Pvote Software Review Assurance Document

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suggestions that have led to substantial improvements. David Wagner,
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Chapter 1

Scope

This document is a preparatory guide for reviewers of the Pvote software for voting machines, which is based on the prerendered user interface approach. Pvote is implemented in a subset of Python.

Pvote is not a complete voting system. It is just the component responsible for presenting the ballot to the voter and recording the voter’s selections. (The EVT paper on prerendered user interfaces for voting argues that this is a crucial component to get right because the voting interactions of individual voters must be kept secret, whereas other parts of the process can be made publishable.) Voter registration, vote tallying, and administrative functions are not part of Pvote.

The following sections set out expectations for the scope of the review based on Pvote’s design assumptions and design intent. However, as reviewers, if you find it necessary to look beyond the scope suggested here, you should feel free to direct the course of the review as you see fit.

1.1 Overview

Pvote is intended to be small and not changed often. The election parameters and the voting user interface are described by a ballot definition file that Pvote accepts as input. Pvote is flexible enough to support a wide range of election types and interface designs, just by using different ballot definition files. It can be considered a virtual machine for a high-level user interface specification language.

Pvote could be used as the core user interface component of a cryptographically auditable voting system, an electronic ballot marking or printing device, a DRE with a paper or audio audit trail, or (gasp!) a paperless DRE.

1.2 Responsibilities

We say committed to mean voter selections are finalized as far as the machine is concerned — for a DRE this means “recorded” or “cast,” but for a ballot printer this means “printed.” A voting session consists of the time from when a voting machine starts interacting with a particular voter (e.g. when the first screen of the voting user interface comes up) until the ballot is committed or the voter abandons the machine. This does not include per-voter initialization steps by pollworkers.
We intend to establish that Pvote can be relied upon to do the following:

R1. Never abort during a voting session. (Specifically, given any particular ballot definition, Pvote should either always reject it as invalid and abort immediately without starting a voting session, or always accept it as valid and never abort during any voting session with that ballot definition.)

R2. Remain responsive during a voting session.

R3. Become inert after a ballot is committed.

R4. Display a completion screen when and only when a ballot is committed, and continue to display this screen until the next session begins.

R5. Exhibit behaviour in each session independent of any previous sessions.

R6. Exhibit behaviour independent of which parts of buttons are touched (all touch points within a target region should be equivalent).

R7. Exhibit behaviour that is determined entirely by the ballot definition and the stream of user input events and their timing.

R8. Commit valid selections (no overvotes and no invalid candidates or contests).

R9. Commit the ballot when and only when so requested by the voter.

R10. Correctly and unambiguously commit the selections the voter made.

Pvote should also do the following correctly, according to the ballot definition:

R11. Present instructions, contests, and options as specified.

R12. Navigate among instructions, contests, and options as specified.

R13. Select and deselect options according to user actions as specified.

R14. Correctly indicate which options are selected, when directed to do so.

R15. Correctly indicate whether options are selected, when directed to do so.

R16. Correctly indicate how many options are selected, when directed to do so.

1.3 Assumptions

A1. The voting machine software (ostensibly Pvote) is handed over for review before the election.

A2. The software that runs on the voting machines on election day is exactly what was reviewed.

A3. Pvote is started once per voting session.

A4. Only authorized voters are allowed to carry out voting sessions.

A5. Ballot definition files are published for review and testing before the election.

A6. The correct ballot definition is selected and used for each voting session.

A7. The ballot definitions used on election day are intact, exactly as they were reviewed.

A8. The programming language functions correctly (according to the behaviour specified in Chapter 3).

A9. The operating system and software libraries function correctly (according to the behaviour specified in Chapters 4 and 5).

A10. The voting machine hardware functions correctly.
1.4 Threats in scope

- **Voters.** Voters can interact with Pvote using the touchscreen and keypad. Is there any sequence of interactions that can cause Pvote to allow a voter to commit multiple ballots (R3), allow committing of an invalid ballot (R8), mislead pollworkers about whether a ballot has been committed (R4), or violate voter privacy (R5)?

- **Bugs.** Though bugs are not usually considered security threats in the sense of being willful attackers, they do threaten the integrity of the election. Can any valid ballot definitions or user interactions ever cause Pvote to behave incorrectly (R1, R2, R6, R7, R8, R9, R10, R11, R12, R13, R14, R15, R16)?

- **Insiders among voting software suppliers.** Pvote could be modified to contain backdoors or hidden weaknesses before being handed over for review and installation. Could an attacker make effective changes that would go unnoticed by reviewers? What effect does Pvote have on the difficulty of performing or detecting such subversion? (This is the “meta-threat” corresponding to the two preceding items.)

- **Insiders among election officials.** Ballot definitions could be designed or altered to contain the wrong information or bias the vote. Could an attacker subvert ballot definitions in a way that would go unnoticed by reviewers and testers? What effect does Pvote have on the difficulty of performing or detecting such subversion?

1.5 Threats out of scope

- **Insiders among pollworkers.** We are relying upon pollworkers not to give voters multiple sessions (A3), not to let unauthorized people vote (A4), and to select the correct ballot style for each voter (A6). We assume election procedures make it hard for an insider working alone to violate these rules.

- **Tampering with the software distribution.** We assume the software is not altered between review and use (A1, A2).

- **Tampering with the ballot definition.** We assume the ballot definition is not altered between review and use (A5, A7).

- **Tampering with cast vote records.** We assume that if Pvote is used in a DRE, some other mechanism will be responsible for protecting the integrity of the vote records that Pvote outputs.

- **Faulty or subverted non-voting-specific software.** We assume that the software components that are not specific to voting function correctly (A8, A9). The threat of attacks on Pvote via these software components can be largely eliminated by choosing to use versions of such software that were released before Pvote was created.

- **Faulty or subverted hardware.** This is a software review (A10).

- **Poor ballot design.** We don’t claim that using Pvote eliminates accessibility or usability problems, though testing with the published ballot definitions might help reveal some of these problems in time to address them.
1.6 Other questions to consider

Depending on the time available, we may be able to look at a broader set of questions surrounding Pvote.

Testing is an issue closely related to security and reliability that may be worth examining. How would Pvote affect the testing process?

- Does Pvote change the required amount of testing?
- Does Pvote change the level of confidence attainable through testing?
- Does Pvote increase or decrease the effectiveness of existing kinds of testing?

Some types of testing to consider are:
- unit testing
- system testing
- manual testing
- automated testing
- parallel testing
- logic and accuracy testing

- Does Pvote make feasible any new kinds of tests?

How does using Pvote affect the ability to mix and match components from different vendors, and what influence would this have on testing and reliability?

How does using Pvote affect the difficulty of reviewing the voting system?

Post-election audits are also an important diagnostic and recovery tool. How does Pvote affect the ability to audit the voting system?

Finally, there is the question of integration with existing and proposed systems and practices. Running an election requires many other components in addition to Pvote. How would or could Pvote interoperate with these other components? How does it compare with, and interoperate with, other software-independent approaches to electronic voting?
Chapter 2

Ballot Definition Format

The format of the ballot definition file is central to Pvote’s design, as it specifies all the capabilities of the voting user interface. The ballot definition describes a state machine where each transition is triggered by a user action or by an idle timeout. Executing a transition can cause options to be selected or deselected. Audio feedback can be associated with states and with transitions between states.

2.1 Overview

The ballot definition contains four parts:

- **Ballot model**: structure of the ballot and interaction flow of the user interface.
- **Text data**: information for the printer.
- **Audio data**: sound data for the audio driver.
- **Video data**: image and layout data for the video driver.

The ballot model consists of:

- **Groups**: sets of options for the voter to select.
- **Pages**: the coarse-grained unit of navigation; a full-screen display state. Pages contain finer-grained **states** for navigation within a page. Both pages and states have **bindings**, which map keypresses and screen touches to selection and navigation actions. Pages and states specify audio feedback in terms of sequences of audio **segments**. Both bindings and segments may be subject to **conditions** concerning the voter’s current selections. Finally, **areas** are parts of the page that change according to the voter’s selections.

The text data contains the names of the contests and candidates. The audio data contains a collection of sound clips. The video data contains:

- **Layouts**: the visual appearance of a page. Each layout corresponds to one page. The layout contains a full-screen image for the page. It also specifies the locations of **targets** (screen regions that respond to touch) and **slots** (screen regions where sprites are pasted). Targets invoke bindings; areas are associated with slots.
- **Sprites**: smaller images for pasting over variable parts of the display.
The next few sections will describe in more detail the contents of these data structures and what they mean, and set out the constraints that have to be met for a ballot definition file to be considered valid.

2.2 Data types and their serialization

2.2.1 Primitive types

The data structures are built up from the following types:

- **int**: An integer in the range from 0 to 2147483647 (0x7fffffff) inclusive. Serialized as four bytes, most significant first.

- **intn**: An integer in the range from 0 to 2147483647 (0x7fffffff) inclusive, or the special value None. An integer value is serialized as four bytes, most significant first; the value None is serialized as "\xff\xff\xff\xff".

- **bool**: A Boolean value. Truth is serialized as "\x00\x00\x00\x01" and falsehood is serialized as "\x00\x00\x00\x00".

- **enum**: A value from a finite set of identifiers. Each of the three uses of enum (in Step, Segment, and Condition) has a distinct domain. Values of an enum correspond to small integers and are serialized in the same way as an int.

- **str**: A string of ASCII bytes with length from 0 up to 2147483647, where each byte is at least 32 and at most 125. Serialized as a four-byte integer length followed by the bytes of the string.

- **pixel**: A pixel colour with red, green, and blue components, each ranging from 0 to 255 inclusive. Serialized as three bytes (red, green, blue).

- **sample**: An individual audio sample value ranging from -32768 to 32767 inclusive. Serialized as a 16-bit signed integer, most significant byte first.

2.2.2 Compound types

The top-level compound type for the entire ballot definition is **Ballot**. A ballot definition file consists of an 8-byte identifying header, followed by the serialized content of the Ballot structure, followed by the 20-byte SHA-1 digest of the serialized content. The header is "Pvote\x00\x01\x00", where the last two bytes are the major and minor version number of the format.

Figure 2.1 depicts the exact structure of Ballot, which is shown as the heavy box at the top. Within this box, the internal structure of all its constituent types is revealed, except for Binding and Segment, which are described in the boxes below. The figure shows all the fields in the order they are serialized. Each compound type is serialized simply by concatenating its serialized fields with no padding.

Many fields contain lists of elements. A list can have from 0 to 2147483647 elements. A list is serialized as a four-byte integer length followed by all the elements serialized in order. All the list fields (those marked with []) are serialized in this fashion, except the pixels field of an Image. The pixels field is serialized with no length, since the length is already determined by the width and height fields of the Image.
Figure 2.1: Ballot definition data structures. A double border around a subelement signifies a list of subelements of that type.
2.3 Model

The model contains Groups, which describe the ballot structure, and Pages, which describe the user interface. The model also has one integer field, timeout_ms, which specifies an idle timeout in milliseconds. A timeout is defined to occur when there has been no user activity and no audio playing for timeout_ms milliseconds. The ballot definition can specify an automatic transition or audio message to occur in case of a timeout.

Each field whose name ends with _i is an integer index that refers to an element of a list elsewhere in the structure.

2.3.1 Groups

A Group is a container of selectable options. Groups are used for two purposes: as contest groups and as write-in groups. A contest group represents an actual contest on the ballot; its options are options such as candidates. A write-in group represents a single write-in entry field; its options are the individual characters that can appear in the entry field. In all cases, the current selection for a group is a list of options (even though a contest selection has set-like semantics and a write-in selection has ordered sequence semantics). The fields in a Group are:

- max_sels: The maximum allowed number of selections in the group.
- max_chars: For contest groups, this is the maximum number of characters that can be entered for any write-in option in the contest. If this is zero, the contest has no write-ins. For write-in groups, max_chars must be zero.
- option_clips: The number of audio clips associated with each option.
- options: The list of options in the group.

Each option (in any kind of group) is associated with exactly two sprites, one to display when the option is selected, and one to display when it is not selected. Each option can be associated with any number of audio clips (the same number for all options in a group, specified by option_clips in the Group). These come from the sprites and clips lists in the Video and Audio structures, respectively.

There are three fields in an Option:

- sprite_i: An index into video.sprites. The sprite at index sprite_i is shown for the selected option, and the sprite at index sprite_i + 1 is shown for the unselected option.
- clip_i: An index into audio.clips. The clips with indices from clip_i to clip_i + option_clips − 1 are used to represent the option.
- writein_group_i: If this field is None, this option is a regular option. Otherwise, this option is a write-in option; writein_group_i specifies the write-in group that will hold the text entered for this write-in.

Note the logical relationships among these fields. If a group’s max_chars is zero, then all its options must have None as their writein_group_i. Only in a contest group may writein_group_i can take on values other than None; these values must be the indices of write-in groups. The referenced write-in groups must have max_chars set to zero and max_sels equal to the contest group’s max_chars. These relationships are summarized in the following table.
2. Ballot Definition Format

<table>
<thead>
<tr>
<th>Type of group</th>
<th>Kinds of options it contains</th>
<th>writein_group_i</th>
</tr>
</thead>
<tbody>
<tr>
<td>contest group</td>
<td>regular option</td>
<td>None</td>
</tr>
<tr>
<td>(max_chars ≥ 0)</td>
<td>write-in option</td>
<td>index of a write-in group</td>
</tr>
<tr>
<td>write-in group</td>
<td>character option</td>
<td>None</td>
</tr>
<tr>
<td>(max_chars = 0)</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Table 2.1: Types of groups and the options they contain.

2.3.2 Pages

The Page represents an overall display appearance such as a page of instructions or a selection page for a particular contest. The fields in a Page are as follows:

- **bindings**: Bindings that apply in all the states in this page.
- **states**: States that belong to this page (i.e. have this overall appearance).
- **option_areas**: Parts of the visual display that show specific options and indicate whether the options are selected or unselected.
- **counter_areas**: Parts of the visual display that change based on the number of options that are selected in a particular group.
- **review_areas**: Parts of the visual display that list all the selected options (with their write-in text, if any) in a particular group.

There is a one-to-one correspondence between pages and layouts: item $i$ in the Model’s list of pages corresponds to item $i$ in the Video’s list of layouts. The corresponding Layout gives the full-screen image for the page. The slots in the Layout also correspond to elements of the page: if there are $s$ states, $o$ option areas, $c$ counter areas, and $r$ review areas, then the states get the first $s$ slots in the list, the option areas get the next $o$ slots, the counter areas get the next $c$ slots, and the review areas get the rest.

An OptionArea has two fields, `group_i` and `option_i`, which give the index of a group in the Model’s groups and the index of the option in that group’s list of options that will appear in the option area’s slot.

A CounterArea has two fields, `group_i` and `sprite_i`. The sprite at index $sprite_i + n$ will appear in the counter area’s slot, where $n$ is the number of options currently selected in group `group_i`.

A ReviewArea has two fields, `group_i` and `cursor_sprite_i`. For each of the selected options in group `group_i`, the review area uses one slot for the option and max_chars slots for its write-in characters, for a total of $(1 + \text{max_chars}) \times \text{max_sels}$ slots. The `cursor_sprite_i` field can be None, or it can specify a sprite to be shown in the first unused option slot when the group is not full.

The actual states of the state machine are represented by the State data structure. The states are grouped into pages because several states often share a similar display appearance (e.g. states could highlight different user interface elements in a fixed layout of elements on the screen) and similar behaviours (e.g. the “next page” button, a common element of voting user interfaces, takes you to a new screen regardless of which element has the focus on the current screen). Organizing states into pages reduces redundancy and simplifies the work of ballot definition creators and reviewers.
A **State** has these fields:

- **sprite_i**: A sprite to be displayed in the state’s slot while in this state.
- **segments**: A list of audio segments (see **Audio feedback** below).
- **bindings**: Bindings that apply to just this state. These override page-level bindings; when the user presses a key or touches a target, an operative binding is sought first in the **State** and then in the **Page**.
- **timeout_segments**: A list of audio segments to be played upon timeout (see **Audio feedback** below).
- **timeout_page_i, timeout_state_i**: The state to automatically enter upon timeout. If **timeout_page_i** is None, no automatic transition occurs.

**User input**

The lists of **Bindings** in pages and states specify behaviour in response to user input. Each binding specifies a triplet of stimulus, condition, and response.

There are two kinds of stimuli: keypresses, which are received as an integer key code, and screen touches, which are translated into a target index by looking up the screen coordinates of the touch point in the layout’s list of targets. A binding can specify either a key code or a target index or both. A binding is said to **match** the stimulus if it specifies the pressed key or touched target.

The condition specifies constraints on the current selection state in order for the binding to apply. A binding is considered **operative** if its condition is satisfied.

The response consists of three parts: selection operations (given as **Steps**), audio feedback (given as **Segments**), and navigation. To **invoke** a binding is to carry out the response. When the user provides a stimulus, at most one binding is invoked: the first matching, operative binding found in the current state or the current page.

The fields in a **Binding** are:

- **key**: A key code that this binding will match.
- **target_i**: A target index that this binding will match.
- **conditions**: A list of **Conditions** that must all be satisfied in order for this binding to be operative.
- **steps**: A list of **Steps** to be carried out when this binding is invoked.
- **segments**: A list of **Segments** to be played when the binding is invoked.
- **next_page_i, next_state_i**: The state to enter when this binding is invoked. If **next_page_i** is None, no state transition occurs.

A **Condition** has four fields:

- **predicate**: One of the following predicate types.
  0. **PR_GROUP_EMPTY**: Satisfied when a group is empty.
  1. **PR_GROUP_FULL**: Satisfied when a group is full.
  2. **PR_OPTION_SELECTED**: Satisfied when a specific option is selected.
- **group_i, option_i**: Identifies the group or option to which the predicate is applied (see **Group and option references** below).
- **invert**: If true, the sense of the condition is inverted.
A **Step** has three fields:

- **op**: One of the following operation types.
  0. **OP_ADD**: Append the specified option to its group’s selection list if not already present.
  1. **OP_REMOVE**: Remove the specified option from its group’s selection list if it is present.
  2. **OP_APPEND**: Append the specified option to its group’s selection list.
  3. **OP_POP**: Remove the last option from the specified group’s selection list.
  4. **OP_CLEAR**: Clear the specified group’s selection list.

- **group_i, option_i**: Identifies the group or option to which the operation is applied (see **Group and option references** below).

**Audio feedback**

Audio feedback is specified as a list of segments. Some segments simply play a particular clip; others can play different clips depending on the selection state.

At any given moment, at most one clip can be playing at a time; there is a play queue for clips waiting to be played next. Whenever a clip finishes playing, the next clip from the queue immediately begins to play, unless the queue is empty.

Invoking a binding always interrupts any currently playing clip and clears the play queue. The segments for the binding, if any, are queued first; if a state transition occurs, the segments for the newly entered state are queued next.

The fields in a **Segment** are:

- **conditions**: A list of **Conditions** that must all be satisfied in order for this segment to be considered (otherwise, it is skipped). The conditions are evaluated when the segment list is being queued, immediately after executing the steps of a **Binding**, after entering a new **State**, or on timeout.

