, "Print": cmdkey 1,4, "P"
MENU 1,5,0, "-"
MENU 1,6,1, "Quit": cmdkey 1,6, "Q"

MENU 2,1,1, "Copy": cmdkey 2,1, "C"

MENU 3,1,1, "Simulated Diff."
MENU 3,2,1, "Manual Fit"
MENU 3,3,1, "Contour Map"
MENU 3,4,1, "Write Results"

MENU 4,1,0, "Params Set": cmdkey 4,1, "M"

MENU 5,1,1, "Vds_id": cmdkey 5,1, "G"
MENU 5,2,1, "Vgs_id": cmdkey 5,2, "H"

ON MENU GOSUB Menucheck: MENU ON
Idle:
  GOTO Idle

Menucheck:
  menunumber = MENU(0)
  menuitem = MENU(1)
  MENU
  ON menunumber GOSUB Filer, ClipBoarder, Runner, Setter, Grapher
RETURN

Filer:
  ON menuitem GOSUB Loader, DataShower, Outer, Quitter, Quitter
  Quitter
RETURN

ClipBoarder:
  ON menuitem GOSUB ClipCopier
RETURN

Runner:
  ON menuitem GOSUB SDRunner, Manualer, Contourer, ResShower
RETURN

Setter:
  ON menuitem GOSUB Quitter
RETURN

Grapher:
  ON menuitem GOSUB Vdslder, Vgslder
RETURN

ClipCopier:
  PICTURE OFF
  image$ = PICTURES
  OPEN "CLIP:PICTURE" FOR OUTPUT AS #3
  PRINT #3, image$
  CLOSE #3
RETURN

Eraser:
  WINDOW 3
  WINDOW 2
  WINDOW 1
  image$ = ""
  CLS
RETURN

Loader:
'--- load data ---
infile$ = FILE$(1, "TEXT")
IF (infile$ = "") THEN RETURN
OPEN infile$ FOR INPUT AS #2
'--- input ---
skipLoadFlag% = 0
idata% = 0
iX% = 0: iF% = nXP% + 1

```

```

line% = 0
WHILE NOT EOF(2)
LINE INPUT #2, inline$
line% = line% + 1
'--- parse the input line ---
CALL parse(inline$, tokens$, ntokens$, errorParseFlag%)
IF (errorParseFlag% = 1) GOTO breakLoadLoop
IF (tokens$(1) = "I") OR (tokens$(1) = "P") THEN skipLoadFlag% = 1
IF (ntokens% <> 0) AND (tokens$(1) <> "I") AND (skipLoadFlag% = 0)
THEN
IF (tokens$(2) = "V") THEN
'--- voltage card ---
SELECT CASE UCASE$(tokens$(1))
CASE "VGS"
IF (tokens$(3) = "") THEN ivgdb% = 1 ELSE vgs = VAL(tokens$(3))
CASE "VDS"
IF (tokens$(3) = "") THEN ivgdb% = 2 ELSE vds = VAL(tokens$(3))
CASE "VBS"
IF (tokens$(3) = "") THEN ivgdb% = 3 ELSE vbs = VAL(tokens$(3))
'--- variable parameter card ---
CASE "VTO"
CALL paramRead(tokens$, D%, IP%, Ito%)
CASE "NSUB"
CALL paramRead(tokens$, D%, IP%, insub%)
CASE "GAMMA"
CALL paramRead(tokens$, D%, IP%, igammac%)
CASE "UO"
CALL paramRead(tokens$, D%, IP%, iuo%)
IF (minX(IV2D%(iuo%)) <= 10!) THEN
minX(IV2D%(iuo%)) = 10!
END IF
CASE "THETA"
CALL paramRead(tokens$, D%, IP%, itheta%)
CASE "KAPPA"
CALL paramRead(tokens$, D%, IP%, ikappa%)
CASE "VMAX"
CALL paramRead(tokens$, D%, IP%, ivmax%)
CASE "ETA"
CALL paramRead(tokens$, D%, IP%, ista%)
CASE "XJ"
CALL paramRead(tokens$, D%, IP%, bxj%)
IF (minX(IV2D%(bxj%)) <= 0) THEN minX(IV2D%(bxj%)) =
infinitesimal
CASE "LD"
CALL paramRead(tokens$, D%, IP%, lid%)
CASE "TOX"
CALL paramRead(tokens$, D%, IP%, itox%)
CASE "NFS"
CALL paramRead(tokens$, D%, IP%, infsa%)
CASE "L"
CALL paramRead(tokens$, D%, IP%, l%)
CASE "W"
CALL paramRead(tokens$, D%, IP%, iw%)
CASE ELSE
msg$ = "Undefined token "+tokens$(1)+" in line"+STR$(line%)
CALL errmsg(msg$)
GOTO breakLoadLoop
END SELECT
ELSE
'--- real data ---
idata% = idata% + 1
vgs(m(idata%)) = vgs
vds(m(idata%)) = vds
vbs(m(idata%)) = vbs
ivgdb(m(idata%)) = ivgdb%
SELECT CASE ivgdb%
CASE 1
vgs(m(idata%)) = VAL(tokens$(1))
CASE 2
vds(m(idata%)) = VAL(tokens$(1))
CASE 3
vbs(m(idata%)) = VAL(tokens$(1))
END SELECT
idm(idata%) = VAL(tokens$(2))
IF (tokens$(3) = "I") THEN
weightm(idata%) = 1!
ELSE
weightm(idata%) = VAL(tokens$(3))
END IF
END IF
ELSE
IF (tokens$(1) = "I") THEN skipLoadFlag% = 0
END IF

```

```

WEND
breakLoadLoop:
'--- post-processing of the input ---
IF (idata% > 0) THEN ndata% = idata% ELSE CALL errmsg("No measured
data.")
IF (IP% - D% <> 1) THEN CALL errmsg("Parameters or variables
missing.")
nX% = D%: sP% = IP%: nP% = nX%
'--- define markov chain length ---
'ninitRND% = nX% * 50
'maxniNT% = nX% * 24
'ninitRND% = 200
'maxniNT% = nX% * 15
CLOSE #2
'--- put initial X into X ---
FOR D% = 1 TO nX%
x(D%) = iniX(D%)
rangeX(D%) = maxX(D%) - minX(D%)
NEXT
RETURN

X2V:
vto = x(IV2D%(Ito%))
nsub = x(IV2D%(insub%)) * 100000!
gammac = x(IV2D%(igammac%))
uo = x(IV2D%(iuo%)) * .0001
theta = x(IV2D%(itheta%))
kappa = x(IV2D%(ikappa%))
vmax = x(IV2D%(ivmax%))
eta = x(IV2D%(ista%))
xj = x(IV2D%(bxj%))
ld = x(IV2D%(lid%))
tox = x(IV2D%(itox%))
nfs = x(IV2D%(infsa%)) * 1000!
l = x(IV2D%(l%))
w = x(IV2D%(iw%))
RETURN

DataShower:
'--- show loaded data ---
WINDOW 3
PRINT CHR$(13) + CHR$(13) + CHR$(13) + CHR$(13)
PRINT "-----"
PRINT "Click mouse to pause."
PRINT "-----"
'--- show parameter info ---
FOR D% = 1 TO nX%
DataShowerLoop1:
IF (MOUSE(0) <> 0) GOTO DataShowerLoop1
NEXT
FOR IP% = sP% TO nP%
PRINT #1, nameVS(D2IV%(D%), minX(D%), maxX(D%), iniX(IP%))
DataShowerLoop2:
IF (MOUSE(0) <> 0) GOTO DataShowerLoop2
NEXT
'--- show measured data ---
PRINT #1, "vgs", "vds", "vbs", "ld", "weight", "ivgdb"
FOR idata% = 1 TO ndata%
PRINT #1, vgs(m(idata%)), vds(m(idata%)), vbs(m(idata%)), idm(idata%),
weightm(idata%), ivgdb(m(idata%))
DataShowerLoop3:
IF (MOUSE(0) <> 0) GOTO DataShowerLoop3
NEXT
'--- show other critical info ---
PRINT #1, "nX%="; nX%
RETURN

ResShower:
'--- show result data ---
OPEN "mosfil.gr" FOR OUTPUT AS #5
'--- Vds - Id graph ---
vgs(m(0)) = infinity: vds(m(0)) = infinity: vbs(m(0)) = infinity
igrph% = 0
'--- calculate vdsmax & vgsmax ---
vdsmax = 0: vgsmax = 0
FOR idata% = 1 TO ndata%
IF (vgs(m(idata%)) > vgsmax) THEN vgsmax = vgs(m(idata%))
IF (vds(m(idata%)) > vdsmax) THEN vdsmax = vds(m(idata%))
NEXT
FOR idata% = 1 TO ndata%
vgs = vgs(m(idata%))
vds = vds(m(idata%))

```

```

vbs = vbem(idata%)
ivgdb% = ivgdbm%(idata%)
SELECT CASE ivgdb%
CASE 1
  '--- changing vgs ---
  IF (vds < vdsmin(idata%-1)) OR (vbs < vbem(idata%-1)) OR (ivgdb%
  < ivgdbm%(idata%-1)) THEN
    igrph% = igrph% + 1
    FOR vgs = 0 TO vgsmax*1.001 STEP vgsmax/20
      GOSUB Mos3
      PRINT #5, vgs, ids
    NEXT
    PRINT #5, ""
  END IF
CASE 2
  '--- changing vds ---
  IF (vgs < vgsmin(idata%-1)) OR (vbs < vbem(idata%-1)) OR (ivgdb%
  < ivgdbm%(idata%-1)) THEN
    igrph% = igrph% + 1
    FOR vds = 0 TO vdsmax*1.001 STEP vdsmax/20
      GOSUB Mos3
      PRINT #5, vds, ids
    NEXT
    PRINT #5, ""
  END IF
END SELECT
NEXT
'--- show parameter info ---
FOR idata% = 1 TO ndata%
  igrph% = igrph% + 1
  PRINT #5, "Line_n_type_marker_label": igrph%, "1"; "31"; idata%
  IF (ivgdbm%(idata%) = 1) THEN
    PRINT #5, vgsmin(idata%)*1!, idm(idata%)
    PRINT #5, vgsmax(idata%)*1!, idm(idata%)
  END IF
  IF (ivgdbm%(idata%) = 2) THEN
    PRINT #5, vdsmin(idata%)*1!, idm(idata%)
    PRINT #5, vdsmax(idata%)*1!, idm(idata%)
  END IF
  PRINT #5, ""
NEXT
CLOSE #5
SetCreate "mosfit.gr", "MSWD"
'--- print out parameters ---
OPEN "mosfit.par" FOR OUTPUT AS #4
FOR i% = 1 TO nX%
  PRINT #4, nameVS(X2i%*(i%)), x(i%)
NEXT
PRINT #4, ""
FOR i% = sP% TO nP%
  PRINT #4, nameVS(X2i%*(i%)), x(i%)
NEXT
PRINT #4, ""
'--- print out important info ---
PRINT #4, "c="; oldEXT Cost; "T="; oldT; "ave="; aveINTACost
PRINT #4, "E="; iEXT%; "PF="; epsRndFac; "s="; sigmaINTACost
PRINT #4, "Gasp="; iLastGasp%; "iCoat="; iCoat&
PRINT #4, "iAccept"; iAccept%; "gAccept"; gAccept%
PRINT #4, "exitEXTrelCoat"; exitEXTrelCoat
CLOSE #4
SetCreate "mosfit.par", "MSWD"
RETURN

```

```

Vdslder:
'--- Vds - Id graph ---
WINDOW 3
INPUT "Vbs": vbs
INPUT "Vgsmin, Vgsmax, Vgsstep": vgsmin, vgsmax, vgsstep
INPUT "Vdsmin, Vdsmax, Vdsstep": vdsmin, vdsmax, vdsstep
FOR vgs = vgsmin TO vgsmax STEP vgsstep
  FOR vds = vdsmin TO vdsmax STEP vdsstep
    GOSUB Mos3
    PRINT #1, vds, ids
  NEXT
NEXT
PRINT #1, ""
NEXT
RETURN

```

```

Vgslder:
'--- Vgs - Id graph ---
WINDOW 3
INPUT "Vds": vds
INPUT "Vbsmin, Vbsmax, Vbsstep": vbsmin, vbsmax, vbsstep

```

```

INPUT "Vgsmin, Vgsmax, Vgsstep": vgsmin, vgsmax, vgsstep
FOR vbs = vbsmin TO vbsmax STEP vbsstep
  FOR vgs = vgsmin TO vgsmax STEP vgsstep
    GOSUB Mos3
    PRINT #1, vgs, ids
  NEXT
NEXT
PRINT #1, ""
NEXT
RETURN

```

```

Outer:
'--- output device select ---
WINDOW 3
PRINT "Output to screen(0)"
INPUT "or new file(1) or append to a file(2) or to printer(2)": outdev%
CLOSE #1
SELECT CASE outdev%
CASE 0
  OPEN "scm:" FOR OUTPUT AS #1
CASE 1
  outfile$ = FILE$(0)
  IF (outfile$ = "") THEN
    CALL errmsg("File not found.")
    RETURN
  ELSE
    OPEN outfile$ FOR OUTPUT AS #1
    PRINT #1, "; PRINT #1, ""
  END IF
CASE 2
  outfile$ = FILE$(1, "TEXT")
  IF (outfile$ = "") THEN
    CALL errmsg("File not found.")
    RETURN
  ELSE
    OPEN outfile$ FOR APPEND AS #1
    PRINT #1, "; PRINT #1, ""
  END IF
CASE 3
  OPEN "pt1:" FOR OUTPUT AS #1
CASE ELSE
  OPEN "scm:" FOR OUTPUT AS #1
END SELECT
RETURN

```

```

Manualer:
'--- manual fitting ---
WINDOW 1
INPUT "maximum ids for graph": maxIds
vgsmin(0) = infinity: vdsmin(0) = infinity: vbsmin(0) = infinity
'--- calculate vdsmax & vgsmax ---
vdsmax = 0: vgsmax = 0
FOR idata% = 1 TO ndata%
  IF (vgsmin(idata%) > vgsmax) THEN vgsmax = vgsmin(idata%)
  IF (vdsmin(idata%) > vdsmax) THEN vdsmax = vdsmin(idata%)
NEXT
IF (vdsmax > vgsmax) THEN maxVgd = vdsmax ELSE maxVgd = vgsmax
'--- maxVgd & maxIds given ---
'--- fitting loop ---
ManualFitLoop:
WINDOW 1
PRINT "Variables"
FOR i% = 1 TO nX%
  PRINT nameVS(X2i%*(i%)), "="; x(i%);
  INPUT ss$
  IF (ss$ <> "") THEN
    valls = VAL(ss$)
    x(i%) = valls
  END IF
NEXT
PRINT "Parameters"
FOR i% = sP% TO nP%
  PRINT nameVS(X2i%*(i%)), "="; x(i%);
  INPUT ss$
  IF (ss$ <> "") THEN
    valls = VAL(ss$)
    x(i%) = valls
  END IF
NEXT
FOR i% = 1 TO nXP%
  PRINT nameVS(X2i%*(i%)), "="; x(i%)
NEXT
'--- plotting measured data ---
WINDOW 2

```

```

marksize% = 2
FOR idata% = 1 TO ndata%
  ivgdb% = ivgdbm%(idata%)
  igraph% = igraph% + 1
  IF (ivgdbm%(idata%) = 1) THEN vv = vgsm(idata%)
  IF (ivgdbm%(idata%) = 2) THEN vv = vdsb(idata%)
  ii = idm(idata%)
  CALL User2World(vv, ii, wx%, wy%)
  SetRect rec%(0), wx%-marksize%, wy%-marksize%
  marksize%, wx%+marksize%, wy%+marksize%
  IF (ivgdb% = 1) THEN
    CALL PAINTOVAL(VARPTR(rec%(0)))
  ELSE
    CALL FRAMEOVAL(VARPTR(rec%(0)))
  END IF
NEXT
'--- plot calculated point ---
FOR idata% = 1 TO ndata%
  vgs = vgsm(idata%)
  vds = vdsb(idata%)
  vbs = vbsm(idata%)
  ivgdb% = ivgdbm%(idata%)
  SELECT CASE ivgdb%
  CASE 1
    '--- changing vgs ---
    IF (vds <> vdsb(idata%-1)) OR (vbs <> vbsm(idata%-1)) OR
    (ivgdb% <> ivgdbm%(idata%-1)) THEN
      PENSIZE 1.1
      vgs = 0
      GOSUB Mos3
      CALL User2World(vgs, ids, wx%, wy%)
      MOVETO wx%, wy%
      FOR vgs = 0 TO vgsmax*1.001 STEP vgsmax/20
        GOSUB Mos3
        CALL User2World(vgs, ids, wx%, wy%)
        LINETO wx%, wy%
      NEXT
    END IF
  CASE 2
    '--- changing vds ---
    IF (vgs <> vgsm(idata%-1)) OR (vbs <> vbsm(idata%-1)) OR
    (ivgdb% <> ivgdbm%(idata%-1)) THEN
      PENSIZE 2.2
      vds = 0
      GOSUB Mos3
      CALL User2World(vds, ids, wx%, wy%)
      MOVETO wx%, wy%
      FOR vds = 0 TO vdsmax*1.001 STEP vdsmax/20
        GOSUB Mos3
        CALL User2World(vds, ids, wx%, wy%)
        LINETO wx%, wy%
      NEXT
    END IF
  END SELECT
NEXT
MOVETO 5,20
INPUT "Try Again(0) or Exit(1)": ss$
IF (ss$ = "1") THEN GOTO BreakManualFitLoop
GOTO ManualFitLoop
BreakManualFitLoop:
RETURN