- **type**: One of the following segment types.
  0. **SG_CLIP**: Play the clip at clip_i.
  1. **SG_OPTION**: Play the clip at offset clip_i from the specified option’s clip_i. If the option has a write-in group, also play the clips for all the selected options in the write-in group (when playing the character options for a write-in, use each option’s clip_i with no offset).
  2. **SG_LIST_SELS**: For each selected option in the specified group, play the clip at offset clip_i from the selected option’s clip_i. If the option has a write-in group, also play the clips for all the selected options in the write-in group (use each option’s clip_i with no offset).
  3. **SG_COUNT_SELS**: Play the clip at offset n from the specified clip_i, where n is the number of selected options in the specified group.
  4. **SG_MAX_SELS**: Play the clip at offset n from the specified clip_i, where n is max_sels for the specified group.

- **clip_i**: A clip index or offset applied to a clip index, depending on type.

- **group_i, option_i**: Identifies the option or group for which a clip is played (see **Group and option references** below).
Group and option references

In a Condition, Step, or Segment, the pair of fields group_i and option_i is used to refer to a group or option. If group_i is None, then option_i is the index of an OptionArea on the current page; the pair (group_i, option_i) indirectly refers to the group or option of this OptionArea. Otherwise, the pair (group_i, option_i) directly refers to group group_i in the Model’s list of groups or option option_i in that Group’s list of options.

2.4 Text

The text data provides textual labels for groups and options so that the user’s selections can be printed out. The Text structure has just one field, groups, which is a list of of TextGroups. Each TextGroup has three fields:

- name: The name of the group.
- writein: If true, the group is to be printed as a write-in group. Otherwise, the group is to be printed as a contest group.
- options: A list of the names of the options in the group.

2.5 Audio

The Audio structure contains two fields:

- sample_rate: The playback rate in samples per second.
- clips: A list of audio clips, referenced by index in Option and Segment structures.

Each clip is a Clip structure, which contains just one field:

- samples: A list of signed 16-bit samples. Audio clips have one channel.

2.6 Video

The Video structure has the following fields:

- width, height: The display screen resolution.
- layouts: A list of Layouts, one for each Page in the Model.
- sprites: A list of Images for pasting onto the display, referenced by index in Option, State, and ReviewArea structures.

The fields in a Layout are as follows:

- screen: The full-screen page image (over which sprites will be pasted).
- targets: A list of rectangular screen regions where touches will be detected and acted upon.
- slots: A list of rectangular screen regions where sprites will be pasted.

Images are specified as an integer width and integer height followed by pixel data (3 bytes per pixel). The rectangular regions for targets and slots are specified as four integers, left, top, width, and height.
2.7 Validity constraints

A ballot definition is considered valid if it meets the constraints in this section. These constraints are intended to be sufficient (though not necessary) to ensure that Pvote will not terminate abnormally through a fatal runtime error at the language level or illegal calls to library routines. Possible causes of such errors are pointed out in the specifications given in Chapters 3, 4, and 5. For example, these constraints try to ensure that list indices will be within bounds, but not that every option appears on the ballot. No rules can enforce the correctness of the user interface, so the job of helping humans evaluate ballot designs is left to other tools (which can apply usability recommendations or region-specific election rules).

The following specification of the data structures is annotated with validity constraints on the right. In these constraint expressions, all arithmetic is performed with mathematical integers. \(\text{length}(x)\) refers to the length of a list \(x\), and the symbol \(\triangleq\) means “sizes match” (that is, \(a \triangleq b \iff a.\text{width} = b.\text{width} \text{ and } a.\text{height} = b.\text{height}\)). For brevity, some unqualified names are used:

- groups and pages refer to the fields of the Model object
- group and page refer to the Group or Page containing the current element
- clips refers to the field of the Audio object
- sprites refers to the field of the Video object

<table>
<thead>
<tr>
<th>Ballot:</th>
</tr>
</thead>
<tbody>
<tr>
<td>Model model</td>
</tr>
<tr>
<td>Text text</td>
</tr>
<tr>
<td>Audio audio</td>
</tr>
<tr>
<td>Video video</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Model:</th>
</tr>
</thead>
<tbody>
<tr>
<td>Group[] groups</td>
</tr>
<tr>
<td>(\text{length}(\text{groups}) = \text{length}(\text{text.groups}) &gt; 0)</td>
</tr>
<tr>
<td>Page[] pages</td>
</tr>
<tr>
<td>(\text{length}(\text{pages}) = \text{length}(\text{layouts}) &gt; 0)</td>
</tr>
<tr>
<td>int timeout_ms</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Group:</th>
</tr>
</thead>
<tbody>
<tr>
<td>int max_sels</td>
</tr>
<tr>
<td>int max_chars</td>
</tr>
<tr>
<td>int option_clips</td>
</tr>
<tr>
<td>Option[] options</td>
</tr>
<tr>
<td>(\text{option_clips} &gt; 0)</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Option:</th>
</tr>
</thead>
<tbody>
<tr>
<td>int sprite_i</td>
</tr>
<tr>
<td>(\text{sprite}_i + 1 &lt; \text{length}(\text{sprites}))</td>
</tr>
<tr>
<td>sprites[\text{sprite}_i] \triangleq sprites[\text{sprite}_i + 1] \triangleq \text{group's option size}</td>
</tr>
<tr>
<td>int clip_i</td>
</tr>
<tr>
<td>(\text{clip}_i + \text{group.option_clips} - 1 &lt; \text{length}(\text{clips}))</td>
</tr>
<tr>
<td>intn writein_group_i</td>
</tr>
<tr>
<td>writein_group_i \neq \text{None} \Rightarrow (\text{writein_group}_i &lt; \text{length}(\text{groups}) \text{ and} \text{groups[writein_group}_i].\text{max_chars} = 0 \text{ and} \text{\forall option} \in \text{groups[writein_group}_i].\text{options}: \text{sprites[option.sprite}_i] \triangleq \text{group's character size})</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Page:</th>
</tr>
</thead>
<tbody>
<tr>
<td>Binding[] bindings</td>
</tr>
<tr>
<td>State[] states</td>
</tr>
<tr>
<td>(\text{length}(\text{states}) &gt; 0)</td>
</tr>
<tr>
<td>OptionArea[] option_areas</td>
</tr>
<tr>
<td>CounterArea[] counter_areas</td>
</tr>
<tr>
<td>ReviewArea[] review_areas</td>
</tr>
</tbody>
</table>
State:
25 int sprite_i
sprite_i < length(sprites)
26 segments
27 intn group_i
28 intn option_i
29 sprites[sprite_i] = slots[state_i]

Segment[] segments
30 timeout_segments
31 intn timeout_page_i
32 intn timeout_state_i
timeout_page_i ≠ None ⇒ timeout_page_i < length(pages)
timeout_state_i ≠ None ⇒ timeout_state_i < length(page[timeout_page_i].states)

Binding[] bindings
33 timeout_segments
34 intn timeout_page_i
35 intn timeout_state_i

OptionArea:
36 int group_i
group_i < length(groups)
37 int option_i
option_i < length(groups[group_i].options)

CounterArea:
38 int group_i
group_i < length(groups)
39 int sprite_i
sprite_i < length(groups[group_i].max_sels < length(sprites)

ReviewArea:
40 int group_i
group_i < length(groups)
41 intn cursor_sprite_i
cursor_sprite_i ≠ None ⇒ (cursor_sprite_i < length(sprites) and
42 sprites[cursor_sprite_i] = groups[group_i].option_size)
43 intn target_i
44 Condition[] conditions
45 Step[] steps
46 Segment[] segments
47 intn next_page_i
48 intn next_state_i
next_page_i ≠ None ⇒ next_page_i < length(pages)
next_state_i ≠ None ⇒ next_state_i < length(page[next_page_i].states)

Condition:
49 enum predicate
50 group_i ≠ None ⇒ group_i < length(groups)
51 int group_i
group_i = None ⇒ option_i < length(page.option_areas)
52 int option_i
53 bool invert
group_i ≠ None ⇒ option_i < length(groups[group_i].options)

Step:
54 enum op
55 group_i ≠ None ⇒ group_i < length(groups)
56 int group_i
group_i = None ⇒ option_i < length(page.option_areas)
57 int option_i
group_i ≠ None ⇒ option_i < length(groups[group_i].options)

Segment:
58 Condition[] conditions
59 enum type
type ∈ {0, 1, 2, 3, 4}
60 int clip_i
type = 0 ⇒ clip_i < length(clips)
type ∈ {1, 2} ⇒ clip_i < length(groups[g].options)
61 type ∈ {3, 4} ⇒ clip_i + groups[g].max_sels < length(clips)
62 where g = group_i if group_i ≠ None, or
63 g = page.option_areas[option_i].group_i otherwise
64 intn group_i
group_i ≠ None ⇒ group_i < length(groups)
65 int option_i
type ≠ 0 and group_i = None ⇒ option_i < length(page.option_areas)
type ≠ 0 and group_i ≠ None ⇒ option_i < length(groups[group_i].options)
Some of the above constraints refer to the option area’s slot, counter area’s slot, and review area’s slots, which are slots taken from the slots list of the page’s corresponding Layout object, as described in Section 2.3.2.

The size constraints on sprites and slots also refer to the option size and character size of a group, even though the Group structure doesn’t have fields for specifying option size and character size. This just means that all the objects that are required to match a particular group’s option size must all have the same size, and all the objects that are required to match a particular group’s character size must all have the same size.

The constraints requiring each Clip to have a nonzero length and each Image to have nonzero width and height are present due to a Pygame limitation: Pygame refuses to create zero-length sounds or zero-sized images. Were it not for this limitation, they would be unnecessary—it would be logical for playing a zero-length clip or pasting a zero-sized image to have no effect.
Chapter 3

Pthin

Though the implementation of Pvote is developed, tested, and demonstrated on the open-source Python interpreter (versions 2.3, 2.4, and 2.5), it only uses a small subset of the Python language. To limit the scope of the review and to save the reviewers from having to read the entire Python reference manual, this section defines “Pthin”, a subset of Python sufficient to run Pvote. Differences between the Pthin specification and the behaviour of the Python interpreter are out of scope for this review.

3.1 Types

Values in Pthin are typed, but variables are not. There is a unique special value called None whose only supported operation is comparison to None. Aside from None, there are six types of values in Pthin: integers, strings, lists, functions, classes, and objects.

Integers are signed and unlimited in size. Integer literals are written in decimal.

Strings are variable-length arrays of 8-bit bytes. String literals are written exactly as in C. Null bytes have no special significance.

Lists are variable-length arrays of Pthin values. Lists can be heterogeneous and can contain values of any type as elements. List literals are written in square brackets with elements separated by commas.

Functions may take any number of arguments and always return one value. Functions are defined with the def keyword (see Section 3.4 for more on functions).

Classes contain method definitions and can be invoked to instantiate objects. Classes are defined with the class keyword (see Section 3.5 for more on classes).

Objects are instances of classes. Each object contains its own public namespace, accessed with a dot. For example, if x is an object, then x.foo = 3 binds foo to 3 in the namespace belonging to x. An object’s methods are simply functions residing in its namespace (see Section 3.5 for more on methods).

Table 1 is a summary of expressions involving these types. When the arguments to an operation are of unacceptable types, a fatal runtime error occurs.

Assignment binds a name to a reference, lists and object namespaces contain references, and arguments are passed by reference. (This works like Scheme or Java with objects only: all values are boxed, even integers.)
3. Pthin

**Expression** | **Preconditions** | **Definition**
---|---|---
(expr) |  | evaluate expr
None |  | literal for the special value None
123 |  | integer literal
"abc" |  | string literal
[expr1, expr2, ...] |  | list literal
[expr for name in l] |  | evaluate expr with name bound to each element of l
f(arg1, ...) | arguments match f's arity | call a function
c(arg1, ...) | arguments match c's arity | create an object that is an instance of c
o.field | field is bound in o's namespace | access a field in the object o's namespace
s[i:j] | 0 ≤ i ≤ j < length of s | get a substring (skip first i bytes, get next j - i bytes)
l[i] | 0 ≤ i < length of l | get the element of l at index i (counting starts at zero)
i * j |  | multiply
i / j |  j ≠ 0 | divide and round down
i % j |  j ≠ 0 | i - j*(i/j)
s * i |  i ≥ 0 | concatenate i copies of s to make a new string
i + j |  | add
i - j |  | subtract
l + m |  | concatenate two lists to make a new list
s + t |  | concatenate two strings to make a new string

**Comparison operators can be chained (e.g. 10 <= x < 20). The result is the conjunction of all the comparisons.**

i == j | 1 if i = j; 0 otherwise
i != j | 1 if i ≠ j; 0 otherwise
i == None | 1 if i is None; 0 otherwise
i != None | 1 if i is not None; 0 otherwise
i < j | 1 if i < j; 0 otherwise
i > j | 1 if i > j; 0 otherwise
i <= j | 1 if i ≤ j; 0 otherwise
i >= j | 1 if i ≥ j; 0 otherwise
s == t | 1 if s and t are identical strings; 0 otherwise
s != t | 1 if s and t are different strings; 0 otherwise
i in l | 1 if i is an element of l; 0 otherwise
i not in l | 1 if i is not an element of l; 0 otherwise
not i | 1 if i is zero; 0 otherwise
i and j | 1 if i and j are both nonzero; 0 otherwise
i or j | 1 if i or j or both are nonzero; 0 otherwise

Table 3.1: Expression syntax, with operators grouped by precedence (highest at the top). The above expressions are only legal with the types of operands indicated: i and j are integers, s and t are strings, l and m are lists, f is a function, c is a class, o is an object, and x is a value of any type. If operands of unacceptable types are used in these expressions or a precondition is violated, a fatal error occurs.
3.2 Namespaces

Bindings are created by assignment statements, the for statement, function definitions, and class definitions. Bindings can exist in three types of namespaces: global namespaces, local namespaces, and object namespaces.

Each Pthin file has one global namespace. Whenever a function is invoked, a new local namespace is created for the execution frame, and it lasts until the frame is exited.

Pthin has lexical scoping with just two levels. When names are bound outside of a function, the binding is created in the global namespace. When names are bound inside of a function, the binding is created in the local namespace.

Within a function, names can refer to bindings in the global or local namespace. A name refers to a local binding if a binding to that name exists anywhere within the function definition. Otherwise, the name refers to a global binding.

Every object has its own public object namespace. Object namespaces are always accessed explicitly using the dot operator on the object.

3.3 Statements

Many kinds of statements contain blocks of code that are syntactically delimited by indentation. A block is introduced with a colon at the end of a line. The body of the block is indented with respect to its introducing line, and ends when the indentation level returns to match the indentation of the introducing line.

The assert statement evaluates an integer-valued expression and causes a fatal runtime error if the value is zero.

The print statement sends a string to the printer.

An if statement takes the form if condition: followed by an indented block. The condition must evaluate to an integer. The block is executed if the condition is nonzero. This can be optionally followed by else: (indented to match its if) and another indented block to be executed if the condition is zero.

A while loop takes the form while condition: followed by an indented block. The condition must evaluate to an integer. Just as in C, the block is repeatedly evaluated as long as the condition is nonzero.

A for loop takes the form for name in expr: followed by an indented block. The expression expr must evaluate to a list. The for loop binds name to each element of the list in turn, executing the body once for each element.

The import statement imports Pthin modules and makes them available in the current namespace. A Pthin module is just a text file containing Pthin code, with a filename ending in .py. The statement import name creates a new object to represent the module and executes name.py using that object’s namespace as the global namespace. That is, all the global bindings in the file appear as bindings in the module object’s namespace. The module object is then bound to name. If the module has already been imported, it is not executed again; name is bound to the already existing module object.

See Table 3.2 for a summary of these statement types.
### Statement  

<table>
<thead>
<tr>
<th>Preconditions</th>
<th>Definition</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>name</strong> = x</td>
<td>create or replace a binding in the current namespace</td>
</tr>
<tr>
<td><strong>o.field</strong> = x</td>
<td>create or replace a binding in the object o’s namespace</td>
</tr>
<tr>
<td><strong>l[i]</strong> = x</td>
<td>set the element of l at index i to x</td>
</tr>
<tr>
<td><strong>[lvalue₁, ..., lvalueₙ]</strong> = l</td>
<td>assign to multiple lvalues (names, fields, or list items)</td>
</tr>
<tr>
<td>assert i</td>
<td>cause a fatal runtime error if i is zero</td>
</tr>
<tr>
<td><strong>print</strong> s</td>
<td>send s and a newline to the printer</td>
</tr>
</tbody>
</table>
| if i:  
| block | if i is nonzero, execute the first block |
| else:  
| block | otherwise execute the second block |
| while i:  
| block | execute block repeatedly as long as i is nonzero |
| for **lvalue** in l:  
| block | for each element of l, assign it to lvalue and execute block |
| **import** name₁, name₂, ... | import the modules name₁, name₂, ... from the files name₁.py, name₂.py, ... respectively |
| **def** name(param₁, param₂, ...):  
| block | create a function with parameters param₁, param₂, ... |
| **return** expr | exit a function, returning expr as the result |
| **class** name:  
|  
| def method(param₁, param₂, ...):  
| block | create a class with the given methods |
|  
| ... | |

### Table 3.2: Statements in Pthin. These are only legal with the types indicated: i is an integer, s is a string, l is a list, o is an object, and x is a value of any type. If an unacceptable type is supplied or a precondition is violated, a fatal error occurs.

### 3.4 Functions

A function is defined with the **def** keyword followed by the name of the function, a pair of parentheses surrounding a comma-separated list of parameter names, and a colon. The body of the function is an indented block. Executing a function definition binds the name to the newly created function. Here’s an example:

```python
def factorial(n):
    if n == 0 or n == 1:
        return 1
    return n * factorial(n - 1)
```

Calling a function creates a new local namespace in which the parameter names are bound to the arguments passed in. If the number of arguments does not match the number of parameters, a fatal runtime error occurs.

Within the body of a function, **return expr** exits the function with a return value. If no return statement is executed, the function returns None.
3.5 Classes and objects

A class is defined with the class keyword followed by the name of the class and a colon, then an indented block containing a series of method definitions. Each method definition is a function definition with at least one parameter. Since the object itself is always passed into a method as the first argument, the first parameter is conventionally named self.

Invoking a class creates a new object belonging to the class. The new object’s namespace acquires a binding for each method in the class. Each method definition with \( n \) parameters in the class yields a function of the same name with \( n - 1 \) parameters in the object’s namespace. Invoking this function with some arguments is equivalent to invoking the corresponding method with one extra argument, the object itself, prepended to the given argument list.

Immediately after the object is created, the function named \( \text{__init__} \) in its namespace is invoked with the arguments passed into the invocation of the class.

Here’s an example of a simple class definition:

```python
class Counter:
    def __init__(self, n):
        self.count = count
    def next(self):
        self.count = self.count + 1
        return self.count

c = Counter(5)
```

\( c = \text{Counter}(5) \) would create a new Counter object with \( c\.count \) initially bound to 5. Invoking \( c\.next() \) would increment \( c\.count \) to 6 and return 6.

3.6 Built-in functions and methods

The functions in Table 3.3 are available from any scope.

<table>
<thead>
<tr>
<th>Expression</th>
<th>Result</th>
<th>Preconditions</th>
<th>Definition</th>
</tr>
</thead>
<tbody>
<tr>
<td>range(i)</td>
<td>list</td>
<td>( i \geq 0 )</td>
<td>make a list of the ( i ) integers from 0 to ( i - 1 )</td>
</tr>
<tr>
<td>chr(i)</td>
<td>string</td>
<td>( 0 \leq i \leq 255 )</td>
<td>convert ( i ) to a one-byte string</td>
</tr>
<tr>
<td>ord(s)</td>
<td>integer</td>
<td>( \text{len}(s) = 1 )</td>
<td>convert the first byte of ( s ) to an integer</td>
</tr>
<tr>
<td>len(s)</td>
<td>integer</td>
<td></td>
<td>get the number of bytes in ( s )</td>
</tr>
<tr>
<td>list(s)</td>
<td>list</td>
<td></td>
<td>break ( s ) into a list of one-byte strings</td>
</tr>
<tr>
<td>len(l)</td>
<td>integer</td>
<td></td>
<td>get the number of elements in ( l )</td>
</tr>
<tr>
<td>enumerate(l)</td>
<td>list</td>
<td></td>
<td>make a list of pairs ([i, x]) for each element ( x ) and its index ( i )</td>
</tr>
<tr>
<td>l.append(x)</td>
<td></td>
<td></td>
<td>append ( x ) as one more element at the end of ( l )</td>
</tr>
<tr>
<td>l.remove(i)</td>
<td>None</td>
<td>( i ) is an element of ( l )</td>
<td>find and remove the first element that equals ( i ) from ( l )</td>
</tr>
<tr>
<td>l.pop()</td>
<td>any</td>
<td>( l ) is not empty</td>
<td>remove and return the last element from ( l )</td>
</tr>
<tr>
<td>open(s)</td>
<td>object</td>
<td>a file named ( s ) exists and is readable</td>
<td>open a file for reading, yielding a readable stream object</td>
</tr>
</tbody>
</table>

Table 3.3: Built-in functions and methods in Pthin. In these descriptions, \( i \) is an integer, \( s \) is a string, \( l \) is a list, and \( x \) is a value of any type.
3.7 Readable stream objects

The term “readable stream object” refers to any object with a read method that takes a single integer argument, length, and returns a string of up to length bytes. The underlying concept is that the object maintains a current position in a finitely long data stream, and each invocation of read returns the next length bytes from the data stream and advances the current position by length bytes in preparation for the next read. If there are fewer than length bytes remaining to be read, the result is a string containing whatever is left in the data stream; if the end of the stream has been reached, the result is an empty string.

Opening a file with the built-in open function returns an object that provides this protocol. Custom objects that provide this protocol can also be instantiated from class definitions that implement an appropriate read method.

3.8 Memory management

Pthin dynamically allocates memory for data and for the stack. Each Pthin file (the main program or any module being imported) is analyzed before it is executed.

3.8.1 Data

During the analysis phase, a Pthin file is scanned for literals. Memory is allocated just once for literals; their values are created and kept in a pool of constants. During execution, when an expression yields a value, memory is allocated for the value.

Every value has a reference count. The reference count is incremented whenever an assignment statement binds a global name, a local name, or a field of an object to the value. The reference count is also incremented whenever a reference to the value is placed in a list, either by assignment or the append method.

The reference count is decremented whenever a binding to the value is replaced or a name bound to the value goes out of scope. The reference count is also decremented whenever a reference to the value is removed from a list by replacement or the remove or pop methods.

Arguments and returned values are passed to and from functions and methods by pushing them onto an internal stack. Reference counts are also incremented and decremented when values are pushed onto or popped off of this stack.

When decrementing the reference count causes the count to reach zero, the memory for the value is deallocated. If the value is a list or object, the reference counts of all its elements or fields are also decremented.

3.8.2 Stack

During the analysis phase, the entire file is scanned for global names, and enough space is allocated to hold all of the global bindings. Then, every function and method declaration is scanned for local names, and the amount of space needed for each function or method’s local bindings is recorded.

Whenever a function or method is called, memory is allocated for a new stack frame, which holds the local bindings and saves the parent execution context. When the function or method returns, its stack frame is deallocated.
Chapter 4

Pygame

Pvote uses the Pygame library for graphics, sound, and user input. This section specifies the parts of Pygame that Pvote uses and their expected behaviour.

4.1 Events

A Pygame program is built around a main event loop that processes incoming events one at a time. When events occur, Pygame adds them to an internal queue. Each call to `pygame.event.wait()` waits until the queue is nonempty, then removes and returns the first event from the queue. The returned event object always has an integer field `type` specifying the kind of event, and may have other fields for details of the event, depending on the type.

<table>
<thead>
<tr>
<th>Function</th>
<th>Preconditions</th>
<th>Definition</th>
</tr>
</thead>
<tbody>
<tr>
<td><code>pygame.event.wait()</code></td>
<td></td>
<td>Wait for the next event and return an event object describing it.</td>
</tr>
<tr>
<td><code>pygame.time.set_timer()</code></td>
<td><code>event</code> is an integer event type code greater than or equal to <code>pygame.USEREVENT = 24</code> and less than <code>pygame.NUMEVENTS = 32</code>. <code>period</code> is an integer number of milliseconds.</td>
<td>Set the timer period for event type <code>event</code> to <code>period</code>. If <code>period &gt; 0</code>, an event of type <code>event</code> will be placed on the queue in <code>period</code> ms and again every <code>period</code> ms thereafter. Each event type has its own timer. If <code>period = 0</code>, the timer for event type <code>event</code> is disabled.</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Event type value</th>
<th>Definition</th>
</tr>
</thead>
<tbody>
<tr>
<td><code>pygame.KEYDOWN (2)</code></td>
<td>A key has been pressed. The integer key code is given in the <code>key</code> field of the event object.</td>
</tr>
<tr>
<td><code>pygame.MOUSEBUTTONDOWN (5)</code></td>
<td>A mouse button has been pressed. The coordinates of the mouse pointer are given in the <code>pos</code> field of the event object, which is a list of two integers.</td>
</tr>
</tbody>
</table>

Table 4.1: Pygame event operations and event types used by Pvote.
4.2 Audio

Pygame provides a mixer facility for playing audio. The mixer can play many sounds at once, though Pvote is designed specifically to avoid this capability. Sound clips are represented by Sound objects that can be told to play() themselves. Each time a Sound starts playing, it is assigned to an available Channel; the mixer mixes all the channels together (by default, there are 8 channels). A channel can be asked to trigger a notification event when its current sound clip finishes playing.

Table 4.2 summarizes the Pygame functions and methods that Pvote uses to implement audio playback.

<table>
<thead>
<tr>
<th>Function</th>
<th>Preconditions</th>
<th>Definition</th>
</tr>
</thead>
<tbody>
<tr>
<td>pygame.mixer.init(rate, format, stereo)</td>
<td>rate is a valid sample rate (11025, 22050, or 44100), format is 8 for unsigned 8-bit samples or -16 for signed 16-bit samples. stereo is 0 for mono or 1 for stereo.</td>
<td>Initialize the audio player with the given sample rate (in samples per second), sample format, and mono/stereo setting. Must be called before any other audio operations.</td>
</tr>
<tr>
<td>pygame.mixer.stop()</td>
<td></td>
<td>Stop any currently playing sounds on all channels. Any currently playing channels that previously had an end event set with set_endevent will immediately place their end events on the event queue.</td>
</tr>
<tr>
<td>pygame.mixer.Sound(stream)</td>
<td>stream is a readable stream object (see Section 3.7). When read, stream yields the contents of a valid WAV file (see Section C).</td>
<td>Create a Sound object from the audio data in the given WAV file.</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Class</th>
<th>Method</th>
<th>Preconditions</th>
<th>Definition</th>
</tr>
</thead>
<tbody>
<tr>
<td>Sound</td>
<td>play()</td>
<td></td>
<td>Start playing this sound clip and return the Channel on which the clip is playing.</td>
</tr>
<tr>
<td>Channel</td>
<td>set_endevent(event)</td>
<td>event is an integer event code greater than or equal to pygame.USEREVENT = 24 and less than pygame.NUMEVENTS = 32.</td>
<td>Set the end event for this channel. Each channel can have its own end event type. If event &gt; 0, then from now on, an event of type event will be placed on the event queue each time a sound clip stops playing on this channel. The end event can be triggered by playing to the end of the clip or by a call to stop(). If event = 0, then the sending of end events for this channel is turned off.</td>
</tr>
</tbody>
</table>

Table 4.2: Pygame audio operations used by Pvote.
4.3 Video

All drawing takes place on frame buffers represented by `Surface` objects. Initializing the video system yields a `Surface` for the display. After drawing on the surface, one must call the display’s `update` method to copy the changed contents of the frame buffer to the visible display.

Pvote constructs its visual display entirely by pasting prerendered images onto the screen. It needs to use only one drawing method, `blit`, for this purpose.

Table 4.3 summarizes the functions and methods that Pvote uses for visual display.

<table>
<thead>
<tr>
<th>Function</th>
<th>Preconditions</th>
<th>Definition</th>
</tr>
</thead>
<tbody>
<tr>
<td><code>pygame.display.set_mode(size, flags)</code></td>
<td><code>size</code> is a pair of integers <code>[width, height]</code>. <code>flags</code> is an integer.</td>
<td>Initialize the video display with a resolution of <code>width × height</code> pixels and return a <code>Surface</code> object. If <code>flags</code> is <code>pygame.FULLSCREEN</code>, the display fills the screen.</td>
</tr>
<tr>
<td><code>pygame.display.update()</code></td>
<td></td>
<td>Update the video display to reflect the contents of its surface object. (Drawing commands will alter the surface in memory, but the contents are not placed on the display until <code>update</code> is called.)</td>
</tr>
<tr>
<td><code>pygame.image.fromstring(data, size, &quot;RGB&quot;)</code></td>
<td><code>size</code> is a pair of integers <code>[width, height]</code>. <code>data</code> is a string of <code>width × height × 3</code> bytes.</td>
<td>Create an <code>Image</code> object from the pixel data in <code>data</code>, which is ordered left to right, top to bottom, and has 3 unsigned bytes per pixel (red, green, and blue values respectively).</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Class</th>
<th>Method</th>
<th>Preconditions</th>
<th>Definition</th>
</tr>
</thead>
<tbody>
<tr>
<td><code>Surface</code></td>
<td><code>blit(image, pos)</code></td>
<td><code>image</code> is an <code>Image</code> object with size <code>(width, height)</code>. <code>pos</code> is a list of two integers <code>[x, y]</code>. <code>0 ≤ x &lt; x + width ≤ width of surface. 0 ≤ y &lt; y + height ≤ height of surface.</code></td>
<td>Paste an image onto this surface with its top-left corner at the given <code>(x, y)</code> position.</td>
</tr>
</tbody>
</table>

Table 4.3: Pygame video operations used by Pvote.
Chapter 5

SHA

Pvote uses the Python SHA module to compute SHA-1 digests. After the module has been imported with the statement `import sha`, calling `sha.sha()` creates a new SHA hashing object. The SHA object supports progressively adding more input data with the `update` method; at any point the `digest` method can be called to obtain the digest of the data submitted to far.

<table>
<thead>
<tr>
<th>Function</th>
<th>Preconditions</th>
<th>Definition</th>
</tr>
</thead>
<tbody>
<tr>
<td>sha.sha()</td>
<td></td>
<td>Create a new SHA object.</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Class</th>
<th>Method</th>
<th>Preconditions</th>
<th>Definition</th>
</tr>
</thead>
<tbody>
<tr>
<td>sha</td>
<td>o.update(s)</td>
<td>s is a string.</td>
<td>Append s to the data being hashed.</td>
</tr>
<tr>
<td>sha</td>
<td>o.digest()</td>
<td></td>
<td>Return a 20-byte string with the SHA-1 digest of all the data sent to this object so far.</td>
</tr>
</tbody>
</table>

Table 5.1: SHA module operations used by Pvote.
6. PVote

Chapter 6

PVote

6.1 Design

PVote consists of seven components:

- **Main program and event loop** *(main)*: Responsible for loading the other components and receiving and dispatching Pygame events.
- **Ballot loader** *(Ballot.py)*: Responsible for deserializing the ballot definition file and verifying its header and digest.
- **Ballot verifier** *(verifier.py)*: Responsible for checking the validity of the ballot definition according to the constraints described in Section 2.7.
- **Navigator** *(Navigator.py)*: Responsible for keeping track of the user’s selections and the current state of the user interface, and performing selection, navigation, or audio feedback in response to user actions.
- **Audio driver** *(Audio.py)*: Responsible for queueing and playing audio.
- **Video driver** *(Video.py)*: Responsible for drawing the visual display.
- **Printer driver** *(Printer.py)*: Responsible for printing the committed ballot.

When PVote starts up, the ballot loader is invoked to deserialize the ballot definition into memory, and then the verifier is invoked to check the ballot definition. The purpose of the verifier is to ensure immediate termination on an invalid ballot definition, so that a fatal error cannot be caused by an illegal type, precondition violation, or assertion failure after a voting session has begun.

The remaining five components form the virtual machine (Figure 6.1) that presents the voting user interface to the voter. Each component has limited responsibilities, and there are limited data flows between components.

The **navigator** keeps track of the current page and state and the current selections in each group. The navigator responds to three messages:

- **touch** *(target_i)*: Find the first operative binding for the current state or page that matches the given target, and invoke it.
- **press** *(key)*: Find the first operative binding for the current state or page that matches the given keypress, and invoke it.
- **timeout()**: Add the timeout_segments for the current state to the play queue. Go to the page and state given by timeout_page_i and timeout_state_i if timeout_page_i is not None.
The navigator sends five messages to other modules:

- **goto**(*layout*<sub>i</sub>) is sent to the video driver upon transition to a page. The layout index is the same as the page index.
- **paste**(*sprite*<sub>i</sub>, *slot*<sub>i</sub>) is sent to the video driver to paste sprites into slots as necessary for states, option areas, counter areas, and review areas.
- **play**(*clip*<sub>i</sub>) is sent to the audio driver to queue a clip to be played on the headphones.
- **stop**() is sent to the audio driver to stop the currently playing clip.
- **write**(*selections*) is sent to the printer to commit the user's selections by printing the ballot.

The audio driver maintains a queue of audio clips to be played. It responds to two messages:

- **play**(*clip*<sub>i</sub>): If nothing is currently playing, immediately begin playing the specified clip; otherwise queue the specified clip to be played. *clip*<sub>i</sub> is an index into the list of clips in the Audio part of the ballot definition.
- **next**(): If there are any clips waiting in the queue, start playing the next one.
- **stop**(): Stop whatever is currently playing and clear the queue.

The audio driver also exposes a field named **playing** that the main loop can read to determine whether a sound clip is currently being played. Whenever the audio driver starts playing a clip, it also ensures that a notification event with event type **AUDIO_DONE** will occur when the clip finishes playing.
The **video driver** maintains one piece of state, the index of the current layout. It responds to three messages:

- **goto**(layout_i): Copy the full-screen image for the given layout into the video display’s frame buffer and set the current layout to layout_i.
- **paste**(sprite_i, slot_i): Copy the given sprite into the frame buffer at the position specified by slot slot_i in the current layout’s slot list.
- **locate**(x, y): Find and return the index of the first target that contains the given point in the current layout’s list of targets, or None if the point does not fall within any target.

The **print driver** maintains no state and responds to only one message:

- **write**(selections): Print out the voter’s selections. selections is a list of lists (one for each group). The sublists contain the integer indices of selected options within each group.

The **event loop** receives four kinds of Pygame events:

- Keypresses (**KEYDOWN**): Upon receiving a keypress event, the event loop notifies the navigator with a **press** message.
- Mouse clicks (**MOUSEBUTTONDOWN**): Upon receiving a touch event, the event loop invokes **locate** on the video driver to translate the touch coordinates into a target index, then passes this target index to the navigator in a **touch** message.
- Audio notifications (**AUDIO_DONE**): Upon receiving notification that a sound clip has finished playing, the event loop invokes **next** on the audio driver.
- Timer notifications (**TIMER_DONE**): Upon receiving notification that the timer has expired, if no sound clip is currently playing, the event loop sends **timeout** to the navigator to indicate that the ballot’s specified timeout has passed with no activity.

The event loop also reschedules a **TIMER_DONE** event for timeout_ms milliseconds in the future every time it receives any event.

The audio driver, video driver, and printer driver are passive components: they only respond to received messages and initiate no messages of their own.

### 6.2 Source Code

The following sections display a complete listing of the source code to Pvote, with three columns of annotations on the left. The **PRECONDITIONS** column contains assumptions and preconditions for each line, function, or method. The **REASONS FOR VALIDITY** column explains why each line will not cause a fatal runtime error, or marks potential causes of a fatal error with the symbol ▲. The **POSTCONDITIONS** column identifies what is expected to be true after a line, function, or method has completed execution. The preconditions and postconditions for each function or method are given on the first line (the **def** line) to facilitate modular reasoning.