Contourer:
'--- Contour output ---
ContourLoop:
WINDOW 3
FOR Dx% = 1 TO nXP%
  PRINT nameVS(Dx2V%(Dx%)):"="x(Dx%);
  INPUT ss$
  IF (ss$ <> ") THEN x(Dx%) = VAL(ss$)
NEXT
FOR Dx% = 1 TO nXP%
  PRINT "var#="Dx%," nameVS(Dx2V%(Dx%)):"="x(Dx%)
NEXT
'--- select variables ---
ilogXc% = 0; ilogYc% = 0; ilogZc% = 0
ix% = 1: PRINT "X var " nameVS(Dx2V%(Dx%)); INPUT ss$: IF (ss$ <>
") THEN Dx% = VAL(ss$)
INPUT "linear or log(1)": ss$: IF (ss$ = "1") THEN ilogXc% = 1
minXc = minX(Dx%): PRINT "minX",minXc: INPUT ss$: IF (ss$ <> ")
THEN minXc = VAL(ss$)
maxXc = maxX(Dx%): PRINT "maxX",maxXc: INPUT ss$: IF (ss$ <> ")
THEN maxXc = VAL(ss$)

IF (ilogXc% = 1) THEN stepXc = EXP(LOG(maxXc/minXc)/10) ELSE
stepXc = rangeX(Dx%)/10
PRINT "stepX",stepXc: INPUT ss$: IF (ss$ <> ") THEN stepXc =
VAL(ss$)
ix% = 2: PRINT "Y var " nameVS(Dx2V%(Dx%)); INPUT ss$: IF (ss$ <>
") THEN Dy% = VAL(ss$)
INPUT "linear or log(1)": ss$: IF (ss$ = "1") THEN ilogYc% = 1
minYc = minX(Dy%): PRINT "minY",minYc: INPUT ss$: IF (ss$ <> ")
THEN minYc = VAL(ss$)
maxYc = maxX(Dy%): PRINT "maxY",maxYc: INPUT ss$: IF (ss$ <> ")
THEN maxYc = VAL(ss$)
IF (ilogYc% = 1) THEN stepYc = EXP(LOG(maxYc/minYc)/10) ELSE
stepYc = rangeX(Dy%)/10
PRINT "stepY",stepYc: INPUT ss$: IF (ss$ <> ") THEN stepYc =
VAL(ss$)
INPUT "Z-axis linear or log(1)": ss$: IF (ss$ = "1") THEN ilogZc% = 1
'--- print out input param ---
PRINT "X var = " nameVS(Dx2V%(Dx%))
PRINT "min,max,step,log=";minXc,maxXc,stepXc,ilogXc%
PRINT "Y var = " nameVS(Dx2V%(Dy%))
PRINT "min,max,step,log=";minYc,maxYc,stepYc,ilogYc%
PRINT "Z-axis log=";ilogZc%
INPUT "OK or Try Again(1)": ss$
IF (ss$ = "1") THEN GOTO ContourLoop
'--- output xyz file for contour 81 ---
OPEN "mosfit.cont" FOR OUTPUT AS #4
IF (ilogXc% <> 0) THEN
  minXc = LOG(minXc)
  maxXc = LOG(maxXc)
  stepXc = LOG(stepXc)
END IF
IF (ilogYc% <> 0) THEN
  minYc = LOG(minYc)
  maxYc = LOG(maxYc)
  stepYc = LOG(stepYc)
END IF
scalec = (maxXc - minXc) / (maxYc - minYc)
FOR Xc = minXc TO maxXc STEP stepXc
  IF (ilogXc% <> 0) THEN x(Dx%) = EXP(Xc) ELSE x(Dx%) = Xc
  FOR Yc = minYc TO maxYc STEP stepYc
    IF (ilogYc% <> 0) THEN x(Dy%) = EXP(Yc) ELSE x(Dy%) = Yc
    GOSUB Cost
    IF (ilogZc% <> 0) THEN Zc = LOG(retCost)/LOG(10!) ELSE Zc =
retCost
    PRINT Xc, (Yc-minYc)*scalec+minYc, Zc
    PRINT #4, Xc, (Yc-minYc)*scalec+minYc, Zc
  NEXT
NEXT
CLOSE #4
SetCreate "mosfit.cont", "MSWD"
INPUT "OK or Try Again(1)": ss$
IF (ss$ = "1") THEN GOTO ContourLoop
RETURN

SDRunner:
'--- set initial T & X & Cost ---
GOSUB InitialX
GOSUB Cost
oldEXTCost = retCost
GOSUB InitialT
oldT = T
iCost = 0
oldEXTCost = retCost
GOSUB EXTReport
'--- save oldEXTX for optEXTX, & optINTX ---
FOR Dx% = 1 TO nXP%
  optEXTX(Dx%) = x(Dx%)
  optINTX(Dx%) = x(Dx%)
NEXT
optEXTCost = oldEXTCost
optINTCost = oldEXTCost
EXT% = 0
EXTLoop:
'--- count-up loop counter ---
EXT% = EXT% + 1
'--- initialize random generator ---
RANDOMIZE REED%
RANDOMIZE TIMER
iNT% = 0
sumiNTACost = 0: sumiNTACost2 = 0
iAccept% = 0: gAccept% = 0
INTLoop:
inner% = 1

```

```

'--- internal loop with same T ---
iNT% = iNT% + 1
'--- generate new X and calculate cost ---
GOSUB GenerateX
'--- calculate cost ---
GOSUB Cost
'--- check accept or not ---
GOSUB Accept
GOSUB Tpoint
GOSUB Xpoint
IF (retAccept% = 1) THEN
'--- accepted ---
GOSUB UpdateX
oldINTCost = retCost
IF (iGenerateXCalled% = 0) THEN
iAccept% = iAccept% + 1
histINTACost(iAccept%) = retCost
ELSE
gAccept% = gAccept% + 1
END IF
'--- save current status if optimal ---
IF (retCost < optINTCost) THEN
optINTCost = retCost
FOR iX% = 1 TO nX%
optINTX(iX%) = x(iX%)
NEXT
END IF
'GOSUB Tpoint
ELSE
GOSUB ResumeOldX
END IF
'--- exit INT loop? ---
GOSUB ExitINTLoop
IF (retExitINTLoop% = 1) THEN GOTO BreakiNTLoop
GOTO INTLoop
BreakiNTLoop:
'--- post-process of INT loop ---
inner% = 0
nINT% = iINT%
'GOTO JumpiNTGreedy
'--- resume optINTX since it is minimal ---
oldINTCost = optINTCost
FOR iX% = 1 TO nX%
x(iX%) = optINTX(iX%)
NEXT
JumpiNTGreedy:
oldEXTCost = oldINTCost
'--- update optEXTX if this is optimal up to now ---
IF (oldEXTCost < optEXTCost) THEN
optEXTCost = oldEXTCost
FOR iX% = 1 TO nX%
optEXTX(iX%) = x(iX%)
NEXT
END IF
'GOTO JumpEXTGreedy
'--- resume optEXTX if current Cost is not optimal ---
IF (oldEXTCost > optEXTCost) THEN
oldEXTCost = optEXTCost
FOR iX% = 1 TO nX%
x(iX%) = optEXTX(iX%)
NEXT
END IF
JumpEXTGreedy:
retCost = oldEXTCost
'GOSUB Tpoint
histEXTCost(iEXT%) = oldEXTCost
'--- exit EXT loop? ---
GOSUB ExitEXTLoop
IF (retExitEXTLoop% = 1) THEN
IF (iLastGasp% >= 8) THEN
GOTO breakEXTLoop
ELSE
iLastGasp% = iLastGasp% + 1
'--- resume optEXTX if current Cost is not optimal ---
IF (oldEXTCost > optEXTCost) THEN
oldEXTCost = optEXTCost
FOR iX% = 1 TO nX%
x(iX%) = optEXTX(iX%)
NEXT
END IF
END IF
ELSE
IF (histEXTCost(iEXT%) < histEXTCost(iEXT%-1)) THEN

```

```

iLastGasp% = 0
END IF
END IF
'--- update Temp ---
GOSUB UpdateT
'--- update epsilon for random part ---
GOSUB UpdateEpsRandFac
GOSUB EXTReport
oldT = T
GOTO EXTLoop
breakEXTLoop:
'--- post-process of EXT loop ---
GOSUB ResShower
RETURN

Accept:
'--- decide accept or reject using Boltzmann dist. ---
deltaINTCost = retCost - oldINTCost
IF (deltaINTCost < 0) THEN
retAccept% = 1
ELSE
boltzmann = EXP(- deltaINTCost / T)
IF (RND(1) < boltzmann) THEN
retAccept% = 1
ELSE
retAccept% = 0
END IF
END IF
RETURN

InitialX:
'--- initialize X ---
FOR iX% = 1 TO nX%
x(iX%) = initX(iX%)
oldEXTX(iX%) = initX(iX%)
NEXT
RETURN

InitialT:
'--- try random search ninitRND times and guess initial T ---
minCost = infinity
maxCost = -infinity
sumCost = 0: sumCost2 = 0
FOR iinitRND% = 1 TO ninitRND%
'--- random generation of X ---
FOR iX% = 1 TO nX%
nameVc$ = nameVs$(iX2V%(iX%))
IF (nameVc$ = "nsub") OR (nameVc$ = "vmax") THEN
'--- random generation in log space for nsub and vmax ---
logminX = LOG(minX(iX%))
logmaxX = LOG(maxX(iX%))
lograngeX = logmaxX - logminX
dellafacX = RND(1) * lograngeX
dellafacX = EXP(dellafacX)
x(iX%) = minX(iX%) * dellafacX
ELSE
deltaX = RND(1) * rangeX(iX%)
x(iX%) = minX(iX%) + deltaX
END IF
NEXT
GOSUB Cost
'iInitialTFlag% = 1
'GOSUB Xpoint
'iInitialTFlag% = 0
IF (minCost > retCost) THEN
'--- this is the best cost, so update initial X ---
minCost = retCost
FOR iX% = 1 TO nX%
initX(iX%) = x(iX%)
NEXT
END IF
'--- if this is the worst cost, update maxCost ---
IF (maxCost < retCost) THEN minCost = retCost
'--- calculate sum's ---
sumCost = sumCost + retCost
sumCost2 = sumCost2 + retCost * retCost
NEXT
'--- calculate aveCost, sigmaCost ---
N = ninitRND%
aveCost = sumCost / N
sigmaCost = SQR((sumCost2 - N * aveCost * aveCost) / (N-1))
'--- initial T = k * sigmaCost (ICCAD'86) ---
initT = initTK * sigmaCost

```

```

initCost = retCost
PRINT #1, "init",initT,"initCost",initCost
T = initT
'--- choose initial X as the minimum Cost X's if it is less than given initX ---
IF (minCost < oldEXTCost) THEN
  FOR iX% = 1 TO nX%
    x(iX%) = initX(iX%)
  NEXT
  oldEXTCost = minCost
  oldINTCost = minCost
ELSE
  FOR iX% = 1 TO nX%
    x(iX%) = oldEXTX(iX%)
  NEXT
  oldEXTCost = oldEXTCost
  oldINTCost = oldEXTCost
END IF
RETURN

GenerateX:
IF (EXT% > minEXT%) THEN
  iGenerateXCalled% = 1 - iGenerateXCalled%
ELSE
  iGenerateXCalled% = 0
END IF
IF (iGenerateXCalled% = 1) THEN
  '--- if icalled% = 1 then gradient ---
  '--- which X is moved ---
  iXV% = 1 + INT((nX% - .00001) * RND(1))
  nameVc$ = nameVs(iXV%(iXV%))
  IF (nameVc$ = "nsub") OR (nameVc$ = "vmax") THEN ilogXg% = 1 ELSE
  ilogXg% = 0
  '--- gradient generation in log space for nsub and vmax ---
  IF (ilogXg% = 1) THEN
    minXg = LOG(minX(iXV%)): maxXg = LOG(maxX(iXV%)): Xg =
    LOG(x(iXV%))
  ELSE
    minXg = minX(iXV%): maxXg = maxX(iXV%): Xg = x(iXV%)
  END IF
  rangeXg = maxXg - minXg
  '--- choose DX value ---
  DX = rangeXg * .00001
  '--- find Xopt by fitting quadratic form ---
  f0 = oldINTCost
  IF (ilogXg% = 0) THEN x(iXV%) = Xg + DX ELSE x(iXV%) = EXP(Xg + DX)
  GOSUB Cost
  fplus = retCost
  IF (ilogXg% = 0) THEN x(iXV%) = Xg - DX ELSE x(iXV%) = EXP(Xg - DX)
  GOSUB Cost
  fminus = retCost
  concave = fplus + fminus - 2 * f0
  IF (concave > 0) THEN
    '--- f > 0 ---
    deltaXg = - DX / 2 * (fplus - fminus) / concave
    '--- limit up to limitDeltaXg ---
    IF (ABS(deltaXg) > rangeXg * .2) THEN deltaXg = SGN(deltaXg) *
    rangeXg * .2
  ELSE
    limitDeltaXg = rangeXg * .03
    '--- f <= 0 ---
    IF (fplus = fminus) THEN
      '--- f = 0 ---
      deltaXg = 0
    ELSE
      iGenerateXLoop0% = 0
      GenerateXLoop0:
      IF (fplus > fminus) THEN
        '--- f > 0 ---
        deltaXg = -limitDeltaXg
      ELSE
        '--- f < 0 ---
        deltaXg = limitDeltaXg
      END IF
      IF (ilogXg% = 0) THEN x(iXV%) = Xg + deltaXg ELSE x(iXV%) =
      EXP(Xg + deltaXg)
      '--- x 1/2 loop ---
      GOSUB Cost
      iGenerateXLoop0% = iGenerateXLoop0% + 1
      initialTFlag% = 1
      GOSUB Xpoint
      initialTFlag% = 0
      IF (retCost > f0) AND (iGenerateXLoop0% <= 2) THEN
        limitDeltaXg = limitDeltaXg / 2
      END IF
    END IF
  END IF
  '--- update X and if X is out of range, then pull back ---
  IF (logXg% = 0) THEN x(iXV%) = Xg + deltaXg ELSE x(iXV%) = EXP(Xg +
  deltaXg)
  IF (x(iXV%) < minX(iXV%)) THEN x(iXV%) = minX(iXV%)
  IF (x(iXV%) > maxX(iXV%)) THEN x(iXV%) = maxX(iXV%)
  ELSE
    '--- if icalled% = 0 then, random generation ---
    FOR iX% = 1 TO nX%
      nameVc$ = nameVs(iXV%(iXV%))
      IF (nameVc$ = "nsub") OR (nameVc$ = "vmax") THEN
        '--- random generation in log space for nsub and vmax ---
        logminX = LOG(minX(iXV%))
        logmaxX = LOG(maxX(iXV%))
        lograngeX = logmaxX - logminX
        GenerateXLoop1:
        GOSUB GaussRnd: rndNum = retGaussRnd
        deltafacX = rndNum * lograngeX / 3.1 * epsRndFac
        deltafacX = EXP(deltafacX)
        '--- if X is out of range, then pull back ---
        IF (x(iXV%) * deltafacX < minX(iXV%)) THEN GenerateXLoop2
        IF (x(iXV%) * deltafacX > maxX(iXV%)) THEN GenerateXLoop2
        x(iXV%) = x(iXV%) * deltafacX
      ELSE
        GenerateXLoop2:
        GOSUB LorentzRnd: rndNum = retLorentzRnd
        GOSUB GaussRnd: rndNum = retGaussRnd
        deltaX = rndNum * rangeX(iXV%) / 3.1 * epsRndFac
        '--- if X is out of range, then pull back ---
        IF (x(iXV%) + deltaX < minX(iXV%)) THEN GenerateXLoop2
        IF (x(iXV%) + deltaX > maxX(iXV%)) THEN GenerateXLoop2
        x(iXV%) = x(iXV%) + deltaX
      END IF
    NEXT
  END IF
  RETURN

UpdateEpsRndFac:
'--- update epsilon for random part ---
epsRndFac = epsRndFac * (T / oldT) ^ .75
IF (LastGasp% >= 1) THEN
  epsRndFac = SQR(T / initT)
ELSE
  IF (epsRndFac <= .05) THEN epsRndFac = .05
END IF
RETURN

UpdateEpsRndFacOld:
'--- update epsilon for random part ---
acceptRatio = iAccept% / nINT%
IF (LastGasp% = 1) THEN
  IF (epsRndFac >= .5) THEN epsRndFacUp% = 0 ELSE epsRndFacUp%
  = 1
  END IF
  IF (LastGasp% >= 1) THEN
    IF (epsRndFacUp% = 0) THEN
      epsRndFac = epsRndFac * .75
    ELSE
      epsRndFac = epsRndFac * 1.5
    END IF
    IF (epsRndFac > 1) THEN
      epsRndFac = .75
      epsRndFacUp% = 0
    ELSE
      IF (epsRndFac < .1) THEN
        epsRndFac = .15
        epsRndFacUp% = 1
      END IF
    END IF
  ELSE
    IF (EXT% > minEXT%) THEN acceptRatio = acceptRatio * 2
    IF (acceptRatio < .5) THEN epsRndFac = epsRndFac *
    SQR(1/factorUpdateTLB)
    IF (acceptRatio < .5) THEN epsRndFac = epsRndFac * 2^(1/nX%)
    epsRndFac = epsRndFac * SQR(T / oldT)
    IF (epsRndFac > 1) THEN epsRndFac = 1
  END IF
  RETURN
UpdateX:

```