Assumptions and postconditions of other lines are cited as evidence. Small numbers in parentheses (123) refer to lines in the current file, and lines in other files are cited with the filename and a colon, as in (Navigator:123).
<table>
<thead>
<tr>
<th>PRECONDITIONS</th>
<th>REASONS FOR VALIDITY</th>
<th>POSTCONDITIONS</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td></td>
<td></td>
</tr>
<tr>
<td>2</td>
<td>pygame.USEREVENT is an int.</td>
<td>AUDIO_DONE is an int.</td>
</tr>
<tr>
<td>3</td>
<td>pygame.USEREVENT is an int.</td>
<td>TIMER_DONE is an int.</td>
</tr>
<tr>
<td>4</td>
<td>A file named ballot exists.</td>
<td>ballot is a Ballot object.</td>
</tr>
<tr>
<td>5</td>
<td></td>
<td>ballot is valid (verifier.1).</td>
</tr>
<tr>
<td>6</td>
<td></td>
<td>audio is an Audio.Audio.</td>
</tr>
<tr>
<td>7</td>
<td></td>
<td></td>
</tr>
<tr>
<td>8</td>
<td></td>
<td></td>
</tr>
<tr>
<td>9</td>
<td></td>
<td></td>
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<tr>
<td>10</td>
<td></td>
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<tr>
<td>11</td>
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<tr>
<td>12</td>
<td></td>
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<tr>
<td>13</td>
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<tr>
<td>14</td>
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<td>15</td>
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<td>16</td>
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<td></td>
<td></td>
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<tr>
<td>23</td>
<td></td>
<td></td>
</tr>
<tr>
<td>24</td>
<td></td>
<td></td>
</tr>
<tr>
<td>25</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>
6.2.1 main.py

```python
import Ballot, verifier, Audio, Video, Printer, Navigator, pygame

AUDIO_DONE = pygame.USEREVENT
TIMER_DONE = pygame.USEREVENT + 1

ballot = Ballot.Ballot(open("ballot"))
verifier.verify(ballot)
audio = Audio.Audio(ballot.audio)
video = Video.Video(ballot.video)
printer = Printer.Printer(ballot.text)
navigator = Navigator.Navigator(ballot.model, audio, video, printer)

while 1:
    pygame.display.update()
    pygame.time.set_timer(TIMER_DONE, ballot.model.timeout_ms)
    event = pygame.event.wait()
    pygame.time.set_timer(TIMER_DONE, 0)
    if event.type == pygame.KEYDOWN:
        navigator.press(event.key)
    if event.type == pygame.MOUSEBUTTONDOWN:
        [x, y] = event.pos
        target_i = video.locate(x, y)
        if target_i != None:
            navigator.touch(target_i)
    if event.type == AUDIO_DONE:
        audio.next()
    if event.type == TIMER_DONE and not audio.playing:
        navigator.timeout()
```

6. Pvote 32
<table>
<thead>
<tr>
<th>PRECONDITIONS</th>
<th>REASONS FOR VALIDITY</th>
<th>POSTCONDITIONS</th>
</tr>
</thead>
<tbody>
<tr>
<td>1. stream is a readable stream.</td>
<td>sha is bound to the SHA module.</td>
<td>sha is bound to the SHA module.</td>
</tr>
<tr>
<td>2. stream is a readable stream.</td>
<td>sha is a string (3). if file header not present.</td>
<td>sha is a readable stream (3). self.sha is a string.</td>
</tr>
<tr>
<td>3. stream is a readable stream.</td>
<td>sha is the SHA module (1) ⇒ sha.sha is a function.</td>
<td>self.stream is a readable stream (3). self.sha is a Ballot.Model.</td>
</tr>
<tr>
<td>4. stream is a readable stream.</td>
<td>self is a readable stream (11).</td>
<td>self.model is a Ballot.Model.</td>
</tr>
<tr>
<td>5. stream is a readable stream.</td>
<td>self is a readable stream (11).</td>
<td>self.text is a Ballot.Text.</td>
</tr>
<tr>
<td>6. stream is a readable stream.</td>
<td>self is a readable stream (11).</td>
<td>self.audio is a Ballot.Audio.</td>
</tr>
<tr>
<td>7. stream is a readable stream.</td>
<td>self.sha is a sha (5). if hash does not match.</td>
<td>self.video is a Ballot.Video.</td>
</tr>
<tr>
<td>8. stream is a readable stream.</td>
<td>length is an int.</td>
<td>The ballot definition file is complete and the types of its fields are valid, or 4.</td>
</tr>
<tr>
<td>9. stream is a readable stream.</td>
<td>self.stream is a stream (5). length is an int (11).</td>
<td>The ballot definition file is complete and the loaded ballot definition data matches its concluding hash.</td>
</tr>
<tr>
<td>10. stream is a readable stream.</td>
<td>self.sha is a sha (5). data is a string (12).</td>
<td>Returns the next length bytes of the stream (12, 14).</td>
</tr>
<tr>
<td>11. stream is a readable stream.</td>
<td>self.stream is a stream (5).</td>
<td>self.stream is a stream (5), so data is a string.</td>
</tr>
<tr>
<td>12. stream is a readable stream.</td>
<td>stream is a stream (16). Group is a class (20).</td>
<td>self.groups is a list of Group (136).</td>
</tr>
<tr>
<td>13. stream is a readable stream.</td>
<td>stream is a stream (16). Page is a class (31).</td>
<td>self.pages is a list of Page (136).</td>
</tr>
<tr>
<td>14. stream is a readable stream.</td>
<td>stream is a stream (16).</td>
<td>allow_none = 0, so self.timeout_ms is an int (122).</td>
</tr>
<tr>
<td>15. stream is a readable stream.</td>
<td>stream is a stream (21).</td>
<td>allow_none = 0, so self.max_sels is an int (122).</td>
</tr>
<tr>
<td>16. stream is a readable stream.</td>
<td>stream is a stream (21).</td>
<td>allow_none = 0, so self.max_chars is an int (122).</td>
</tr>
<tr>
<td>17. stream is a readable stream.</td>
<td>stream is a stream (21).</td>
<td>allow_none = 0, so self.option_clips is an int (122).</td>
</tr>
<tr>
<td>18. stream is a readable stream.</td>
<td>stream is a stream (21). Option is a class (31).</td>
<td>self.options is a list of Option (136).</td>
</tr>
<tr>
<td>19. stream is a readable stream.</td>
<td>stream is a stream (27).</td>
<td>self.sprite_i is an int (122).</td>
</tr>
<tr>
<td>20. stream is a readable stream.</td>
<td>stream is a stream (27).</td>
<td>self.clip_i is an int (122).</td>
</tr>
<tr>
<td>21. stream is a readable stream.</td>
<td>stream is a stream (27).</td>
<td>allow_none = 1, so self.writein_group_i is int or None (122).</td>
</tr>
<tr>
<td>22. stream is a readable stream.</td>
<td>stream is a stream (32). Binding is a class (58).</td>
<td>self.bindings is a list of Binding (136).</td>
</tr>
<tr>
<td>23. stream is a readable stream.</td>
<td>stream is a stream (32). State is a class (38).</td>
<td>self.states is a list of State (136).</td>
</tr>
<tr>
<td>24. stream is a readable stream.</td>
<td>stream is a stream (32). OptionArea is a class (46).</td>
<td>self.option_areas is a list of OptionArea (136).</td>
</tr>
<tr>
<td>25. stream is a readable stream.</td>
<td>stream is a stream (32). CounterArea is a class (50).</td>
<td>self.counter_areas is a list of CounterArea (136).</td>
</tr>
<tr>
<td>26. stream is a readable stream.</td>
<td>stream is a stream (32). ReviewArea is a class (54).</td>
<td>self.review_areas is a list of ReviewArea (136).</td>
</tr>
<tr>
<td>27. stream is a readable stream.</td>
<td>stream is a stream (39).</td>
<td>allow_none = 0, so self.sprite_i is an int (122).</td>
</tr>
<tr>
<td>28. stream is a readable stream.</td>
<td>stream is a stream (39). Segment is a class (78).</td>
<td>self.segments is a list of Segment (136).</td>
</tr>
<tr>
<td>29. stream is a readable stream.</td>
<td>stream is a stream (39). Binding is a class (58).</td>
<td>self.bindings is a list of Binding (136).</td>
</tr>
<tr>
<td>30. stream is a readable stream.</td>
<td>stream is a stream (39). Segment is a class (78).</td>
<td>self.timeout_segments is a list of Segment (136).</td>
</tr>
<tr>
<td>31. stream is a readable stream.</td>
<td>stream is a stream (39).</td>
<td>allow_none = 1, so self.timeout_page_i is int or None (122).</td>
</tr>
<tr>
<td>32. stream is a readable stream.</td>
<td>stream is a stream (39).</td>
<td>allow_none = 0, so self.timeout_state_i is an int (122).</td>
</tr>
</tbody>
</table>
6.2.2 Ballot.py

```python
import sha

class Ballot:
    def __init__(self, stream):
        assert stream.read(8) == "Pvote\x00\x01\x00"
        [self.stream, self.sha] = [stream, sha.sha()]
        self.model = Model(self)
        self.text = Text(self)
        self.audio = Audio(self)
        self.video = Video(self)
        assert self.sha.digest() == stream.read(20)

    def read(self, length):
        data = self.stream.read(length)
        self.sha.update(data)
        return data

class Model:
    def __init__(self, stream):
        self.groups = get_list(stream, Group)
        self.pages = get_list(stream, Page)
        self.timeout_ms = get_int(stream, 0)

class Group:
    def __init__(self, stream):
        self.max_sels = get_int(stream, 0)
        self.max_chars = get_int(stream, 0)
        self.option_clips = get_int(stream, 0)
        self.options = get_list(stream, Option)

class Option:
    def __init__(self, stream):
        self.sprite_i = get_int(stream, 0)
        self.clip_i = get_int(stream, 0)
        self.writein_group_i = get_int(stream, 1)

class Page:
    def __init__(self, stream):
        self.bindings = get_list(stream, Binding)
        self.states = get_list(stream, State)
        self.option_areas = get_list(stream, OptionArea)
        self.counter_areas = get_list(stream, CounterArea)
        self.review_areas = get_list(stream, ReviewArea)

class State:
    def __init__(self, stream):
        self.sprite_i = get_int(stream, 0)
        self.segments = get_list(stream, Segment)
        self.bindings = get_list(stream, Binding)
        self.timeout_segments = get_list(stream, Segment)
        self.timeout_page_i = get_int(stream, 1)
        self.timeout_state_i = get_int(stream, 0)
```
<table>
<thead>
<tr>
<th>PRECONDITIONS</th>
<th>REASONS FOR VALIDITY</th>
<th>POSTCONDITIONS</th>
</tr>
</thead>
<tbody>
<tr>
<td>stream is a readable stream.</td>
<td>stream is a stream (47).</td>
<td>allow_none = 0, so self.group_i is an int (122).</td>
</tr>
<tr>
<td>stream is a readable stream.</td>
<td>stream is a stream (51).</td>
<td>allow_none = 0, so self.group_i is an int (122).</td>
</tr>
<tr>
<td>stream is a readable stream.</td>
<td>stream is a stream (55).</td>
<td>allow_none = 0, so self.option_i is an int (122).</td>
</tr>
<tr>
<td>stream is a readable stream.</td>
<td>stream is a stream (68).</td>
<td>self.predicate is 0, 1, or 2 (127).</td>
</tr>
<tr>
<td>stream is a readable stream.</td>
<td>stream is a stream (74).</td>
<td>self.op is 0, 1, 2, 3, or 4 (127).</td>
</tr>
<tr>
<td>stream is a readable stream.</td>
<td>stream is a stream (79).</td>
<td>self.conditions is a list of Condition (136).</td>
</tr>
<tr>
<td>stream is a readable stream.</td>
<td>Condition is a class (67).</td>
<td>self.type is 0, 1, 2, 3, or 4 (127).</td>
</tr>
</tbody>
</table>
class OptionArea:
    def __init__(self, stream):
        self.group_i = get_int(stream, 0)
        self.option_i = get_int(stream, 0)

class CounterArea:
    def __init__(self, stream):
        self.group_i = get_int(stream, 0)
        self.sprite_i = get_int(stream, 0)

class ReviewArea:
    def __init__(self, stream):
        self.group_i = get_int(stream, 0)
        self.cursor_sprite_i = get_int(stream, 1)

class Binding:
    def __init__(self, stream):
        self.key = get_int(stream, 1)
        self.target_i = get_int(stream, 1)
        self.conditions = get_list(stream, Condition)
        self.steps = get_list(stream, Step)
        self.segments = get_list(stream, Segment)
        self.next_page_i = get_int(stream, 1)
        self.next_state_i = get_int(stream, 0)

class Condition:
    def __init__(self, stream):
        self.predicate = get_enum(stream, 3)
        self.group_i = get_int(stream, 1)
        self.option_i = get_int(stream, 0)
        self.invert = get_enum(stream, 2)

class Step:
    def __init__(self, stream):
        self.op = get_enum(stream, 5)
        self.group_i = get_int(stream, 1)
        self.option_i = get_int(stream, 0)

class Segment:
    def __init__(self, stream):
        self.conditions = get_list(stream, Condition)
        self.type = get_enum(stream, 5)
        self.clip_i = get_int(stream, 0)
        self.group_i = get_int(stream, 1)
        self.option_i = get_int(stream, 0)
<table>
<thead>
<tr>
<th>PRECONDITIONS</th>
<th>REASONS FOR VALIDITY</th>
<th>POSTCONDITIONS</th>
</tr>
</thead>
<tbody>
<tr>
<td>stream is a readable stream.</td>
<td>stream is a stream (87). TextGroup is a class (88).</td>
<td>self.groups is a list of TextGroup (136).</td>
</tr>
<tr>
<td>stream is a readable stream.</td>
<td>stream is a stream (89).</td>
<td>self.name is a string (131).</td>
</tr>
<tr>
<td>stream is a readable stream.</td>
<td>stream is a stream (94). Clip is a class (97).</td>
<td>allow_none = 0, so self.clips is a list of Clip (136).</td>
</tr>
<tr>
<td>stream is a readable stream.</td>
<td>stream is a stream (98). allow_none = 0, so get_int returns an int (122).</td>
<td>stream is a stream (98), so self.samples is a string.</td>
</tr>
<tr>
<td>stream is a readable stream.</td>
<td>stream is a stream (101).</td>
<td>allow_none = 0, so self.width is an int (122).</td>
</tr>
<tr>
<td>stream is a readable stream.</td>
<td>stream is a stream (101), Layout is a class (106).</td>
<td>allow_none = 0, so self.height is an int (122).</td>
</tr>
<tr>
<td>stream is a readable stream.</td>
<td>stream is a stream (101), Image is a class (111).</td>
<td>self.layouts is a list of Layout (136).</td>
</tr>
<tr>
<td>stream is a readable stream.</td>
<td>Image is a class (111). stream is a stream (107).</td>
<td>self.sprites is a list of Image (136).</td>
</tr>
<tr>
<td>stream is a readable stream.</td>
<td>stream is a stream (107), Rect is a class (116).</td>
<td>self.targets is a list of Rect (136).</td>
</tr>
<tr>
<td>stream is a readable stream.</td>
<td>stream is a stream (107), Rect is a class (116).</td>
<td>self.slots is a list of Rect (136).</td>
</tr>
<tr>
<td>stream is a readable stream.</td>
<td>stream is a stream (112).</td>
<td>allow_none = 0, so self.width is an int (122).</td>
</tr>
<tr>
<td>stream is a readable stream.</td>
<td>stream is a stream (112).</td>
<td>allow_none = 0, so self.height is an int (122).</td>
</tr>
<tr>
<td>stream is a stream (112), self.width is an int (113).</td>
<td>stream is a stream (112), self.height is an int (114).</td>
<td>stream is a stream (112), so self.pixels is a string.</td>
</tr>
<tr>
<td>stream is a readable stream.</td>
<td>stream is a stream (117).</td>
<td>allow_none = 0, so self.left is an int (122).</td>
</tr>
<tr>
<td>stream is a readable stream.</td>
<td>stream is a stream (117).</td>
<td>allow_none = 0, so self.top is an int (122).</td>
</tr>
<tr>
<td>stream is a readable stream.</td>
<td>stream is a stream (117).</td>
<td>allow_none = 0, so self.width is an int (122).</td>
</tr>
<tr>
<td>stream is a readable stream.</td>
<td>stream is a stream (117).</td>
<td>allow_none = 0, so self.height is an int (122).</td>
</tr>
</tbody>
</table>
class Text:
    def __init__(self, stream):
        self.groups = get_list(stream, TextGroup)

class TextGroup:
    def __init__(self, stream):
        self.name = get_str(stream)
        self.writein = get_enum(stream, 2)
        self.options = get_list(stream, get_str)

class Audio:
    def __init__(self, stream):
        self.sample_rate = get_int(stream, 0)
        self.clips = get_list(stream, Clip)

class Clip:
    def __init__(self, stream):
        self.samples = stream.read(get_int(stream, 0)*2)

class Video:
    def __init__(self, stream):
        self.width = get_int(stream, 0)
        self.height = get_int(stream, 0)
        self.layouts = get_list(stream, Layout)
        self.sprites = get_list(stream, Image)

class Layout:
    def __init__(self, stream):
        self.screen = Image(stream)
        self.targets = get_list(stream, Rect)
        self.slots = get_list(stream, Rect)

class Image:
    def __init__(self, stream):
        self.width = get_int(stream, 0)
        self.height = get_int(stream, 0)
        self.pixels = stream.read(self.width*self.height*3)

class Rect:
    def __init__(self, stream):
        self.left = get_int(stream, 0)
        self.top = get_int(stream, 0)
        self.width = get_int(stream, 0)
        self.height = get_int(stream, 0)
<table>
<thead>
<tr>
<th>PRECONDITIONS</th>
<th>REASONS FOR VALIDITY</th>
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</tr>
</thead>
<tbody>
<tr>
<td>122 stream is a stream.</td>
<td>allow_none is 0 or 1.</td>
<td>Returns an int if allow_none = 0 (125, 126); otherwise returns an int or None (126). ▲ if the next 4 bytes read do not represent an int or None, or if they represent None but allow_none = 0.</td>
</tr>
<tr>
<td>123</td>
<td>stream is a stream (122). ▲ if read returns less than 4 bytes. list returns a list of 4 length-1 strings.</td>
<td>▲ if the next 4 bytes read do not represent an int or None (126).</td>
</tr>
<tr>
<td>124</td>
<td>▲ if str returns less than 4 bytes. list returns a list of 4 length-1 strings.</td>
<td>▲ if the next 4 bytes read do not represent an int or None (126).</td>
</tr>
<tr>
<td>125</td>
<td>a, b, c, d are 1-byte strings.</td>
<td>None can be returned only if allow_none ≠ 0.</td>
</tr>
<tr>
<td>126</td>
<td>allow_none is an int (122). a, b, c, d are strings (126).</td>
<td>None can be returned only if allow_none ≠ 0.</td>
</tr>
<tr>
<td>127</td>
<td>stream is a stream.</td>
<td>Returns an int where 0 ≤ n &lt; cardinality (129, 130). ▲ if the next 4 bytes read do not represent an int in this range.</td>
</tr>
<tr>
<td>128</td>
<td>cardinality is an int.</td>
<td>allow_none = 0, so value is an int (122).</td>
</tr>
<tr>
<td>129</td>
<td>▲ if value is out of range.</td>
<td>None can be returned only if allow_none ≠ 0.</td>
</tr>
<tr>
<td>130</td>
<td>▲ if value is out of range.</td>
<td>None can be returned only if allow_none ≠ 0.</td>
</tr>
<tr>
<td>131</td>
<td>stream is a stream.</td>
<td>Returns a string containing only bytes between 32 and 125 inclusive (133–135). ▲ if the stream does not yield a valid string.</td>
</tr>
<tr>
<td>132</td>
<td>▲ if any byte in str falls outside the range from 32 to 125 inclusive.</td>
<td>▲ if any byte in str falls outside the range from 32 to 125 inclusive.</td>
</tr>
<tr>
<td>133</td>
<td>get_int returns an int (122).</td>
<td>▲ if any byte in str falls outside the range from 32 to 125 inclusive.</td>
</tr>
<tr>
<td>134</td>
<td>str is a string.</td>
<td>▲ if any byte in str falls outside the range from 32 to 125 inclusive.</td>
</tr>
<tr>
<td>135</td>
<td>ch is a 1-byte string.</td>
<td>▲ if any byte in str falls outside the range from 32 to 125 inclusive.</td>
</tr>
<tr>
<td>136</td>
<td>stream is a stream.</td>
<td>A string is returned.</td>
</tr>
<tr>
<td>137</td>
<td>stream is a stream (136), allow_none = 0 ⇒ get_int returns an int (122).</td>
<td>Returns a list of instances of Class (124).</td>
</tr>
</tbody>
</table>
def get_int(stream, allow_none):
    [a, b, c, d] = list(stream.read(4))

    if ord(a) < 128:
        return ord(a)*16777216 + ord(b)*65536 + ord(c)*256 + ord(d)
    assert allow_none and a + b + c + d == '\xff\xff\xff\xff'

    def get_enum(stream, cardinality):
        value = get_int(stream, 0)
        assert value < cardinality
        return value

    def get_str(stream):
        str = stream.read(get_int(stream, 0))
        for ch in list(str):
            assert 32 <= ord(ch) <= 125
        return str

    def get_list(stream, Class):
        return [Class(stream) for i in range(get_int(stream, 0))]

<table>
<thead>
<tr>
<th>PRECONDITIONS</th>
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<th>POSTCONDITIONS</th>
</tr>
</thead>
<tbody>
<tr>
<td>1  ballot is a Ballot.</td>
<td>ballot.satisfies the validity constraints in Section 2.7, or ▲.</td>
<td></td>
</tr>
<tr>
<td>2  ballot.model is a Model (1, Ballot:6). ballot.video is a Video (1, Ballot:9).</td>
<td>groups is a list of Group (Ballot:17). sprites is a list of Image (Ballot:105). option_sizes is a list of length(groups) empty lists. char_sizes is a list of length(groups) empty lists.</td>
<td></td>
</tr>
<tr>
<td>3</td>
<td>model.groups is a list (1, Ballot:6, Ballot:17). text.groups is a list (1, Ballot:7, Ballot:87). ▲ if assertion fails.</td>
<td>model.groups and text.groups have the same length &gt; 0.</td>
</tr>
<tr>
<td>4</td>
<td>model.pages is a list (1, Ballot:6, Ballot:18). video.layouts is a list (1, Ballot:9, Ballot:104). ▲ if assertion fails.</td>
<td>model.pages and video.layouts have the same length &gt; 0.</td>
</tr>
<tr>
<td>5</td>
<td>model.pages is a list (1, Ballot:6, Ballot:18). page_i is a valid index in model.pages (7) ⇒ page_i is a valid index in video.layouts (6).</td>
<td>page_i is a valid page index. page is the associated Page (Ballot:18). layout is a Layout (Ballot:104).</td>
</tr>
<tr>
<td>6</td>
<td>page.bindings is a list (7, Ballot:33).</td>
<td>binding is a Binding (Ballot:33).</td>
</tr>
<tr>
<td>7</td>
<td>ballot is a Ballot (8). page is a Page (7). binding is a Binding (9).</td>
<td>binding is a valid Binding for this page (71).</td>
</tr>
<tr>
<td>8</td>
<td>page.states is a list (7, Ballot:34). ▲ if assertion fails.</td>
<td>page.states is nonempty.</td>
</tr>
<tr>
<td>9</td>
<td>page.states is a list (Ballot:34). ▲ if state.sprite_i is out of bounds. ▲ if state_i is out of bounds. sprites is a list of Image (2). layout.slots is a list of Rect (8, Ballot:110).</td>
<td></td>
</tr>
<tr>
<td>10</td>
<td></td>
<td>state_i is a valid state index. state is the associated State (Ballot:34). state.sprite_i is a valid index in video.sprites (2). state_i is a valid index in layout.slots. The state's sprite at state.sprite_i has the same size as the state's slot (95).</td>
</tr>
<tr>
<td>11</td>
<td></td>
<td>Every element of state.segments is a valid Segment (78).</td>
</tr>
<tr>
<td>12</td>
<td></td>
<td>binding is a Binding (Ballot:42).</td>
</tr>
<tr>
<td>13</td>
<td></td>
<td>binding is a valid Binding for this page (68).</td>
</tr>
<tr>
<td>14</td>
<td></td>
<td>Every element of state.timeout_segments is a valid Segment (78).</td>
</tr>
<tr>
<td>15</td>
<td></td>
<td>Either timeout_page_i is None, or timeout_page_i and timeout_state_i are a valid page and state index (75).</td>
</tr>
<tr>
<td>16</td>
<td></td>
<td>slot_i is the index of the first remaining slot after slots have been assigned to states.</td>
</tr>
<tr>
<td>17</td>
<td></td>
<td>area is an OptionArea (7, Ballot:35).</td>
</tr>
<tr>
<td>18</td>
<td></td>
<td>area.group_i is an int (Ballot:48). area.group_i is a valid group index and area.option_i is a valid option index in that group (89). This page's layout contains a slot for this option area. option_sizes for this option area's group contains this option area's slot. slot_i is the index of the next available slot.</td>
</tr>
<tr>
<td>19</td>
<td></td>
<td></td>
</tr>
<tr>
<td>20</td>
<td></td>
<td>area is a CounterArea (7, Ballot:36).</td>
</tr>
<tr>
<td>21</td>
<td></td>
<td>area.group_i is a valid group index. i is an int from 0 to max_sels inclusive.</td>
</tr>
<tr>
<td>22</td>
<td></td>
<td>This page's layout contains a slot for this counter area. sprite_i through sprite_i + max_sels are valid sprite indices. These sprites all fit the counter area's slot (99). slot_i is the index of the next available slot.</td>
</tr>
</tbody>
</table>
6.2.3 verifier.py

```python
def verify(ballot):
    
    [groups, sprites] = [ballot.model.groups, ballot.video.sprites]
    option_sizes = [[] for group in groups]
    char_sizes = [[] for group in groups]

    assert len(ballot.model.groups) == len(ballot.text.groups) > 0
    assert len(ballot.model.pages) == len(ballot.video.layouts) > 0

    for [page_i, page] in enumerate(ballot.model.pages):
        layout = ballot.video.layouts[page_i]

        for binding in page.bindings:
            verify_binding(ballot, page, binding)

        assert len(page.states) > 0

        for [state_i, state] in enumerate(page.states):
            verify_size(sprites[state.sprite_i], layout.slots[state_i])

            verify_segments(ballot, page, state.segments)

            for binding in state.bindings:
                verify_binding(ballot, page, binding)

            verify_segments(ballot, page, state.timeout_segments)

            verify_goto(ballot, state.timeout_page_i, state.timeout_state_i)

            slot_i = len(page.states)

        for area in page.option_areas:
            verify_option_ref(ballot, page, area)

            option_sizes[area.group_i].append(layout.slots[slot_i])

            slot_i = slot_i + 1

        for area in page.counter_areas:
            for i in range(groups[area.group_i].max_sels + 1):
                verify_size(sprites[area.sprite_i + i], layout.slots[slot_i])

                slot_i = slot_i + 1
```

<table>
<thead>
<tr>
<th>PRECONDITIONS</th>
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<th>POSTCONDITIONS</th>
</tr>
</thead>
<tbody>
<tr>
<td>page.review_areas is a list (7, Ballot:37).</td>
<td>option_sizes for this review area’s group contains all of the review area’s option sizes.</td>
<td>area is a ReviewArea (7, Ballot:37).</td>
</tr>
<tr>
<td>▲ if area.group_i is out of bounds. groups is a list of Group (2) ⇒ groups[area.group_i].max_sels is an int (Ballot:22).</td>
<td>slot_i is the index of the next available slot.</td>
<td>area.group_i is a valid group index. i is an int from 0 to max_sels – 1 inclusive.</td>
</tr>
<tr>
<td>option_sizes is a list of lists (3). area.group_i is a valid group index (29). ▲ if slot_i is out of bounds.</td>
<td>group_i is a valid group index. group is the associated Group (2).</td>
<td>optionprites remains valid sprite indices. optionprites for this review area’s group contains the review area’s cursor sprite.</td>
</tr>
<tr>
<td>slot_i is an int (19, 23, 27, 31).</td>
<td>group_i is a valid group index. group is the associated Group (2).</td>
<td>optionprites remains valid sprite indices. optionprites for this review area’s group contains the review area’s cursor sprite.</td>
</tr>
<tr>
<td>area.group_i is a valid group index (29). groups is a list of Group (2) ⇒ groups[area.group_i].max_chars is an int (Ballot:23).</td>
<td>optionprites remains valid sprite indices. optionprites for this review area’s group contains the review area’s cursor sprite.</td>
<td>optionprites remains valid sprite indices. optionprites for this review area’s group contains the review area’s cursor sprite.</td>
</tr>
<tr>
<td>option_sizes is a list of lists (3). area.group_i is a valid group index (29). ▲ if area.cursor_sprite_i is out of bounds.</td>
<td>group_i is a valid group index. group is the associated Group (2).</td>
<td>optionprites remains valid sprite indices. optionprites for this review area’s group contains the review area’s cursor sprite.</td>
</tr>
<tr>
<td>slot_i is an int (19, 23, 27, 31).</td>
<td>optionprites remains valid sprite indices. optionprites for this review area’s group contains the review area’s cursor sprite.</td>
<td>optionprites remains valid sprite indices. optionprites for this review area’s group contains the review area’s cursor sprite.</td>
</tr>
<tr>
<td>area.group_i is a valid group index (29). groups is a list of Group (2) ⇒ groups[area.group_i].max_chars is an int (Ballot:23).</td>
<td>optionprites remains valid sprite indices. optionprites for this review area’s group contains the review area’s cursor sprite.</td>
<td>optionprites remains valid sprite indices. optionprites for this review area’s group contains the review area’s cursor sprite.</td>
</tr>
<tr>
<td>option_sizes is a list of lists (3). area.group_i is a valid group index (29). ▲ if area.cursor_sprite_i is out of bounds.</td>
<td>group_i is a valid group index. group is the associated Group (2).</td>
<td>optionprites remains valid sprite indices. optionprites for this review area’s group contains the review area’s cursor sprite.</td>
</tr>
<tr>
<td>char_sizes is a list of lists (4). area.group_i is a valid group index (29). ▲ if slot_i is out of bounds.</td>
<td>optionprites remains valid sprite indices. optionprites for this review area’s group contains the review area’s cursor sprite.</td>
<td>optionprites remains valid sprite indices. optionprites for this review area’s group contains the review area’s cursor sprite.</td>
</tr>
<tr>
<td>slot_i is an int (19, 23, 27, 31).</td>
<td>optionprites remains valid sprite indices. optionprites for this review area’s group contains the review area’s cursor sprite.</td>
<td>optionprites remains valid sprite indices. optionprites for this review area’s group contains the review area’s cursor sprite.</td>
</tr>
<tr>
<td>area cursor sprite_i is an int or None (Ballot:57).</td>
<td>optionprites remains valid sprite indices. optionprites for this review area’s group contains the review area’s cursor sprite.</td>
<td>optionprites remains valid sprite indices. optionprites for this review area’s group contains the review area’s cursor sprite.</td>
</tr>
<tr>
<td>option_sizes is a list of lists (3). area.group_i is a valid group index (29). ▲ if area.cursor_sprite_i is out of bounds.</td>
<td>group_i is a valid group index. group is the associated Group (2).</td>
<td>optionprites remains valid sprite indices. optionprites for this review area’s group contains the review area’s cursor sprite.</td>
</tr>
<tr>
<td>groups is a list (2).</td>
<td>optionprites remains valid sprite indices. optionprites for this review area’s group contains the review area’s cursor sprite.</td>
<td>optionprites remains valid sprite indices. optionprites for this review area’s group contains the review area’s cursor sprite.</td>
</tr>
<tr>
<td>group.options is a list (37, Ballot:25).</td>
<td>optionprites remains valid sprite indices. optionprites for this review area’s group contains the review area’s cursor sprite.</td>
<td>optionprites remains valid sprite indices. optionprites for this review area’s group contains the review area’s cursor sprite.</td>
</tr>
<tr>
<td>option_sizes is a list of lists (3). area.group_i is a valid group index (37). ▲ if option.sprite_i is out of bounds.</td>
<td>optionprites remains valid sprite indices. optionprites for this review area’s group contains the review area’s cursor sprite.</td>
<td>optionprites remains valid sprite indices. optionprites for this review area’s group contains the review area’s cursor sprite.</td>
</tr>
<tr>
<td>option_sizes is a list of lists (3). area.group_i is a valid group index (37). ▲ if option.sprite_i + 1 is out of bounds.</td>
<td>optionprites remains valid sprite indices. optionprites for this review area’s group contains the review area’s cursor sprite.</td>
<td>optionprites remains valid sprite indices. optionprites for this review area’s group contains the review area’s cursor sprite.</td>
</tr>
<tr>
<td>group is a Group (37). ▲ if assertion fails.</td>
<td>optionprites remains valid sprite indices. optionprites for this review area’s group contains the review area’s cursor sprite.</td>
<td>optionprites remains valid sprite indices. optionprites for this review area’s group contains the review area’s cursor sprite.</td>
</tr>
<tr>
<td>audio.clips is a list (1, Ballot:8, Ballot:96). ▲ if option.clip_i + group.option.clips – i is out of bounds.</td>
<td>The integers option.clip_i through option.clip_i + group.option.clips – i are all valid clip indices.</td>
<td>optionprites remains valid sprite indices. optionprites for this review area’s group contains the review area’s cursor sprite.</td>
</tr>
<tr>
<td>option is a Option (38).</td>
<td>optionprites remains valid sprite indices. optionprites for this review area’s group contains the review area’s cursor sprite.</td>
<td>optionprites remains valid sprite indices. optionprites for this review area’s group contains the review area’s cursor sprite.</td>
</tr>
<tr>
<td>groups is a list of Group (2). option is a Option (38). ▲ if option.writein_group_i is out of bounds.</td>
<td>max_chars = 0 for this option’s write-in group.</td>
<td>max_chars for this option’s write-in group matches max_chars for this option’s parent group. group cannot be the write-in group for any option (43–46).</td>
</tr>
<tr>
<td>writein_groups is a Group (44). ▲ if assertion fails.</td>
<td>max_chars for this option’s write-in group matches max_chars for this option’s parent group. group cannot be the write-in group for any option (43–46).</td>
<td>max_chars for this option’s write-in group matches max_chars for this option’s parent group. group cannot be the write-in group for any option (43–46).</td>
</tr>
<tr>
<td>writein_groups is a Group (44). ▲ if assertion fails.</td>
<td>object is a Slot or a Sprite (22, 30, 36, 39, 40).</td>
<td>object is a Slot or a Sprite (22, 30, 36, 39, 40).</td>
</tr>
<tr>
<td>writein_groups is a list (44, Ballot:25).</td>
<td>After loop: all options in the write-in group have valid sprite indices.</td>
<td>After loop: all options in the write-in group have valid sprite indices.</td>
</tr>
<tr>
<td>char_sizes is a list of lists (4). group_i is a valid group index (37). ▲ if option.sprite_i is out of bounds.</td>
<td>object is a Slot or a Sprite (22, 30, 36, 39, 40).</td>
<td>object is a Slot or a Sprite (22, 30, 36, 39, 40).</td>
</tr>
<tr>
<td>group_i is a valid group index (37).</td>
<td>After loop: all slots and sprites for options in this group have the same size.</td>
<td>After loop: all slots and sprites for options in this group have the same size.</td>
</tr>
<tr>
<td>option_sizes[group_i] is a list (3).</td>
<td>After loop: all slots and sprites for options in this group have the same size.</td>
<td>After loop: all slots and sprites for options in this group have the same size.</td>
</tr>
</tbody>
</table>
for area in page.review_areas:
    for i in range(groups[area.group_i].max_sels):
        option_sizes[area.group_i].append(layout.slots[slot_i])

        slot_i = slot_i + 1
    for j in range(groups[area.group_i].max_chars):
        char_sizes[area.group_i].append(layout.slots[slot_i])

        slot_i = slot_i + 1
        if area.cursor_sprite_i != None:
            option_sizes[area.group_i].append(sprites[area.cursor_sprite_i])

for [group_i, group] in enumerate(groups):
    for option in group.options:
        option_sizes[group_i].append(sprites[option.sprite_i])
        option_sizes[group_i].append(sprites[option.sprite_i + 1])

        assert group.option_clips > 0
        ballot.audio.clips[option.clip_i + group.option_clips - 1]

        if option.writein_group_i != None:
            writein_group = groups[option.writein_group_i]

            assert writein_group.max_chars == 0
            assert writein_group.max_sels == group.max_chars > 0

            for option in writein_group.options:
                char_sizes[group_i].append(sprites[option.sprite_i])

                for object in option_sizes[group_i]:
                    verify_size(object, option_sizes[group_i][0])

                for object in char_sizes[group_i]:
                    verify_size(object, char_sizes[group_i][0])
<table>
<thead>
<tr>
<th>PRECONDITIONS</th>
<th>REASONS FOR VALIDITY</th>
<th>POSTCONDITIONS</th>
</tr>
</thead>
<tbody>
<tr>
<td>text.groups is a list of size 1 (Ballot:77, Ballot:87).</td>
<td>text.groups is a list of size 1 (Ballot:77, Ballot:87).</td>
<td>Since text.groups and model.groups have the same length (5), group_i is a valid group index and group is the associated TextGroup (1, Ballot:77, Ballot:87). group.name is no more than 50 bytes long. This TextGroup group has the same number of options as its corresponding Group in model.groups. option is a string (53, Ballot:92). option is no more than 50 bytes long. clip is a Clip (1, Ballot:8, Ballot:96), clip has a nonempty string of samples. video has nonzero width and nonzero height. layout has a Layout (1, Ballot:9, Ballot:104). layout.screen has the same size as video. The sum of lists is a list of Rect, so rect is a Rect. rect does not extend beyond the right edge of the screen. rect does not extend beyond the bottom edge of the screen. sprite is an Image (1, Ballot:8, Ballot:105). sprite has a nonzero width and height and the correct amount of pixel data for an image with size width × height. binding is a valid Binding, or △. condition is a Condition (68, Ballot:62). After loop: every element of binding.conditions is a valid Condition. step is a Step (68, Ballot:63). step.group_i and step.option_i form a valid option reference. All the segments in binding.segments are valid for this page (78). Either next_page_i is None, or next_page_i is a valid page index and next_state_i is a valid state index for that page (75). Either page_i is None (76), or page_i is a valid page index and state_i is a valid state index for that page (77), or △. page_i is a valid page index and state_i is a valid state index for that page. Every segment in segments is a valid Segment. segment is a Segment (78). condition is a Condition (79, Ballot:80). After loop: every element of segment.conditions is a valid Condition. segment.clip_i is a valid clip index. The segment’s group_i and option_i form a valid option reference. group is the referenced Group. If type is 1 or 2, segment.clip_i is a valid option clip offset for the referenced group (83, 85). If type is 3 or 4, segment.clip_i + max_sels is a valid clip index for the referenced group (83, 87).</td>
</tr>
</tbody>
</table>
for [group_i, group] in enumerate(ballot.text.groups):
    assert len(group.name) <= 50
    assert len(group.options) == len(groups[group_i].options)

    for option in group.options:
        assert len(option) <= 50

    for clip in ballot.audio.clips:
        assert len(clip.samples) > 0

assert ballot.video.width*ballot.video.height > 0

for layout in ballot.video.layouts:
    verify_size(layout.screen, ballot.video)