```

FOR iX% = 1 TO nX%
  oldX(iX%) = x(iX%)
NEXT
RETURN

ResumeOldX:
FOR iX% = 1 TO nX%
  x(iX%) = oldX(iX%)
NEXT
RETURN

ExitINTLoop:
'--- INT loop exit condition ---
retExitINTLoop = 0
IF (iINT% >= maxnINT%) THEN
  '--- if EXT loop count exceed limit, simply exit INT loop ---
  retExitINTLoop = 1
RETURN
END IF
RETURN

ExitEXTLoop:
'--- EXT loop exit condition, frozen condition ---
retExitEXTLoop% = 0
IF (iEXT% > maxnEXT%) THEN
  '--- if EXT loop count exceed limit, simply exit EXT loop ---
  retExitEXTLoop% = 1
RETURN
END IF
'--- if iEXT% < minnEXT%, continue ---
IF (iEXT% > minnEXT%) THEN
  GOTO JumpHistoryEval
aveCost = 0
minCost = infinity
maxCost = -infinity
'--- calculate average, max, and min of recent Cost ---
FOR iP% = iEXT% - 1 TO iEXT%
  hCost = histEXT Cost(iP%)
  aveCost = aveCost + hCost
  IF (hCost > maxCost) THEN maxCost = hCost
  IF (hCost < minCost) THEN minCost = hCost
NEXT
aveCost = aveCost / 2
'--- exit condition using ave and min and max ---
exitEXTrelCost = (maxCost - minCost) / (ABS(aveCost) + infinitesimal)
IF (exitEXTrelCost < epsExitEXTrelCost) THEN retExitEXTLoop% = 1
JumpHistoryEval:
delCost = histEXT Cost(iEXT%) - histEXT Cost(iEXT% - 1)
exitEXTrelCost = ABS(delCost) /
  (ABS(histEXT Cost(iEXT%)) + infinitesimal)
IF (exitEXTrelCost < epsExitEXTrelCost) THEN retExitEXTLoop% = 1
IF (delCost >= 0) THEN retExitEXTLoop% = 1
END IF
RETURN

UpdateT:
'--- update T by ICCAD86 ---
IF (iLastGasp% >= 1) THEN
  IF (iLastGasp% >= 3) THEN
    T = .5 * T
  ELSE
    T = 1.6 * T
  END IF
  IF (T > initT) THEN T = .1 * T
ELSE
  N% = iAccept%
  IF (N% >= 3) THEN
    '--- if acceptance ratio is high enough ---
    sumINTACost = 0
    FOR iU% = 1 TO N%
      sumINTACost = sumINTACost + histINTACost(iU%)
    NEXT
    aveINTACost = sumINTACost / N%
    FOR iU% = 1 TO N%
      sigmaINTACost = (histINTACost(iU%) - aveINTACost) ^ 2
    NEXT
    sigmaINTACost = SQR(sigmaINTACost / (N% - 1))
    IF (sigmaINTACost = 0) THEN sigmaINTACost = infinitesimal
    factorUpdateT = EXP(-updateTLambda * T / sigmaINTACost)
    IF (factorUpdateT < factorUpdateTLB) THEN factorUpdateT =
factorUpdateTLB
    T = factorUpdateT * T
  ELSE

```

```

    IF (IX% MOD 1 = 0) THEN PRINT "
NEXT
PRINT #1, "
RETURN

Xpoint:
'--- point a circle ---
WINDOW 2
SHOWPEN
IF (IXpointCalled% = 0) THEN
'--- write frame for the first time ---
PENSIZE 1,1
SetRect rect%(0),0,0,280,280
CALL FRAMERECT(VARPTR(rect%(0)))
IXpointCalled% = IXpointCalled% + 1
END IF
IF (IinitialFlag% = 1) THEN marksize% = 1 ELSE marksize% = 2
wX% = 280 * (x(1) - minX(1)) / rangeX(1)
wY% = 280 * (1 - LOG(x(2)/minX(2))) / LOG(maxX(2)/minX(2))
SetRect rect%(0), wX%-marksize%,wY%-marksize%
marksize%,wX%+marksize%,wY%+marksize%
IF (retAccept% = 1) THEN
IF (IGenerateXCalled% = 1) THEN
CALL PAINTRECT(VARPTR(rect%(0)))
ELSE
CALL PAINTOVAL(VARPTR(rect%(0)))
END IF
ELSE
IF (IGenerateXCalled% = 1) THEN
CALL FRAMERECT(VARPTR(rect%(0)))
ELSE
CALL FRAMEOVAL(VARPTR(rect%(0)))
END IF
END IF
HIDEPEN
RETURN

Tpoint:
'--- point a circle ---
WINDOW 2
marksize% = 2
rect%(1) = 50 * ABS(LOG(oldT / initT)) / LOG(10) - marksize%
rect%(0) = 50 * ABS(LOG(ABS(retCost / initCost))) / LOG(10) - marksize%
rect%(3) = 50 * ABS(LOG(oldT / initT)) / LOG(10) + marksize%
rect%(2) = 50 * ABS(LOG(ABS(retCost / initCost))) / LOG(10) + marksize%
IF (IGenerateXCalled% = 1) THEN
CALL PAINTOVAL(VARPTR(rect%(0)))
ELSE
CALL FRAMEOVAL(VARPTR(rect%(0)))
END IF
RETURN

Mos3:
GOSUB X2V
IF (tox <= 0) THEN CALL errmsg("tox negative or zero in Mos3")
coxpu = epsox / tox
phif = vtherm * LOG(nsub / ni)
IF (phif <= 0) THEN
errmsg$ = "phif < 0 (" + STR$(nsub) + ") in Mos3"
CALL errmsg(errmsg$)
END IF
phif2 = phif + phif
leff = l - ld - ld
IF (leff <= .1 * l) THEN leff = .1 * l
phibs = phif2 - vbs
IF (phibs <= 0) THEN phibs = infinitesimal
sqphbs = SQR(phibs)

'--- THRESHOLD VOLTAGE ---
pfn = delta * pi * epsi * .5 * coxpu * w
xd = SQR (2 * epsi / q / nsub)
wp = xd * sqphbs
wc = .0631353 * xj + .8013292# * wp + .01110777# * wp * wp / xj
wpj = wp / (xj + wp)
fs = 1 - xj / leff * ((ld + wc) / xj) * SQR (1 - wpj * wpj) - ld / xj
IF (fs <= 0) THEN
errmsg$ = "fs negative in Mos3. Use larger nsub.
nsub="+STR$(nsub)+" xd="+STR$(xd)
CALL errmsg(errmsg$)
END IF
sigma = eta * 8.15E-22 / coxpu / leff / leff / leff
vfb = vto - phif2 - gammac * SQR (phif2)
vth = vfb + phif2 - sigma * vds + gammac * fs * sqphbs + pfn * phibs

```

```

'--- ON VOLTAGE ---
cd = coxpu * (gammac * fs / 2 / sqphbs + pfn / 2)
mos3N = 1 + (q * nfs + cd) / coxpu
von = vth + mos3N * vtherm

'--- NOMINAL GATE VOLTAGE ---
IF (vgs > von) THEN vgsx = vgs ELSE vgsx = von

'--- SATURATION VOLTAGE ---
us = uo / (1 + theta * (vgsx - vth))
fb = gammac * fs / 4 / sqphbs + pfn
arga = (vgsx - vth + .0000001) / (1 + fb)
argb = vmax * leff / us
vdsat = 2 * arga * argb
argc = arga + argb + SQR(arga * arga + argb * argb)
IF (argc <= 0) THEN argc = infinitesimal
vdsat = vdsat / argc
IF (vds > vdsat) THEN vdsx = vdsat ELSE vdsx = vds
ueff = us / (1 + us * vdsx / vmax / leff)

'--- LINEAR REGION ---
IF (vds <= vdsat) THEN
ids = (w / leff) * ueff * coxpu
ids = ids * (vgsx - vth - (1 + fb) / 2 * vds) * vds
'--- SATURATED REGION ---
ELSE
ep = vmax / us * (1 + vmax * leff / us / vdsat)
arga = ep * xd * xd / 2
argb = kappa * xd * xd * (vds - vdsat)
argc = SQR(arga * arga + argb) + arga
IF (argc <= 0) THEN argc = infinitesimal
debt = argb / argc
'--- PUNCHTHROUGH APPROX. ---
IF (debt > .5 * leff) THEN
debt = leff * (1 - leff / 4 / debt)
END IF
ids = (w / (leff - debt)) * ueff * coxpu
ids = ids * (vgsx - vth - (1 + fb) / 2 * vdsat) * vdsat
END IF

'--- SUBTHRESHOLD REGION ---
IF (vgs < von) THEN
vgsVonVtherm = (vgs - von) / vtherm / mos3N
IF (vgsVonVtherm > -20) THEN vgsvon = vgsVonVtherm ELSE
vgsvon = -20
idsexp = ids * EXP(vgsvon)
IF (idsexp > 1E-15) THEN ids = idsexp ELSE ids = 1E-15
END IF
RETURN