    for rect in layout.targets + layout.slots:
        assert rect.left + rect.width <= ballot.video.width
        assert rect.top + rect.height <= ballot.video.height

    for sprite in ballot.video.sprites:
        assert len(sprite.pixels) == sprite.width*sprite.height*3 > 0

def verify_binding(ballot, page, binding):
    for condition in binding.conditions:
        verify_option_ref(ballot, page, condition)

    for step in binding.steps:
        verify_option_ref(ballot, page, step)

    verify_segments(ballot, page, binding.segments)

    verify_goto(ballot, binding.next_page_i, binding.next_state_i)

def verify_goto(ballot, page_i, state_i):
    if page_i != None:
        ballot.model.pages[page_i].states[state_i]

def verify_segments(ballot, page, segments):
    for segment in segments:
        for condition in segment.conditions:
            verify_option_ref(ballot, page, condition)

        if segment.type in [1, 2, 3, 4]:
            group = verify_option_ref(ballot, page, segment)

            if segment.type in [1, 2]:
                assert segment.clip_i < group.option_clips

            if segment.type in [3, 4]:
                ballot.audio.clips[segment.clip_i + group.max_sels]
<table>
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</tr>
</thead>
<tbody>
<tr>
<td>ballot is a Ballot, page is a Page, object is an OptionArea, Condition, Step, or Segment.</td>
<td>page.option_areas is a list of OptionArea (7, Ballot:35), <img src="null" alt="if object.option_i is out of bounds." /></td>
<td>object.group_i and object.option_i form a valid direct or indirect option reference, or <img src="null" alt="if object.group_i is out of bounds." />. Returns the referenced Group (92, 94).</td>
</tr>
<tr>
<td><img src="null" alt="if object.option_i is out of bounds." /></td>
<td>model.groups is a list (1, Ballot:6, Ballot:17), area is an OptionArea (91), <img src="null" alt="if group_i is out of bounds." /></td>
<td>If group_i is None, then option_i is a valid option area index for page, area is the associated OptionArea.</td>
</tr>
<tr>
<td>model.groups is a list (1, Ballot:6, Ballot:17), <img src="null" alt="if object.group_i is out of bounds." /></td>
<td>object.group_i is out of bounds. groups[object.group_i].options is a list (25), <img src="null" alt="if object.option_i is out of bounds." /></td>
<td>The referenced option area’s group is returned. group_i is a valid group index and option_i is a valid option index in that group.</td>
</tr>
<tr>
<td>model.groups is a list (1, Ballot:6, Ballot:17), <img src="null" alt="if object.group_i is out of bounds." /></td>
<td>model.groups is a list (1, Ballot:6, Ballot:17), group_i is a valid group index (93).</td>
<td>The referenced group is returned.</td>
</tr>
<tr>
<td>a is a Video, Image, or Rect, b is a Video, Image, or Rect.</td>
<td>a.width and b.width are ints (95, Ballot:102, Ballot:113, Ballot:120), a.height and b.height are ints (95, Ballot:103, Ballot:114, Ballot:121).</td>
<td>a and b have equal width and equal height.</td>
</tr>
</tbody>
</table>
def verify_option_ref(ballot, page, object):
    if object.group_i == None:
        area = page.option_areas[object.option_i]
        return ballot.model.groups[area.group_i]
    return ballot.model.groups[object.group_i].options[object.option_i]

def verify_size(a, b):
    assert a.width == b.width and a.height == b.height
INVARIANTS

INV1. OP_ADD = 0, OP_REMOVE = 1, OP_APPEND = 2, OP_POP = 3, OP_CLEAR = 4 (1).
INV2. SG_CLIP = 0, SG_OPTION = 1, SG_LIST_SELS = 2, SG_COUNT_SELS = 3, SG_MAX_SELS = 4 (2).
INV3. PR_GROUP_EMPTY = 0, PR_GROUP_FULL = 1, PR_OPTION_SELECTED = 2 (3).

In an initialized Navigator object:
INV4. self.model is a valid Model (6).
INV5. self.audio is an Audio.Audio (7).
INV6. self.video is a Video.Video (7).
INV7. self.printer is a Printer (7).

INV8. self.selections is a list of length(model.groups) lists (8).
INV9. self.selections[i] always contains at most model.groups[i].max_sels elements (8, 82, 83).
INV10. The elements of self.selections[i] are always valid indexes into model.groups[i].options (8).
INV11. self.page_i is a valid page index and self.page is the Page at self.model.pages[self.page_i] (16).
INV12. self.state_i is a valid state index in the page self.page and self.state is the State at self.page.states[self.state_i] (17).

PRECONDITIONS | REASONS FOR VALIDITY | POSTCONDITIONS
---|---|---
1 | | INV1.
2 | | INV2.
3 | | INV3.
4 | model is a valid Model. audio is a Audio.Audio. video is a Video.Video. printer is a Printer.Printer. | INV4.
5 | | INV5, INV6, INV7.
6 | model.groups is a list (INV4, Ballot:17). | INV8. self.selections is a list of length(model.groups) empty lists.
7 | | |
8 | 0 is a valid page index (verifier:6) and 0 is a valid state index in the page (verifier:11). | If page_i ≠ None, then self.page_i and self.state_i are set to page_i and state_i.
9 | | |
10 | Either page_i is None, or page_i is a valid page index and state_i is a valid state index in that page. | self.model.pages is a list (INV4, Ballot:18).
11 | | self.state_i and state_i are a valid page index and state index (12).
12 | | |
13 | | |
14 | INV7, INV8, INV9, INV10. | self.model.pages is a list (INV4, Ballot:18), page_i is a valid index into self.model.pages (13).
15 | | self.page.states is a list (INV4, Ballot:18), state_i is a valid index into self.page.states (13).
16 | | self.state.segments is a list of valid Segments (16, verifier:14).
17 | | |
18 | | |
19 | INV11 and model.pages and video.layouts have equal length (verifier:6) ⇒ self.page_i is a valid layout index. | The video display shows the current page and state. The option areas, counter areas, and review areas on the display accurately reflect the current selections.
20 | | slot_i points to the next available slot after the states’ slots.
21 | | |
22 | self.page.option_areas is a list (INV11, Ballot:35). area is an OptionArea (23). INV8. area.group_i is a valid group index (verifier:21). | The unselected or selected sprite for this option is correctly displayed in this option area.
23 | | area is an OptionArea (INV11, Ballot:35), unselected is 0 if this option area’s option is selected, else it is 1.
24 | | |
25 | area.group_i is a valid group index (verifier:21). | |
26 | area.group_i and area.option_i are a valid option reference (verifier:21). | |
27 | unselected is 0 or 1 (24), slot_i is this option area’s slot index (22, 23, 28). sprite_i and sprite_i + 1 are valid sprite indices (verifier:39–40). The option area’s slot (verifier:22) and the sprite to be pasted (verifier:39–40) have the same size (verifier:50). | |
6.2.4 Navigator.py

class Navigator:
    def __init__(self, model, audio, video, printer):
        self.model = model
        [self.audio, self.video, self.printer] = [audio, video, printer]
        self.selections = [[] for group in model.groups]
        self.page_i = None
        self.goto(0, 0)

    def goto(self, page_i, state_i):
        if page_i != None and self.page_i != len(self.model.pages) - 1:
            if page_i == len(self.model.pages) - 1:
                self.printer.write(self.selections)
            [self.page_i, self.page] = [page_i, self.model.pages[page_i]]
            [self.state_i, self.state] = [state_i, self.page.states[state_i]]
            self.play(self.state.segments)
            self.update()

    def update(self):
        self.video.goto(self.page_i)
        self.video.paste(self.state.sprite_i, self.state_i)
        slot_i = len(self.page.states)
        for area in self.page.option_areas:
            unselected = area.option_i not in self.selections[area.group_i]
            group = self.model.groups[area.group_i]
            option = group.options[area.option_i]
            self.video.paste(option.sprite_i + unselected, slot_i)
            slot_i = slot_i + 1
PRECONDITIONS

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REASONS FOR VALIDITY

self.page.counter_areas is a list (INV11, Ballot:36).

area is a CounterArea (29). INV8. area.group_i is a valid group index (verifier:23).

count is an int from 0 to max_sels. slot_i is this counter area’s slot index (22, 23, 29, 32). sprite_i + count is a valid sprite index (verifier:26). The pasted sprite matches the size of the counter area’s slot (verifier:26).

self.page.review_areas is a list (INV11, Ballot:37).

area.group_i is a valid group index (verifier:29). slot_i is this review area’s first slot index (22, 23, 28, 29, 32, 33). slot_i + k × (1 + max_chars) is the valid index of a slot with size matching the group’s options’ sprites (verifier:30–34, verifier:39, verifier:49–50). area.cursor_sprite_i is a valid sprite index or None (verifier:36).

group_i is a valid group index. ∀ k ∈ {0, 1, ..., max_sels − 1}, slot_i + k × (1 + max_chars) is the valid index of a slot with size matching the group’s options’ sprites. cursor_sprite_i is None or a valid sprite index.

group_i is a valid group index (35).
group_i is a valid group index (35).
group.max_sels is an int (35, Ballot:22).
i is an int (38). selections is a list (37).
i is a valid index into selections (39). selections[i] is a valid index into group.options (36, 37, INV10).

option.sprite_i is a valid sprite index (verifier:39). slot_i is a valid slot index referring to a slot of matching size (35, 40).

writein.group_i is a valid group index (verifier:44, 42). That group has max_chars = 0 (verifier:44, verifier:45) and max_sels = group.max_chars (verifier:46). ∀ k ∈ {0, 1, ..., group.max_chars − 1}, slot_i + 1 + k is the valid index of a slot with size matching the write-in group’s options’ sprites (verifier:31–34, verifier:47–48, verifier:51–52).

cursor.sprite_i is a valid sprite index (35, 44). The cursor sprite has the same size as slot slot_i (verifier:30, verifier:36, verifier:50).

slot_i is the first slot for the next option in this review area. slot_i + max_sels × (1 + max_chars) is returned (38, 46).

The operative binding, if any, for this keypress is invoked. Returns None.

state.bindings is a list (INV12, Ballot:42). page.bindings is a list (INV11, Ballot:33). binding.key is an int (48, Ballot:60). binding.conditions is a list of valid Conditions (49, Ballot:62, verifier:70).

If binding is operative, it is invoked. Returns None (69).

The operative binding, if any, for this target is invoked. Returns None.

Since the lists contain only valid Bindings (verifier:10, verifier:16), binding is a valid Binding.

If binding is operative, it is invoked. Returns None (69).

POSTCONDITIONS

area is a CounterArea (INV11, Ballot:36).

By INV9, 0 ≤ count ≤ groups[area.group_i].max_sels.

The counter area displays the correct sprite according to the number of selections in its group.

area is a ReviewArea (INV11, Ballot:37).

The review area is properly populated with options. slot_i is the first slot after this review area’s slots.

The review area shows the selections in its group, with write-in text for any selected write-in options. Returns slot_i + max_sels × (1 + max_chars) (47).

The review area shows the sprites for the selected options in its group.

The review area shows the write-in characters for this selected option.

Since the lists contain only valid Bindings (verifier:10, verifier:16), binding is a valid Binding.

Since the lists contain only valid Bindings (verifier:10, verifier:16), binding is a valid Binding.

Since the lists contain only valid Bindings (verifier:10, verifier:16), binding is a valid Binding.
for area in self.page.counter_areas:
    count = len(self.selections[area.group_i])
    self.video.paste(area.sprite_i + count, slot_i)
    slot_i = slot_i + 1
for area in self.page.review_areas:
    slot_i = self.review(area.group_i, slot_i, area.cursor_sprite_i)

def review(self, group_i, slot_i, cursor_sprite_i):
    group = self.model.groups[group_i]
    selections = self.selections[group_i]
    for i in range(group.max_sels):
        if i < len(selections):
            option = group.options[selections[i]]
            self.video.paste(option.sprite_i, slot_i)
            if option.writein_group_i != None:
                self.review(option.writein_group_i, slot_i + 1, None)
        if i == len(selections) and cursor_sprite_i != None:
            self.video.paste(cursor_sprite_i, slot_i)
    slot_i = slot_i + 1 + group.max_chars
    return slot_i

def press(self, key):
    for binding in self.state.bindings + self.page.bindings:
        if key == binding.key and self.test(binding.conditions):
            return self.invoke(binding)

def touch(self, target_i):
    for binding in self.state.bindings + self.page.bindings:
        if target_i == binding.target_i and self.test(binding.conditions):
            return self.invoke(binding)
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</thead>
<tbody>
<tr>
<td>56 conditions is a list of valid Conditions.</td>
<td>conditions is a list (56).</td>
<td>Returns 1 if all the conditions are met, otherwise 0 (67, 68). cond is a valid Condition (56).</td>
</tr>
<tr>
<td>58</td>
<td>cond is a valid Condition (57).</td>
<td>group_i and option_i are a valid group index and option index (116).</td>
</tr>
<tr>
<td>59</td>
<td>cond.predicate is 0, 1, or 2 (Ballot:69). PR_GROUPEMPTY is 0 (INV3).</td>
<td></td>
</tr>
<tr>
<td>60</td>
<td>group_i is the valid index of a list in self.selections (58, INV8).</td>
<td>result is 1 if the group is empty, otherwise 0.</td>
</tr>
<tr>
<td>61</td>
<td>cond.predicate is 0, 1, or 2 (Ballot:69). PR_GROUPFULL is 1 (INV3).</td>
<td>max is an int (INV4, Ballot:17, Ballot:22).</td>
</tr>
<tr>
<td>62</td>
<td>group_i is a valid group index (58).</td>
<td></td>
</tr>
<tr>
<td>63</td>
<td>group_i is the valid index of a list in self.selections (58, INV8).</td>
<td>result is 1 if the group is full, otherwise 0.</td>
</tr>
<tr>
<td>64</td>
<td>cond.predicate is 0, 1, or 2 (Ballot:69). PR_OPTIONSELECTED is 2 (INV3).</td>
<td>result is 1 if the option is selected, otherwise 0.</td>
</tr>
<tr>
<td>65</td>
<td>group_i is the valid index of a list in self.selections (58, INV8).</td>
<td></td>
</tr>
<tr>
<td>66</td>
<td>cond.invert is 0 or 1 (Ballot:72).</td>
<td>0 is returned if any condition is not met. 1 is returned if no condition is not met.</td>
</tr>
<tr>
<td>67</td>
<td>binding is a valid Binding.</td>
<td>binding is invoked. Returns None.</td>
</tr>
<tr>
<td>69</td>
<td>binding.steps is a list (69, Ballot:83).</td>
<td>step is a Step (69, Ballot:63).</td>
</tr>
<tr>
<td>70</td>
<td>step is a Step (70).</td>
<td></td>
</tr>
<tr>
<td>71</td>
<td>step is a Step (70).</td>
<td></td>
</tr>
<tr>
<td>72</td>
<td>binding.segments is a list of valid Segment (69, verifier:73).</td>
<td></td>
</tr>
<tr>
<td>74</td>
<td>Either next_page_i is None or next_page_i and next_state_i are a valid page index and state index (69, verifier:74).</td>
<td>step is a Step (70).</td>
</tr>
<tr>
<td>75</td>
<td>step is a Step (75) with a valid option reference (verifier:72).</td>
<td>The step is executed. Returns None. group_i and option_i are the group and option referenced by step (116).</td>
</tr>
<tr>
<td>77</td>
<td>group_i is a valid group index (76).</td>
<td>group is the step’s group. selections is the group’s selections. selected is 1 if the referenced option is selected, otherwise 0.</td>
</tr>
<tr>
<td>78</td>
<td>group_i is a valid index into self.selections (76, INV8).</td>
<td></td>
</tr>
<tr>
<td>79</td>
<td>option_i is an int (76). selections is a list (78).</td>
<td></td>
</tr>
<tr>
<td>80</td>
<td>step.op is 0, 1, 2, 3, or 4 (Ballot:75). OP_ADD is 0 and OP_APPEND is 2 (INV1).</td>
<td>option_i is added to the selections for group_i.</td>
</tr>
<tr>
<td>81</td>
<td>selections is a list (78). group.max_sels is an int (77, Ballot:22).</td>
<td></td>
</tr>
<tr>
<td>82</td>
<td>selections is a list (78). option_i is an int (76).</td>
<td>option_i is removed from the selections for group_i.</td>
</tr>
<tr>
<td>83</td>
<td>step.op is 0, 1, 2, 3, or 4 (Ballot:75). OP_REMOVE is 1 (INV1).</td>
<td></td>
</tr>
<tr>
<td>84</td>
<td>selections is a list (78). option_i is an int (76).</td>
<td></td>
</tr>
<tr>
<td>85</td>
<td>step.op is 0, 1, 2, 3, or 4 (Ballot:75). OP_POP is 3 (INV1).</td>
<td></td>
</tr>
<tr>
<td>86</td>
<td>selections is a non-empty list (78, 85).</td>
<td></td>
</tr>
<tr>
<td>87</td>
<td>step.op is 0, 1, 2, 3, or 4 (Ballot:75). OP_CLEAR is 4 (INV1).</td>
<td></td>
</tr>
<tr>
<td>88</td>
<td>group_i is a valid index into self.selections (76, INV8).</td>
<td></td>
</tr>
</tbody>
</table>
6. Pvote

```
def test(self, conditions):
    for cond in conditions:
        [group_i, option_i] = self.get_option(cond)
        if cond.predicate == PR_GROUP_EMPTY:
            result = len(self.selections[group_i]) == 0
        elif cond.predicate == PR_GROUP_FULL:
            max = self.model.groups[group_i].max_sels
            result = len(self.selections[group_i]) == max
        elif cond.predicate == PR_OPTION_SELECTED:
            result = option_i in self.selections[group_i]
        if cond.invert == result:
            return 0
    return 1

def invoke(self, binding):
    for step in binding.steps:
        self.execute(step)
        self.audio.stop()
        self.play(binding.segments)
        self.goto(binding.next_page_i, binding.next_state_i)

def execute(self, step):
    [group_i, option_i] = self.get_option(step)
    group = self.model.groups[group_i]
    selections = self.selections[group_i]
    selected = option_i in selections
    if step.op == OP_ADD and not selected or step.op == OP_APPEND:
        if len(selections) < group.max_sels:
            selections.append(option_i)
    if step.op == OP_REMOVE and selected:
        selections.remove(option_i)
    if step.op == OP_POP and len(selections) > 0:
        selections.pop()
    if step.op == OP_CLEAR:
        self.selections[group_i] = []
```
<table>
<thead>
<tr>
<th>PRECONDITIONS</th>
<th>REASONS FOR VALIDITY</th>
<th>POSTCONDITIONS</th>
</tr>
</thead>
<tbody>
<tr>
<td>segments is a list of valid Segments.</td>
<td>segment.type is 0, 1, 2, 3, or 4 (Ballot:81). SG_OPTION is 1 (INV2).</td>
<td>The sequence of segments is played. segment is a valid Segment (92).</td>
</tr>
<tr>
<td>selection is a list (92). segment.conditions is a list of valid Conditions (93, Ballot:80, verifier:81). self.test returns 0 or 1 (56).</td>
<td>segment.type is 0, 1, 2, 3, or 4 (Ballot:81). SG_CLIP is 0 (INV2). segment.clip_i is a valid clip index (verifier:82). segment is a valid Segment (93).</td>
<td>group_i and option_i are a valid group index and option index (116). selections is the group's selections.</td>
</tr>
<tr>
<td>selection is a list (100). option_i is a valid option index (104). segment.clip_i &lt; group.option_clips (verifier:86).</td>
<td>segment.type is 0, 1, 2, 3, or 4 (Ballot:81). SG_LIST_SELS is 2 INV2).</td>
<td>option_i is a valid option index in group group_i (INV10, 109).</td>
</tr>
<tr>
<td>option is an Option. 0 ≤ offset &lt; group.option_clips for the option's group.</td>
<td>option.clip_i + group.option_clips – 1 is a valid clip index (verifier:42) and offset &lt; group.option_clips (110) ⇒ option.clip_i + offset is a valid clip index.</td>
<td>The clip for option at offset offset is played; if it is a write-in option, the clips for the selected character options are also played, with offset 0. writein_group_i is a Group (INV4, Ballot:17).</td>
</tr>
<tr>
<td>object is a valid Condition, Step, or Segment contained within self.page.</td>
<td>object.group_i is an int or None (116). object.group_i is None (117, 119) and object is contained within self.page (116) ⇒ object.option_i is a valid option area index in self.page (verifier:70, verifier:72, verifier:81, verifier:84, verifier:91).</td>
<td>Returns a list of two ints [group_i, option_i] where group_i is a valid group index and option_i is a valid option index in that group (119, 120). area.group_i is an int (Ballot:48), so a valid group index and option index are returned (verifier:21).</td>
</tr>
<tr>
<td></td>
<td></td>
<td>object.group_i is an int (116, 117), so a valid group index and option index are returned (verifier:70, verifier:72, verifier:81, verifier:84, verifier:93).</td>
</tr>
</tbody>
</table>
```python
    def timeout(self):
        self.play(self.state.timeout_segments)
        self.goto(self.state.timeout_page_i, self.state.timeout_state_i)

    def play(self, segments):
        for segment in segments:
            if self.test(segment.conditions):
                if segment.type == SG_CLIP:
                    self.audio.play(segment.clip_i)
                else:
                    [group_i, option_i] = self.get_option(segment)

                    group = self.model.groups[group_i]
                    selections = self.selections[group_i]

                    if segment.type == SG_OPTION:
                        self.play_option(group.options[option_i], segment.clip_i)

                    if segment.type == SG_LIST SELS:
                        for option_i in selections:
                            self.play_option(group.options[option_i], segment.clip_i)

                    if segment.type == SG_COUNT SELS:
                        self.audio.play(segment.clip_i + len(selections))

        if segment.type == SG_MAX SELS:
            self.audio.play(segment.clip_i + group.max_sels)

    def play_option(self, self, option, offset):
        self.audio.play(option.clip_i + offset)

        if option.writein_group_i != None:
            writein_group = self.model.groups[option.writein_group_i]

            for option_i in self.selections[option.writein_group_i]:
                self.audio.play(writein_group.options[option_i].clip_i)

    def get_option(self, self, object):
        if object.group_i == None:
            area = self.page.option_areas[object.option_i]
        return [area.group_i, area.option_i]

        return [object.group_i, object.option_i]
```
## INVARIANTS

In an initialized `Audio.Audio` object:

**INV1.** `self.clips` is a list of `Sound` the same length as `ballot.audio.clips` (7).

**INV2.** `self.queue` is a list (8, 18).

**INV3.** Each element of `self.queue` is a valid index into `ballot.audio.clips` (10).

**INV4.** Each element of `self.queue` is a valid index into `self.clips` (by INV1 and INV3).

**INV5.** `self.playing` is an int (8, 14).

**INV6.** `self.playing` \( \neq 0 \) \( \iff \) either audio is currently playing, or it has just been stopped and an AUDIO_DONE event is pending. (Audio is only started immediately after setting `self.playing` (14). `self.playing` is updated when audio stops (main:22–23).)

**INV7.** `self.queue` is not empty \( \implies \) `self.playing` \( \neq 0 \). (Only `play()` adds to the queue (10); after doing so, it immediately updates `self.playing` (11, 12, 14).

### PRECONDITIONS

<table>
<thead>
<tr>
<th>Precondition</th>
<th>Reasons for Validity</th>
<th>Postconditions</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>pygame.USEREVENT is an int.</td>
<td>pygame is bound to the Pygame module. AUDIO_DONE is an int.</td>
</tr>
<tr>
<td>2</td>
<td>audio is a Ballot.Audio object.</td>
<td>Since sample_rate is an int (Ballot:123), rate is an int. self.clips is a list of Sound with the same length as audio.clips.</td>
</tr>
<tr>
<td>3</td>
<td>rate is an int (9). ( \iff ) if rate is not accepted as a valid sample rate.</td>
<td></td>
</tr>
<tr>
<td>4</td>
<td>audio is a Ballot.Audio (4) ( \implies ) audio.clips is a list of Ballot.Clip (Ballot:49) ( \implies ) clip.samples is a string.</td>
<td></td>
</tr>
<tr>
<td>5</td>
<td>clip_i is a valid index into ballot.audio.clips.</td>
<td>INV2.</td>
</tr>
<tr>
<td>6</td>
<td>INV2.</td>
<td></td>
</tr>
<tr>
<td>7</td>
<td>INV2.</td>
<td></td>
</tr>
<tr>
<td>8</td>
<td>INV4. self.queue is nonempty (15). INV1. The audio system has been initialized (6). The play() method of Sound returns a Channel. AUDIO_DONE is an int (2).</td>
<td></td>
</tr>
<tr>
<td>9</td>
<td>The audio system has been initialized (6). If audio is playing, this will trigger AUDIO_DONE.</td>
<td></td>
</tr>
<tr>
<td>10</td>
<td>rate is an int. data is a string.</td>
<td>Returns a Sound object for the given audio data (24).</td>
</tr>
<tr>
<td>11</td>
<td>rate is an int (20). put_int returns a string (27). fmt is a string (21).</td>
<td></td>
</tr>
<tr>
<td>12</td>
<td>fmt is a string (22). data is a string (20).</td>
<td>f = a string (21).</td>
</tr>
<tr>
<td>13</td>
<td>file is a string (23). Buffer yields a readable stream object (33). See Appendix C to verify that the WAV file passed to Sound is well-formed.</td>
<td>Returns a RIFF chunk as a string (26).</td>
</tr>
<tr>
<td>14</td>
<td>type and contents are strings.</td>
<td></td>
</tr>
<tr>
<td>15</td>
<td>type and contents are strings (28). len returns an int. put_int returns a string (27).</td>
<td>Returns the big-endian serialization of n (29). n is an int (27), so a, b, c, and d are integers (28).</td>
</tr>
<tr>
<td>16</td>
<td>data is a string.</td>
<td>self.data is a string. self.pos is an int.</td>
</tr>
<tr>
<td>17</td>
<td>length is an int. The caller will not read past the end of data. self.pos is an int (32, 34).</td>
<td>Returns the next length bytes of the buffer (35).</td>
</tr>
<tr>
<td>18</td>
<td>self.pos - length is nonnegative (34). self.data is a string (32). self.pos is no larger than the length of self.data (33).</td>
<td></td>
</tr>
</tbody>
</table>

---
import pygame

AUDIO_DONE = pygame.USEREVENT

class Audio:
    def __init__(self, audio):
        rate = audio.sample_rate
        pygame.mixer.init(rate, -16, 0)
        self.clips = [make_sound(rate, clip.samples) for clip in audio.clips]
        [self.queue, self.playing] = [[], 0]

    def play(self, clip_i):
        self.queue.append(clip_i)
        if not self.playing:
            self.next()

    def next(self):
        self.playing = len(self.queue)
        if len(self.queue):
            self.clips[self.queue.pop(0)].play().set_endevent(AUDIO_DONE)

    def stop(self):
        self.queue = []
        pygame.mixer.stop()

def make_sound(rate, data):
    [comp_channels, sample_size] = ["\x01\x00\x01\x00", "\x02\x00\x10\x00"]
    fmt = comp_channels + put_int(rate) + put_int(rate*2) + sample_size
    file = chunk("RIFF", "WAVE" + chunk("fmt ", fmt) + chunk("data", data))
    return pygame.mixer.Sound(Buffer(file))

def chunk(type, contents):
    return type + put_int(len(contents)) + contents

def put_int(n):
    [a, b, c, d] = [n/16777216, n/65536, n/256, n]
    return chr(d % 256) + chr(c % 256) + chr(b % 256) + chr(a % 256)

class Buffer:
    def __init__(self, data):
        [self.data, self.pos] = [data, 0]

    def read(self, length):
        self.pos = self.pos + length
        return self.data[self.pos - length:self.pos]
**INVARIANTS**

In an initialized `Video.Video` object:

INV1. `self.surface` is a `Surface` (7).

INV2. `self.layouts` is a list of `Layout` (9).

INV3. `self.screens` is a list of Pygame `Image` objects the same length as `video.layouts` (9).

INV4. `self.sprites` is a list of Pygame `Image` objects the same length as `video.sprites` (10).

INV5. `self.layout` is a `Layout` (13).

---

<table>
<thead>
<tr>
<th>PRECONDITIONS</th>
<th>REASONS FOR VALIDITY</th>
<th>POSTCONDITIONS</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>pygame is bound to the Pygame module.</td>
<td></td>
</tr>
<tr>
<td>2</td>
<td><code>im</code> is a <code>Ballot.Image</code>.</td>
<td>Converts raw pixel data to a Pygame <code>Image</code>.</td>
</tr>
<tr>
<td>3</td>
<td><code>im</code> is a <code>Ballot.Image</code> (2). <code>im.pixels</code> has length <code>im.width × im.height × 3</code> (verifier:67). <code>im.width</code> and <code>im.height</code> are nonzero (verifier:67).</td>
<td>pygame.image.fromstring returns a Pygame <code>Image</code>.</td>
</tr>
<tr>
<td>4</td>
<td><code>video</code> is a <code>Ballot.Video</code>.</td>
<td></td>
</tr>
<tr>
<td>5</td>
<td><code>video</code> is a <code>Ballot.Video</code> (5).</td>
<td><code>size</code> is a list of two ints (Ballot:102, Ballot:103).</td>
</tr>
<tr>
<td>6</td>
<td><code>layout_i</code> is a valid layout index.</td>
<td>INV1.</td>
</tr>
<tr>
<td>7</td>
<td><code>sprite_i</code> is a valid sprite index. <code>slot_i</code> is a valid slot index in the current layout. The sprite and slot have the same size.</td>
<td>INV2.</td>
</tr>
<tr>
<td>8</td>
<td><code>x</code> and <code>y</code> are ints.</td>
<td>INV3.</td>
</tr>
<tr>
<td>9</td>
<td><code>self.layout.targets</code> is a list (INV5).</td>
<td><code>i</code> is returned if the target contains <code>(x, y)</code>.</td>
</tr>
</tbody>
</table>
6.2.6 Video.py

```python
import pygame

def make_image(im):
    return pygame.image.fromstring(im.pixels, (im.width, im.height), "RGB")

class Video:
    def __init__(self, video):
        size = [video.width, video.height]
        self.surface = pygame.display.set_mode(size, pygame.FULLSCREEN)
        self.layouts = video.layouts
        self.screens = [make_image(layout.screen) for layout in video.layouts]
        self.sprites = [make_image(sprite) for sprite in video.sprites]
        self.goto(0)

    def goto(self, layout_i):
        self.layout = self.layouts[layout_i]
        self.surface.blit(self.screens[layout_i], [0, 0])

    def paste(self, sprite_i, slot_i):
        slot = self.layout.slots[slot_i]
        self.surface.blit(self.sprites[sprite_i], [slot.left, slot.top])

    def locate(self, x, y):
        for [i, target] in enumerate(self.layout.targets):
            if target.left <= x and x < target.left + target.width:
                if target.top <= y and y < target.top + target.height:
                    return i
```

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**INVARINTS**  
In initialized Printer objects:

**INV1**. self.text is a Ballot.Text (3).

**INV2**. Wherever line is bound, the length of line never exceeds 60 bytes. (When line is lengthened (15), it length increases by at most 51 bytes ( verifier:57). It is cleared immediately preceding this lengthening (14) if the lengthening would have increased its length to more than 60 bytes (12).

**PRECONDITIONS** | **REASONS FOR VALIDITY** | **POSTCONDITIONS**
--- | --- | ---
1. text is a Text. |  | INV1.

4. selections is a list of length(model.groups) lists, where each list contains only valid option indices for each group. selections is a list of lists (4). The selections are printed out.

5. group_i is a valid index into self.text.groups (5, INV1, verifier:5). group_i is a valid group index and selection is a list of valid option indices in that group (4).

6. group_i is a valid index into self.text.groups (5, INV1, verifier:5). group is a TextGroup (Ballot:87).

7. group/writein is an int (7, Ballot:91).

8. selection is a list (5).

9. group.name is a string (6, Ballot:90).

10. selection is a list (5).

11. group.options has the same length as model.groups[group_i].options ( verifier:55), so option_i is a valid index into group.options (5).

12. group.options is a list of strings (6, Ballot:92). option_i is a valid index into group.options (11).

13. line is a string (10, 14, 15).

14. line is a string (10, 14, 15). group.options is a list of strings (6, Ballot:92). option_i is a valid index into group.options (11).

15. line is a string (10, 14, 15).

16. line is a string (10, 14, 15).

17. selection is a list (5).

18. group.name is a string (6, Ballot:90).

19. option_i is a valid option index for group group_i (8). group.options is a list of strings (Ballot:92), so option is a string.

20. option_i is an int (20). selection is a list (5).

21. group.name is a string (6, Ballot:90).
### 6.2.7 Printer.py

```python
class Printer:
    def __init__(self, text):
        self.text = text

    def write(self, selections):
        for [group_i, selection] in enumerate(selections):
            group = self.text.groups[group_i]
            if group.writein:
                if len(selection):
                    print "\n+ " + group.name
                    line = ""
                    for option_i in selection:
                        if len(line) + len(group.options[option_i]) + 1 > 60:
                            print "= " + line
                            line = ""
                            line = line + group.options[option_i] + "~"  
                        print "= " + line  
                else:
                    if len(selection):
                        print "\n* " + group.name
                        for [option_i, option] in enumerate(group.options):
                            if option_i in selection:
                                print "- " + option
                            else:
                                print "\n* " + group.name + " ~ NO SELECTION"
                        print "\n~\n"  
```

---

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Chapter 7

Correctness claims

7.1 No negative integers

A negative integer literal occurs only once in Pvote: Audio.py, line 6, as a constant supplied to pygame.mixer.init. The unary negation operator is never used, and the binary subtraction operator is used exactly twice in Pvote:

- length is subtracted from self.pos (Audio:35), which the preceding line ensures is greater than or equal to length.
- 1 is subtracted from group.option_clips (verifier:42), which the preceding line ensures is greater than or equal to 1.

Therefore, no computations ever result in negative numbers and no variables ever take on negative values.

7.2 Navigator starts on page 0 in state 0

Initialization of the Navigator always calls self.goto(0, 0) (Navigator:10). In the goto method, page_i is 0 (not None) and self.page_i is None (which cannot equal an integer), so it proceeds to set self.page_i and self.state_i to 0, and set self.page and self.state to model.pages[0] and its states[0] respectively. Therefore, the navigator always starts on page 0 in state 0.

7.3 Ballot is committed on the last page

Only one Printer is ever instantiated (main:8). This printer is immediately passed to navigator and never referenced again in main.py. The Navigator assigns the incoming printer to self.printer, which is only ever referenced once (Navigator:14). This line can only be executed when page_i + 1 is equal to len(self.model.pages), that is, on the last page.

Also, there is only one assignment to self.page anywhere in the Navigator (Navigator:15), which is immediately preceded by a call to self.printer.write if transitioning to the last page. Thus, any transition to the last page must call self.printer.write.

Therefore, the Navigator always commits the ballot, and only commits the ballot, when it transitions to the last page.
7.4 Overvoting is impossible

There is only one place where options are ever added to the current selection (Navigator:82). The immediately preceding line ensures that the group is not full (the number of selections is less than max_sels) at that point. Therefore, the number of selections in any group cannot exceed max_sels for that group.

7.5 Contest options cannot be selected twice

There is only one place where options are added to the selection (Navigator:82). This can only be reached with a step.op equal to OP_ADD or OP_APPEND. In the case of OP_ADD, this line cannot be reached if the option to be added is already selected. Therefore, no option can appear twice in a group’s selection list unless OP_APPEND is used. The ballot definition can be examined to confirm that OP_APPEND is used only in write-in groups but never in contest groups.

7.6 Bounded function call depth

Figure 7.1 depicts all the ways Pvote routines can be called during the processing of an event received by the main event loop.

The call to review in the review method (Navigator:43) is the only recursive call. The recursive call passes a write-in group as the group_i argument to review. Since a write-in group cannot have any options that themselves have write-in groups (verifier:45–46), recursion cannot proceed more than one level deep.

The call graph otherwise contains no cycles. Inspection of the call graph shows that a call to play yields a depth of at most 4 calls; thus a call to goto yields a depth of at most 5 calls; thus a call to invoke yields a depth of at most 6 calls. Therefore, the processing of a single event cannot exceed a depth of 7 calls.

7.7 Bounded iteration

Pthin has two looping constructs, while and for. The call graph shown in Figure 7.1 is annotated with bubbles that mark every use of these constructs.

Observe that invoke and goto can each be called at most once, and play can be called at most twice. The number of iterations of any operation that can occur during the processing of a single event is therefore bounded by one of:

- a number of bindings × a number of conditions
- a number of targets
- a number of steps
- a number of groups × a number of selections
- a number of option areas
- a number of counter areas
- a number of review areas × a number of selections × a number of selections
- 2 × a number of segments × a number of conditions
- 2 × a number of segments × a number of selections × a number of selections
Figure 7.1: Call graph among Pvote routines, rooted from the event loop. Every use of iteration is indicated with a round bubble. Where a module name is not specified, the method belongs to Navigator.
7.8 At most one audio clip plays at a time

The Pygame audio system is capable of playing multiple audio clips mixed together, but we wish to avoid ever letting this happen.

To prove that Pvote only ever plays one clip at a time, imagine a token that conveys the permission to play audio. Only one token exists, and it is passed back and forth between Pvote’s Audio object and the Pygame audio system. The playing field of the Audio object represents whether it possesses the token. If playing = 0, then Pvote has the token; otherwise, Pygame has the token. Starting playback of an audio clip with the play method of a Sound object should pass the token from Pvote to Pygame. Receiving an AUDIO_DONE event from Pygame should pass the token from Pygame to Pvote.