'--- parsing ---
SUB parse(s$, token$, rtoken%, errorFlag%) STATIC
errorFlag% = 0
s$ = s$ + " "
'--- clear token array ---
FOR i% = 1 TO UBOUND(tokens)
tokens(i%) = " "
NEXT
rtoken% = 0
WHILE 1
'--- delete leading tabs and spaces ---
T$ = LEFT$(s$, 1)
WHILE ((T$ = " ") OR (T$ = CHR$(34)))
s$ = MID$(s$, 2)
T$ = LEFT$(s$, 1)
WEND
'--- searching tab or space whichever comes first ---
insep% = INSTR(s$, " ")
intab% = INSTR(s$, CHR$(34))
IF (insep% = 0) THEN insep% = 1000
IF (intab% = 0) THEN intab% = 1000
idelim% = insep%
IF (idelim% > intab%) THEN idelim% = intab%
IF (idelim% = 1000) GOTO breakParseLoop
itoken% = itoken% + 1
PRINT #1, s$, itoken%
IF (itoken% >= rtokenMax%) THEN
errorFlag% = 1
msg$ = "Too many field (" + STR$(itoken%) + ") in line " + STR$(line%) + " "
CALL errmsg(msg$)
GOTO breakParseLoop
END IF

```



```

'--- recognize token as an entity from the first char to the next blank ---
tokens$(iToken%) = LEFT$(s$, iDelim%-1)
'--- update line string ---
s$ = MID$(s$, iDelim%+1)
WEND
breakParseLoop:
nToken% = iToken%
END SUB

'--- error message routine ---
SUB errmsg(errormsg$) STATIC
WINDOW 5,,(0,0)-(500,400), 4
TEXTFACE 1
TEXTSIZE 12
MOVETO 100,50
PRINT "Message : ";
PRINT errormsg$
BUTTON 1,1,"OK",(190,100)-(250,120),1
errmsgLoop:
WHILE DIALOG(0) <> 1 : WEND
IF DIALOG(1) <> 1 THEN GOTO errmsgLoop
WINDOW CLOSE 5
END SUB

SUB paramRead(tokens$, iX%, iP%, iV%) STATIC
IF (UCASE$(tokens$(3)) = "FIX") THEN
'--- constant parameters ---
iP% = iP% - 1
iX2iV%(iP%) = iV%
iV2iX%(iV%) = iP%
IF (tokens$(3) = "") THEN iniX(iP%) = iniV(iV%) ELSE iniX(iP%) =
VAL(tokens$(4))
ELSE
IF (tokens$(3) = "") THEN minVal = minV(iV%) ELSE minVal =
VAL(tokens$(3))
IF (tokens$(4) = "") THEN maxVal = maxV(iV%) ELSE maxVal =
VAL(tokens$(4))
PRINT "
iX=";iX%;iV=";nameVS(iV%);"minVal,maxVal";minVal;maxVal;minV(iV%);max
V(iV%)
IF (minVal = maxVal) THEN
'--- constant parameters ---
iP% = iP% - 1
iX2iV%(iP%) = iV%
iV2iX%(iV%) = iP%
iniX(iP%) = minVal
ELSE
'--- variables ---
iX% = iX% + 1
iX2iV%(iX%) = iV%
iV2iX%(iV%) = iX%
minX(iX%) = minVal
maxX(iX%) = maxVal
IF (tokens$(5) = "") THEN iniX(iX%) = iniV(iV%) ELSE iniX(iX%) =
VAL(tokens$(5))
END IF
END IF
END SUB

SUB initializeV(iV%, nameVs$, minVs, maxVs, iniVs) STATIC
'--- initializing V ---
nameVS(iV%) = nameVs$
minV(iV%) = minVs: maxV(iV%) = maxVs: iniV(iV%) = iniVs
END SUB

'--- convert user coord to world coord ---
SUB User2World(x, Y, wX%, wY%) STATIC
wX% = x / maxVgd * 240 + 20
wY% = - Y / maxVds * 240 + 260
END SUB

```

```

'---- Minimization with simulated annealing ----
'---- initialize I/O ----
'---- minEXT is changed to 10 from 5
'---- Lorentzian
OPEN "scm." FOR OUTPUT AS #1
OPEN "funcSD.res" FOR OUTPUT AS #2

FOR iproblem% = 1 TO 18
  P% = iproblem%
  'IF (P% <> 4) AND (P% <> 5) AND (P% <> 12) AND (P% <> 18) THEN GOTO
  BreakProblemLoop
FOR icount% = 1 TO 10
  Windower:
  '---- initialize window 1 ----
  WINDOW 2,"Graphics Window", (200,20)-(480, 300),1
  WINDOW 1,"Text Window", (0,20)-(200, 300),1
  TEXTSIZE 8
  'INPUT "iproblem": iproblem%

OPTION BASE 0
SELECT CASE iproblem%
CASE 0
  nX% = 2
CASE 1
  nX% = 1
CASE 2
  nX% = 1
CASE 3 TO 7, 13
  nX% = 2
CASE 8, 14
  nX% = 3
CASE 9, 15
  nX% = 4
CASE 10, 16
  nX% = 5
CASE 11
  nX% = 8
CASE 12
  nX% = 10
CASE 17
  nX% = 6
CASE 18
  nX% = 7
CASE ELSE
END SELECT
maxnX% = 14
'niniRND% = nX% * 50
niniRND% = 200
maxnINT% = nX% * 24
IF (maxnINT% < 100) THEN maxnINT% = 100
maxnEXT% = 100
DIM SHARED oldX(maxnX%), newX(maxnX%), oldEXTX(maxnX%)
DIM SHARED optX(maxnX%)
DIM SHARED minX(maxnX%), maxX(maxnX%), iniX(maxnX%),
X(maxnX%), rangeX(maxnX%)
DIM SHARED histINTACost(maxnINT%)

Initializer:
iGreedy% = 1
infinity = 1E+20
infinitesimal = 1E-20
iniTK = 2
updateTLambda = .7
factorUpdateTLB = .6
minEXT% = 10
iGaussCalled% = 0
iGenerateXCalled% = 0
opeRndFac = 1!
pi = 3.141592

SELECT CASE iproblem%
CASE 0
FOR D% = 1 TO nX%
  minX(D%) = -1!: maxX(D%) = 1!
  rangeX(D%) = maxX(D%) - minX(D%)
  'iniX(D%) = (maxX(D%) + minX(D%)) / 2
  iniX(D%) = 1!
NEXT
CASE 1 TO 15
FOR D% = 1 TO nX%+1
  minX(D%) = -10: maxX(D%) = 10
  rangeX(D%) = maxX(D%) - minX(D%)
  iniX(D%) = 0

```

```

NEXT
CASE 16 TO 18
FOR D% = 1 TO nX%+1
  minX(D%) = -5: maxX(D%) = 5
  rangeX(D%) = maxX(D%) - minX(D%)
  iniX(D%) = 0
NEXT
CASE ELSE
END SELECT
oldINTCost = infinity
oldEXTCost = infinity

GOSUB SDRunner
'INPUT a
ERASE oldX, newX, oldEXTX, optX
ERASE minX, maxX, iniX, X, rangeX
ERASE histINTACost
NEXT
BreakProblemLoop:
NEXT
SetCreate "funcSD.res", "MSWD"
CLOSE
END

SDRunner:
'---- set initial T & X & Cost ----
GOSUB InitiaX
GOSUB Cost
oldEXTCost = retCost
optCost = retCost
GOSUB InitiaT
iCost& = 0: iLastGasp% = 0
oldEXTCost = retCost
oldINTCost = retCost
EXTCost = retCost
GOSUB EXTReport
'---- save oldEXTX for optX ----
optCost = retCost
FOR D% = 1 TO nX%
  optX(D%) = X(D%)
NEXT
EXT% = 0
EXT Loop:
'---- count-up loop counter ----
EXT% = iEXT% + 1
'---- initialize random generator ----
RANDOMIZE TIMER
iINT% = 0
sumINTACost = 0: sumINTACost2 = 0
iAccept% = 0: gAccept% = 0
INTLoop:
  inner% = 1
  '---- internal loop with same T ----
  iINT% = iINT% + 1
  '---- generate new X and calculate cost ----
  GOSUB GenerateX
  GOSUB Cost
  '---- check accept or not ----
  GOSUB Accept
  GOSUB Tpoint
  GOSUB Xpoint
  IF (retAccept% = 1) THEN
    '---- accepted ----
    GOSUB UpdateX
    oldINTCost = retCost
    IF (iGenerateXCalled% = 0) THEN
      iAccept% = iAccept% + 1
      histINTACost(iAccept%) = retCost
    ELSE
      gAccept% = gAccept% + 1
    END IF
  '---- save current status if optimal ----
  IF (retCost < optCost) THEN
    optCost = retCost
    FOR D% = 1 TO nX%
      optX(D%) = X(D%)
    NEXT
  END IF
ELSE
  GOSUB ResumeOldX
END IF
'---- exit INT loop? ----
GOSUB ExitINTLoop

```