Now let us verify that Pvote actually upholds this model. The Pvote Audio object initializes self.playing to 0, so it initially holds the token (Audio:8). Sound playback is only ever initiated by next method (Audio:16), which can be called in exactly two ways. Either play calls next (Audio:12), which can only happen when self.playing is 0 (i.e. Pvote already holds the token); or the main loop calls next upon receiving an AUDIO_DONE event (main:22–23) (i.e. Pygame has just passed the token to Pvote). Thus, Pvote only initiates playback when it holds the token.

We can also confirm that Pvote accurately tracks whether it holds the token. Sound playback can be initiated only when self.queue is not empty (Audio:15–16), which means self.playing must be set to a nonzero value (Audio:14). Thus, Pvote relinquishes the token when it initiates audio playback.

self.playing is set only upon a call to next (Audio:14). If next is called by play, then Pvote must already have the token (Audio:11). The only other possibility is that next is called by the main loop due to the receipt of an AUDIO_DONE event. Thus, Pvote can acquire the token only when Pygame notifies it that audio playback has stopped.

7.9 Timeout occurs after timeout_ms ms of idle silence

If timeout_ms ms passes with no events and no audio output, the Pygame timer will send a TIMER_DONE event (main:12–13) and audio.playing will be zero, so the timeout behaviour will be triggered (main:24–25).

The Pygame timer is set to run only while Pvote is waiting for an event (main:12, main:14), so a TIMER_DONE event can only occur when timeout_ms ms has passed with no other events occurring. In particular, this includes AUDIO_DONE events, so no sound can have finished playing during the last timeout_ms ms. For the timeout behaviour to be triggered there must not be a sound currently playing (main:24). Therefore, the audio output must have been silent for the last timeout_ms ms.

7.10 Ballot definition is never changed

Inspection of the code shows that, during event processing, assignments are never made and methods are never called on objects in the ballot definition.
7.11 Responsibilities established

R1. Never abort during a voting session.

Termination of a Pthin program can occur in the following ways:

1. Execution reaches the end of the main program.
2. Illegal types of operands are supplied to an expression.
3. A precondition for an expression is violated.
4. A precondition for a library routine is violated.
5. An incorrect number of arguments is passed to a function or method.
6. An assertion fails.
7. Memory is exhausted.

Cause 1: Due to the infinite event loop, execution never reaches the end of the main program (main:10).

Causes 2 through 6: The annotations in the source code identify all the possible places where these kinds of errors can occur. These appear in the ballot loader, the verifier, and the initialization routines for the audio driver and video driver, all of which execute on startup before the voting session begins. After these routines have successfully completed executing, it has been established (mainly by the verifier) that these kinds of errors cannot occur at a later point.

Cause 7: By the memory management rules in section 3.8, memory stays allocated only by binding values to names, placing values in lists, creating cyclic reference chains, or passing values as arguments. Static analysis of the program can determine the total number of global names, local names, and field names used, so the space used by bindings is bounded.

Only strings and lists have variable size. Strings are never manipulated during event processing except when printing the ballot; we will establish for R10 that Printer never constructs a string longer than 70 bytes. Lists are made longer only in two places: the execute method in Navigator appends to the current selection (Navigator:82), and the play method in Audio appends to the play queue (Audio:10). The lengths of selection lists are bounded by max_sels (Navigator:81). Examination of the call graph (Figure 7.1) shows that Audio.play is only called by Navigator.play, which can only be called by timeout, invoke, or goto, which is itself called only by timeout or invoke. timeout can only be called when the play queue is empty (main:24–25), and invoke clears the play queue before adding anything to it (Navigator:72). Since we can see that the number of calls to Audio.play from Navigator.play is bounded, the length of the play queue is bounded.

Cyclic reference chains can only created via list containment or object fields. During event processing, lists or objects are never placed into lists, and assignments to object fields (Audio:14, Audio:18, Navigator:15, Navigator:16, Video:13) always assign integers, empty lists, or elements of the ballot definition, which are never mutated.

Finally, Section 7.6 established a bound on the depth of the call stack, and the size of each stack frame is predetermined by the number of arguments and local names in each function or method.

Thus, Pvote’s maximum memory usage is determined by the ballot definition.
R2. Remain responsive during a voting session.

For an interactive program, “responsive” means that the program is always ready to process user input within a reasonably short time. We are concerned specifically with the code that runs in a voting session—that is, just the main loop, not including the initialization steps that happen before it. Since Pvote’s main loop alternates between waiting for events and processing events, responsiveness depends on the time required to process each event.

We assume that it takes a negligible time to evaluate individual expressions in Pthin. Of all the Pygame functions used during the main loop, only the Surface method `blit()` does a variable amount of work; its work is proportional to the area of the pasted sprite. The verifier ensures that sprites fit into their slots (verifier: {13, 22, 26, 30, 33, 36, 39–40, 48, 49–52}) and that slots can be no larger than the screen resolution (verifier: 61–62), so the area of pasted sprites is bounded by the area of the screen. Thus, we also assume that it takes a negligible time to invoke individual Pygame functions.

There are less than 500 lines of code in Pvote, which isn’t enough for straight-line execution to cause an appreciable delay; only loops could result in enough latency to make Pvote unresponsive. Loops can arise from Pthin’s two looping statements (`while` and `for`) and from recursive function calls. Section 7.6 showed that function call depth is bounded by a constant, and Section 7.7 showed that iteration counts are bounded by parameters in the ballot definition file.

Therefore, there is an upper bound on the time it takes to process each event that depends on the length of lists in the ballot definition. Keeping the sizes of these lists small will ensure that Pvote always stays responsive.

R3. Become inert after a ballot is committed.

As established in Section 7.3, the ballot is only committed upon arrival at the last page, where `self.page_i` becomes `len(self.model.pages) - 1` (Navigator: 13–15). Thereafter, the page and state can never change again, since they can only change if `self.page_i != len(self.model.pages) - 1` (Navigator: 12, Navigator: 15–16). Thus, the ballot can never be committed more than once.

To ensure that Pvote becomes totally inert, one could examine the ballot definition to see that there are no bindings defined for the last page. As the only incoming messages to the navigator are `press` (main:16), `touch` (main:21), and `timeout` (main:25), eliminating bindings would guarantee that only `timeout` would ever get called after that point. The `timeout` method can only play audio and call `goto`, which would not cause a page or state transition because `self.page_i == len(self.model.pages) - 1`.

R4. Display a completion screen when and only when a ballot is committed, and continue to display this screen until the next session begins.

As established in Section 7.3, the ballot is committed upon and only upon arrival at the last page. The last page’s screen is the completion screen. Since no more transitions can happen after the last page is reached, this screen remains on the display until Pvote is restarted.

It is up to the author of the ballot definition to ensure that the completion screen has a distinct appearance.
R5. **Exhibit behaviour in each session independent of any previous sessions.**

By design, Pvote is restarted for each voting session and does not read from any external storage except for the ballot definition, which it never rewrites, so it cannot carry any state from previous voting sessions.

R6. **Exhibit behaviour independent of which parts of buttons are touched.**

Incoming touch events are processed only by a single clause in the main event loop (main:17–21). This clause translates the touch coordinates into a target index by calling `locate` on the `Video` object, which has no side effects (Video:19–22). Only this target index is then passed on to the `Navigator`. Therefore, within a given target, all touch coordinates have the same effect. It is up to the author of the ballot definition to ensure that the targets have reasonable sizes and locations.

R7. **Exhibit behaviour that is determined entirely by the ballot definition and the stream of user input events and their timing.**

Pvote is single-threaded, uses no shared memory, and does not access the clock or any sources of randomness, so its behaviour is deterministic except for information introduced by the incoming event stream. The incoming event stream contains user-generated events, `TIMER_DONE` events, and `AUDIO_DONE` events. `TIMER_DONE` events are determined entirely by the timing of user-generated events and the `timeout_ms` parameter. `AUDIO_DONE` events are determined entirely by the processing of other events and the length of audio clips in the ballot definition. Therefore, given the same sequence and timing of user input events and the same ballot definition, Pvote will always exhibit the same behaviour.

R8. **Commit valid selections.**

Invariant INV8 in the `Navigator` establishes that `self.selections` is always a list of lists, with one list per group. This format ensures that the selection data passed to the `Printer` cannot express any groups (contests or write-ins) other than those specified in the ballot definition. Any option appended to a selection list is an option referenced in a `Step` (Navigator:76, Navigator:82). The verifier ensures that this option reference is valid, whether it is a direct reference (verifier:72) or an indirect reference through an option area (verifier:91, verifier:21). Section 7.4 establishes that overvotes cannot occur. It is up to the author of the ballot definition to ensure that the `Text` data accurately represents the contests and options.

R9. **Commit the ballot when and only when so requested by the voter.**

Section 7.3 established that the ballot is committed when and only when there is a transition to the last page. That is as much as can be upheld by technical means; only a human can verify that the voter’s expectations about committing are met.

To ensure this, one must examine the ballot definition to see that all keys and targets that cause transitions to the last page are clearly identified to the voter (visually and aurally) that they will commit the ballot. Also, no other keys or targets should be presented in a way that implies they will commit the ballot, and no visual display or audio feedback should falsely indicate that the ballot has been committed when it has not.

To minimize the possibility of voter error, one can examine the ballot definition to see that there is adequate confirmation before entering any page or state with a binding that causes a transition to the last page.
R10. Correctly and unambiguously commit the selections the voter made.
This requires establishing four things:

1. Selection and deselection of options indeed occurs correctly according to user actions. This is argued below for R13.
2. The ballot is committed when and only when the voter so requests. This is argued above for R9.
3. The printed selections are accurate. Printing occurs in the write method (Printer:4–25).
   - Every write-in group with a nonzero number of selected options causes the first loop to be executed (Printer:11–15). This loop proceeds through the character options in the order they were selected, and adds each option in the write-in to line exactly once (Printer:15). Anything that is added to line is printed exactly once (Printer:13–14, Printer:16).
   - Every contest group with a nonzero number of selected options causes the second loop to be executed (Printer:20–22). This loop proceeds through options in their order in the Group (Printer:20). Since all the option indices in the selection list must be valid (R8), every option that is present in the selection list will be printed exactly once (Printer:21).

4. The printed selections are unambiguous. Since the print statement always finishes its output with a newline, everything printed by print starts on a new line. Because group and options names are at most 50 bytes long (verifier:54, verifier:57), no string constructed in Printer ever exceeds 70 bytes in length (Printer:9, Printer:12–15, Printer:16, Printer:19, Printer:22, Printer:24). All the strings sent to print contain only printable ASCII characters (Ballot:134). Therefore, as long as the printing hardware can fit 70 characters across the page, no group or option names will wrap. Thus, every printed line can be identified by its first character:
   - + introduces the name of a write-in group (Printer:9).
   - = introduces the content of a write-in (Printer:13, Printer:16).
   - * introduces the name of a contest group (Printer:19, Printer:24).
   - - introduces the name of an option (Printer:22).
   - ~ marks the end of the ballot.

Therefore, if all the TextGroups in the ballot definition have unique names, the groups can be uniquely identified on the printout. Also, options in a contest group are printed separated by newlines, and options in a write-in group are printed separated by tildes (ASCII 126), which are not allowed in option names (Ballot:134). Therefore, if all the options in each TextGroup have unique strings, the options can be uniquely identified on the printout.

R11. Present instructions, contests, and options as specified.
The instructions, contests, and options are prerendered images embedded in the ballot definition. Thus, as long as the text and other information in the images is correct, it will be displayed correctly.
R12. Navigate among instructions, contests, and options as specified.

Navigation occurs only by the goto method, which is called whenever a binding is invoked (Navigator:74) and whenever a timeout occurs (Navigator:91). As long as the destination page and state are specified correctly in the ballot definition, the transition will occur to the correct page and state (Navigator:12–16).

R13. Select and deselect options according to user actions as specified.

Selection and deselection occurs entirely within the execute method, which can only be called in response to the invocation of a binding (Navigator:71), and a binding can only be invoked in response to a user action (Navigator:51, Navigator:55). If the selection steps in bindings are specified correctly in the ballot definition, then the correct selection or deselection operations will take place (Navigator:76–88).

R14. Correctly indicate whether options are selected when directed to do so.

R15. Correctly indicate how many options are selected when directed to do so.

R16. Correctly indicate which options are selected when directed to do so.

The update method in Navigator is called whenever goto is called (Navigator:18), and goto is always called each time a binding is invoked (Navigator:74) or a timeout is received (Navigator:91). The update method always redraws everything on the screen. It first pastes the current layout’s full-screen image (Navigator:20, Video:14). Then it pastes the state’s sprite (Navigator:21).

The indication of whether options are selected is determined by the flag unselected (Navigator:24), which chooses between the selected and unselected sprites for each option area. As long as the option area points to the correct option and the option points to the correct sprite_i, this will be displayed correctly.

The indication of how many options are selected is determined by the count variable (Navigator:30), which is added to a counter area’s sprite_i to select the sprite to display. As long as the counter area points to the correct group and sprite index, this will be displayed correctly.

The indication of which options are selected is done by the review method. Calls to paste appear exactly twice in this method: once for option sprites (Navigator:41) and once for the cursor sprite (Navigator:45). The option sprite is option.sprite_i, the selected sprite for an option, and the option is taken directly from the selection list (Navigator:40). So it cannot display any unselected options. On the other hand, the paste operation is executed once for every option in the selection list, since the number of selections cannot exceed max_sels and i takes on every value from 0 to max_sels − 1.
Appendix A

Glossary

ballot style: A combination of contests and options (for a particular set of voters).
binding: A triple of stimulus, condition, and response.
committed: A ballot is committed when the selection of votes is finalized. For a DRE, a ballot is committed when it is recorded. For a ballot printing or marking device, a ballot is committed when it is printed.
condition: A logical predicate concerning the current selection state.
contest: A race or a proposition.
contest group: A group representing a contest on the ballot, where the options are candidates or referendum choices.
empty: A group, contest, or write-in is empty when it has no options selected.
full: A group, contest, or write-in is full when the maximum options are selected.
group: A set of options that can be selected (see contest group and write-in group).
invoke: To invoke a binding is to carry out the response it specifies.
match: A binding matches when its specified stimulus matches the input received.
operative: A binding is operative when all its conditions are satisfied.
option: A choice in a group (a candidate in a race for office, one of the choices for a proposition, or a character that can be entered for a write-in).
overvote: Selecting more than the maximum allowed number of selections in a particular contest.
response: A system behaviour in response to user input (e.g. changing a selection, navigating to another page, or playing audio).
selection: An option that is currently selected.
selection state: The list of options that are selected in each group.
stimulus: An instance of user input (e.g. a keypress or a screen touch).
undervote: Selecting fewer than the maximum allowed number of selections in a particular contest.
write-in group: A group representing the text written into a single write-in option, where the options are characters.
write-in option: An option that allows a candidate’s name to be written in.
voting session: The period from when a voter starts interacting with a voting machine until a ballot is committed or the voter abandons the machine.
Appendix B

Deployment example

To evaluate Pvote, it may help to have in mind some context in which it will be used. Here is just one example of a possible deployment scenario for an electronic ballot printer based on Pvote.

B.1 Before election day

The ballot definition files are prepared and widely published, along with their hashes, before election day.

B.2 Election day before polls open

The polling place is divided into three areas: the public area, where anyone can stand, the voting area, which voters are permitted to enter after they have been authorized to vote by pollworkers, and the private area, which is accessible to pollworkers only.

The voting area contains any number of voting stations. Each voting station has a touchscreen, a pair of headphones, a keypad, and a printer. There is a shield or curtain around the station to protect the voter’s privacy. The voting stations are stateless.

The private area contains a ballot scanner and a number of bins for flash cards (one bin for each ballot style to be used at that polling place). Before opening the polls, the pollworkers use a flash station to prepare some flash cards for each ballot style. The flash station can be an ordinary PC. For each ballot style, a pollworker carries out the following steps:

1. Load the ballot definition file onto the flash station. The flash station displays the hash of the file.
2. Verify the computed hash against the published hash.
3. Insert flash cards one by one. The flash station erases each card and copies the file onto the card.
4. Label each flash card according to its ballot style.
5. Deposit each flash card in the bin for its ballot style.
The pollworkers can then shut down the flash station, or leave it set up in case they want to be able to prepare flash cards on the fly with other ballot styles throughout the day (e.g. for the occasional voter at the wrong polling place). After the flash cards are prepared, the polling place is opened.

B.3 Election day with polls open

The voting procedure for each voter is as follows:

1. The voter lines up to be authorized to vote.
2. After checking that the voter is authorized and determining which ballot style the voter should get (which might depend on the voter’s party affiliation or address), the pollworker takes a flash card from the appropriate bin.
3. The pollworker proceeds with the voter to any available voting station and inserts the card. The pollworker inserts a key into the station and turns it, which aborts and restarts Pvote. Pvote loads the ballot definition from the card on startup. Once the initial screen appears, the pollworker removes the card, walks away, and returns the card to its bin.
4. The voter privately interacts with Pvote to make selections on the ballot. When the final screen is reached, the voter’s selections are printed out on a paper ballot.
5. The voter verifies the paper ballot.
6. The voter carries the paper ballot (covered in a privacy folder) to the ballot scanner and places it in the scanner. The scanner records the actual scanned image of the paper ballot.

B.4 Election day after polls close

The counts reported by the ballot scanner are posted locally at each polling place. Each polling place posts its counts on a public website.

Each polling place also posts encrypted files containing the scanned images of its paper ballots on the public website. An openly chosen random sample of the polling places, as well as any polling places with a sufficiently narrow margin of victory, post their scanned images of paper ballots without encryption. Members of the public can run their own OCR software to verify the counts.

After 3 years, the encryption keys are published so the entire election can be verified by the public.
Appendix C

WAV audio file format

The essential elements of the Microsoft WAV file format are as follows:

- All integers are represented in little-endian order.
- A chunk is a block of data preceded by an 8-byte header. The first 4 bytes of the header are a chunk type identifier, and the next 4 bytes give the length of the data block, not including the header.
- A WAV file consists of a chunk of type "RIFF" that contains the 4-byte string "WAVE" followed by other chunks.
- The minimal two required chunks are a "fmt " chunk and a "data" chunk.
- The "fmt " chunk contains this 16-byte structure:

<table>
<thead>
<tr>
<th>Size</th>
<th>Contents</th>
</tr>
</thead>
<tbody>
<tr>
<td>2 bytes</td>
<td>compression type (1 for none)</td>
</tr>
<tr>
<td>2 bytes</td>
<td>number of channels (1 for mono, 2 for stereo)</td>
</tr>
<tr>
<td>4 bytes</td>
<td>number of samples per second</td>
</tr>
<tr>
<td>4 bytes</td>
<td>number of bytes per second</td>
</tr>
<tr>
<td>2 bytes</td>
<td>number of bytes per sample × number of channels</td>
</tr>
<tr>
<td>2 bytes</td>
<td>number of bits per sample</td>
</tr>
</tbody>
</table>

- The "data" chunk contains the audio sample data. For 16-bit samples, each sample is a signed little-endian 16-bit value.