```

    IF (retExitINTLoop% = 1) THEN GOTO BreakINTLoop
GOTO INTLoop
BreakINTLoop:
'--- post-process of INT loop ---
inner% = 0
nINT% = iINT%
EXTCost = oldINTCost
originalEXTCost = EXTCost
'--- exit EXT loop? ---
IF (EXTCost > optCost) AND (IGreedy% = 1) THEN GOSUB
ResumeOptX
retCost = EXTCost
GOSUB ExitEXTLoop
IF (retExitEXTLoop% = 1) THEN GOTO BreakEXTLoop
'--- greedy substitution ---
GOSUB Tpoint
'--- update Temp and RndFac ---
GOSUB UpdateT
GOSUB UpdateEpsRndFac
GOSUB EXTReport
oldT = T
oldEXTCost = EXTCost
GOTO EXTLoop
BreakEXTLoop:
'--- post-process of EXT loop ---
GOSUB FinalReport
RETURN

ResumeOptX:
'--- resume optX ---
EXTCost = optCost
FOR D% = 1 TO nX%
    X(D%) = optX(D%)
NEXT
RETURN

InitialX:
'--- initialize X ---
FOR D% = 1 TO nX%
    X(D%) = initX(D%)
    oldEXTX(D%) = initX(D%)
NEXT
RETURN

InitialT:
'--- try random search ninitRND times and guess initial T ---
maxCost = -infinity
sumCost = 0: sumCost2 = 0
FOR iinitRND% = 1 TO ninitRND%
    '--- random generation of X ---
    FOR D% = 1 TO nX%
        X(D%) = minX(D%) + RND(1) * rangeX(D%)
    NEXT
    GOSUB Cost
    IF (optCost > retCost) THEN
        '--- this is the best cost, so update initial X ---
        optCost = retCost
        FOR D% = 1 TO nX%
            initX(D%) = X(D%)
        NEXT
    END IF
    '--- if this is the worst cost, update maxCost ---
    IF (maxCost < retCost) THEN optCost = retCost
    '--- calculate sum's ---
    sumCost = sumCost + retCost
    sumCost2 = sumCost2 + retCost * retCost
NEXT
'--- calculate aveCost, sigmaCost ---
N = ninitRND%
aveCost = sumCost / N
sigmaCost = SQR((sumCost2 - N * aveCost * aveCost) / (N-1))
'--- initial T = k * sigmaCost (ICCAD'86) ---
initT = initTK * sigmaCost
initCost = retCost
PRINT #1, "initT";initT;"initCost";initCost
T = initT
oldT = T
'--- choose initial X as the minimum Cost X's if it is less than given initX ---
IF (optCost < oldEXTCost) THEN
    FOR D% = 1 TO nX%
        X(D%) = initX(D%)
    NEXT
    oldEXTCost = optCost

```

```

    oldINTCost = optCost
ELSE
    FOR D% = 1 TO nX%
        X(D%) = oldEXTX(D%)
    NEXT
    oldEXTCost = oldEXTCost
    oldINTCost = oldEXTCost
END IF
RETURN

GenerateX:
IF (EXT% > minEXT%) THEN
    iGenerateXCalled% = 1 - iGenerateXCalled%
ELSE
    iGenerateXCalled% = 0
END IF
IF (iGenerateXCalled% = 1) THEN
    '--- if icalled% = 1 then gradient ---
    '--- which X is moved ---
    DV% = 1 + INT((nX% - .00001) * RND(1))
    '--- choose DX value ---
    rangeXg = rangeX(DV%)
    DX = rangeXg * .00001
    Xg = X(DV%)
    '--- find Xopt by fitting quadratic form ---
    f0 = oldINTCost
    X(DV%) = Xg + DX
    GOSUB Cost
    fplus = retCost
    X(DV%) = Xg - DX
    GOSUB Cost
    fminus = retCost
    concave = fplus + fminus - 2 * f0
    IF (concave > 0) THEN
        '--- f > 0 ---
        deltaXg = -DX / 2 * (fplus - fminus) / concave
        '--- limit up to limitDeltaXg ---
        IF (ABS(deltaXg) > rangeXg * .1) THEN deltaXg = SGN(deltaXg) *
rangeXg * .1
    ELSE
        '--- f <= 0 ---
        limitDeltaXg = rangeXg * .005
        oldDeltaXg = 0
        iGenerateXLoop0% = 0
        GenerateXLoop0:
        IF (fplus >= fminus) THEN
            '--- f >= 0 ---
            deltaXg = -limitDeltaXg
        ELSE
            '--- f < 0 ---
            deltaXg = limitDeltaXg
        END IF
        X(DV%) = Xg + deltaXg
        '--- x 2 loop ---
        GOSUB Cost
        iGenerateXLoop0% = iGenerateXLoop0% + 1
        IF (retCost < f0) THEN
            oldDeltaXg = deltaXg
            IF (iGenerateXLoop0% <= 3) THEN
                limitDeltaXg = limitDeltaXg * 2
                GOTO GenerateXLoop0
            END IF
        END IF
        deltaXg = oldDeltaXg
    END IF
    '--- update X and if X is out of range, then pull back ---
    X(DV%) = Xg + deltaXg
    IF (X(DV%) < minX(DV%)) THEN X(DV%) = minX(DV%)
    IF (X(DV%) > maxX(DV%)) THEN X(DV%) = maxX(DV%)
ELSE
    '--- if icalled% = 0 then, random generation ---
    FOR D% = 1 TO nX%
        GenerateXLoop2:
        GOSUB LorentzRnd: rndNum = retLorentzRnd / 2
        GOSUB GaussRnd: rndNum = retGaussRnd
        deltaX = rndNum * rangeX(D%) / 3.1 * epsRndFac
        '--- if X is out of range, then pull back ---
        IF (X(D%) + deltaX < minX(D%)) THEN GenerateXLoop2
        IF (X(D%) + deltaX > maxX(D%)) THEN GenerateXLoop2
        X(D%) = X(D%) + deltaX
    NEXT
END IF
RETURN

```

```

Accept:
'---- decide accept or reject using Boltzmann dist. ----
deltaINTCost = retCost - oldINTCost
IF (deltaINTCost < 0) THEN
  retAccept% = 1
ELSE
  boltzmann = EXP(- deltaINTCost / T)
  IF (RND(1) < boltzmann) THEN
    retAccept% = 1
  ELSE
    retAccept% = 0
  END IF
END IF
RETURN

UpdateX:
FOR IX% = 1 TO nX%
  oldX(IX%) = X(IX%)
NEXT
RETURN

ResumeOldX:
FOR IX% = 1 TO nX%
  X(IX%) = oldX(IX%)
NEXT
RETURN

ExitINTLoop:
'---- INT loop exit condition ----
retExitINTLoop% = 0
IF (iINT% >= maxnINT%) THEN
  '---- if EXT loop count exceed limit, simply exit INT loop ----
  retExitINTLoop% = 1
RETURN
END IF
RETURN

ExitEXTLoop:
'---- EXT loop exit condition, frozen condition ----
retExitEXTLoop% = 0
IF (iEXT% > maxnEXT%) THEN
  '---- if EXT loop count exceed limit, simply exit EXT loop ----
  retExitEXTLoop% = 1
RETURN
END IF
'---- if iEXT% < minnEXT%, continue ----
IF (iEXT% < minnEXT%) THEN RETURN
'---- takes care of LastGasp ----
delCost = EXTCost - oldEXTCost
retCost = delCost / (ABS(EXTCost) + infinitesimal)
IF (iGreedy% = 1) THEN
  '---- greedy case ----
  IF (retCost < -.02) THEN
    iLastGasp% = 0
  ELSE
    iLastGasp% = iLastGasp% + 1
  END IF
ELSE
  '---- drift case ----
  IF (EXTCost < optCost) THEN
    iLastGasp% = 0
  ELSE
    IF (ABS(retCost) < .001) THEN
      iLastGasp% = iLastGasp% + 1
    ELSE
      IF (iLastGasp% >= 1) THEN iLastGasp% = iLastGasp% + 1
    END IF
  END IF
  '---- resume optX if current Cost is not optimal ----
  IF (iLastGasp% = 4) AND (EXTCost > optCost) THEN GOSUB
ResumeOptX
  IF (EXTCost < optCost) THEN iLastGasp% = 0
END IF
'---- exit EXT loop if iLastGasp% and epsRndFac conditions are met ----
IF (iLastGasp% >= 14) AND (epsRndFac < .099) THEN retExitEXTLoop%
= 1
RETURN

UpdateEpsRndFac:
'---- update epsilon for random part ----
IF (iLastGasp% >= 3) THEN
  epsRndFac = (T / iIntT)

```

```

ELSE
  epsRndFac = (T / iIntT) ^ .75
  IF (epsRndFac <= .03) THEN epsRndFac = .03
END IF
RETURN

UpdateT:
'---- update T by ICCAD86 ----
IF (iLastGasp% >= 1) THEN
  IF (iLastGasp% >= 4) THEN
    T = .75 * T
  ELSE
    IF (iGreedy% = 1) THEN T = 1.3 * T
  END IF
ELSE
  '====
  'ABS(retCost) = aRelCost
  'IF (aRelCost > 1) THEN T = .5 * T
  'IF (aRelCost > .3) THEN T = .9 * T
  'IF (aRelCost >
  'RETURN
  N% = iAccept%
  IF (N% >= 3) THEN
    '---- if acceptance ratio is high enough ----
    sumINTACost = 0
    FOR IU% = 1 TO N%
      sumINTACost = sumINTACost + histINTACost(iU%)
    NEXT
    aveINTACost = sumINTACost / N%
    FOR IU% = 1 TO N%
      sigmaINTACost = (histINTACost(iU%) - aveINTACost) ^ 2
    NEXT
    sigmaINTACost = SQR(sigmaINTACost / (N% - 1))
    IF (sigmaINTACost = 0) THEN sigmaINTACost = infinitesimal
    factorUpdateT = EXP(-updateTLambda * T / sigmaINTACost)
    IF (factorUpdateT < factorUpdateTLB) THEN factorUpdateT =
factorUpdateTLB
    T = factorUpdateT * T
  ELSE
    T = .9 * T
    sigmaINTACost = 9999!
    aveINTACost = 9999!
  END IF
END IF
RETURN

Cost:
'---- problems ----
SELECT CASE iProblem%
CASE 0
  xx = X(1): yy = X(2)
  retCost = xx*xx + 2*yy*yy -.3*COS(3*pi*xx) -.4*COS(4*pi*yy) + .7
CASE 1
  xx = X(1)
  retCost = xx^6 - 15 * xx^4 + 27 * xx^2 + 250
CASE 2
  xx = X(1)
  CALL G1(xx, retCost)
CASE 3
  xx = X(1): yy = X(2)
  CALL G1beta(xx, yy, 0!, retCost)
CASE 4
  xx = X(1): yy = X(2)
  CALL G1beta(xx, yy, .5, retCost)
CASE 5
  xx = X(1): yy = X(2)
  CALL G1beta(xx, yy, 1!, retCost)
CASE 6
  xx = X(1): yy = X(2)
  retCost = (4 - 2.1*xx^2 + xx^4/3) * xx^2 + xx*yy + (-4 + 4*yy^2) * yy^2
CASE 7 TO 9
  GOSUB G2
  retCost = retG2
CASE 10 TO 12
  GOSUB G3
  retCost = retG3
CASE 13 TO 18
  GOSUB G4
  retCost = retG4
CASE ELSE
  PRINT "No corresponding problem": RETURN
END SELECT
iCost& = iCost& + 1

```

RETURN

G2:

```

k2 = 10
a2 = 1
y1 = 1 + (X(1) - 1) / 4
retG2 = k2 * (SIN(pi * y1)) ^ 2
FOR iGX% = 1 TO nX%-1
  yi = 1 + (X(iGX%) - 1) / 4
  yi1 = 1 + (X(iGX%+1) - 1) / 4
  retG2 = retG2 + (yi-a2)^2 * (1 + k2*(SIN(pi*yi1))^2)
NEXT
retG2 = retG2 + (yi1 - a2)^2
retG2 = pi/nX% * retG2 + .001
RETURN
    
```

G3:

```

k3 = 10
a3 = 1
y1 = X(1)
retG3 = k3 * (SIN(pi * y1)) ^ 2
FOR iGX% = 1 TO nX%-1
  yi = X(iGX%)
  yi1 = X(iGX%+1)
  retG3 = retG3 + (yi-a3)^2 * (1 + k3*(SIN(pi*yi1))^2)
NEXT
retG3 = retG3 + (yi1 - a3)^2
retG3 = pi/nX% * retG3 + .001
RETURN
    
```

G4:

```

k4 = .1: k5 = 1!: a4 = 1: i0 = 3: i1 = 2
x1 = X(1)
retG4 = (SIN(pi*i0*x1)) ^ 2
FOR iGX% = 1 TO nX%-1
  xi = X(iGX%)
  xi1 = X(iGX%+1)
  retG4 = retG4 + (xi-a4)^2 * (1 + k5*(SIN(pi*i0*xi1))^2)
NEXT
retG4 = retG4 + (xi1-a4)^2 * (1 + k5*(SIN(pi*i0*xi1))^2)
retG4 = k4 * retG4 + .001
RETURN
    
```

GaussRnd:

```

'--- gaussian distribution (see p.217 of NR) ---
IF (iGaussCalled% = 0) THEN
  gaussR = 2!
  WHILE (gaussR >= 1!)
    gaussV1 = 2! * RND(1) - 1!
    gaussV2 = 2! * RND(1) - 1!
    gaussR = gaussV1 * gaussV1 + gaussV2 * gaussV2
  WEND
  gaussFac = SQR(-2 * LOG(gaussR) / gaussR)
  gaussSet = gaussV1 * gaussFac
  iGaussCalled% = 1
  retGaussRnd = gaussV2 * gaussFac
ELSE
  retGaussRnd = gaussSet
  iGaussCalled% = 0
END IF
RETURN
    
```

LorentzRnd:

```

'--- Lorentzian distribution (see p.217 of NR) ---
LorentzLoop:
  lorentzR = RND(1)
  IF (lorentzR < 3.141592 * 1.1 / 2) AND (lorentzR > 3.141592 * .9 / 2)
  THEN GOTO LorentzLoop
  retLorentzRnd = TAN(3.141592 * lorentzR)
RETURN
    
```

EXTRReport:

```

'--- External loop report ---
WINDOW 1
PRINT #1, "ip="; iproblem%; "c="; EXTCost; "T="; T
PRINT #1, "E="; EXT%; "RF="; epsRndFac; "Cost"; iCost &
PRINT #1, "iGasp="; iLastGasp%; "retCost"; retCost
PRINT #1, "Accept"; iAccept%; "gAccept"; gAccept%
GOSUB XReport
PRINT #1, "
EXTRReportLoop:
  IF (MOUSE(0) <> 0) THEN GOTO EXTRReportLoop
RETURN
    
```

FinalReport:

```

'--- Final resume ---
WINDOW 1
PRINT #2, "ip="; iproblem%; "c="; icount%; "
T="; oldT; "E="; EXT%; "RF="; epsRndFac;
PRINT #2, "Cost="; iCost & "c="; optCost
'--- print out X values ---
PRINT #2, "X: ";
FOR D% = 1 TO nX%
  PRINT #2, USING "##.#### "; optX(D%);
NEXT
PRINT #2, "
RETURN
    
```

XReport:

```

'--- print out X values ---
PRINT #1, "X: ";
FOR D% = 1 TO nX%
  PRINT #1, USING "##.#### "; X(D%);
  IF (D% MOD 5 = 0) THEN PRINT "
NEXT
PRINT #1, "
RETURN
    
```

Xpoint:

```

'--- point a circle ---
WINDOW 2
marksiz% = 2
rect%(0) = 300 * (-minX(2) + X(2)) / rangeX(2) - marksiz%
rect%(1) = 300 * (-minX(1) + X(1)) / rangeX(1) - marksiz%
rect%(2) = 300 * (-minX(2) + X(2)) / rangeX(2) + marksiz%
rect%(3) = 300 * (-minX(1) + X(1)) / rangeX(1) + marksiz%
IF (retAccept% = 1) THEN
  CALL PAINTOVAL(VARPTR(rect%(0)))
ELSE
  CALL FRAMEOVAL(VARPTR(rect%(0)))
END IF
RETURN
    
```

Tpoint:

```

'--- point a circle ---
WINDOW 2
marksiz% = 2
rect%(1) = 50 * ABS(LOG(oldT / initT)) / LOG(10) - marksiz%
rect%(0) = 50 * ABS(LOG(ABS(retCost / initCost))) / LOG(10) - marksiz%
rect%(3) = 50 * ABS(LOG(oldT / initT)) / LOG(10) + marksiz%
rect%(2) = 50 * ABS(LOG(ABS(retCost / initCost))) / LOG(10) + marksiz%
IF (inner% = 0) THEN
  CALL PAINTOVAL(VARPTR(rect%(0)))
ELSE
  CALL FRAMEOVAL(VARPTR(rect%(0)))
END IF
RETURN
    
```

SUB G1(xx, retG1) STATIC

```

  retG1 = 0
  FOR P% = 1 TO 6
    retG1 = retG1 + P% * COS((P%+1) * xx + 1)
  NEXT
END SUB
    
```

SUB G1beta(xx, yy, beta, retG1beta) STATIC

```

  CALL G1(xx, dummy)
  CALL G1(yy, retG1beta)
  retG1beta = retG1beta * dummy
  retG1beta = retG1beta + beta * ((xx - .42513)^2 + (yy + .1997)^2)
END SUB
    
```